



# SNS COLLEGE OF ENGINEERING

Kurumbapalayam (Po), Coimbatore - 641 107

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Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRICAL AND ELECTRONICS ENGINEERING

COURSE NAME : 19EE504 SPECIAL ELECTRICAL MACHINES

III YEAR / Vth SEMESTER EEE

Unit 1 - PMBLDC

By

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## Chapter: Special Electrical Machines : Permanent Magnet Brushless D.C. Motors

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### EMF EQUATION OF BLPM SQW DC MOTORS

The basic torque emf equations of the brushless dc motor are quite simple and resemble those of the dc commutator motor.

The co-ordinate axis have been chosen so that the center of a north pole of the magnetic is aligned with the x-axis at  $\Theta = 0$ . the stator has 12 slots and a three phasing winding. Thus there are two slots per pole per phase.

∨ Consider a BLPM SQW DC MOTOR

Let 'p' be the number of poles (PM)

' $B_g$ ' be the flux density in the air gap in wb/m<sup>2</sup>.

$B_k$  is assumed to be constant over the entire pole pitch in the air gap ( $180^\circ$  pole arc)

'r' be the radius of the airgap in m.

'l' be the length of the armature in m.

'T<sub>c</sub>' be the number of turns per coil.

'ω<sub>m</sub>' be the uniform angular velocity of the rotor in mechanical rad/sec.

ω<sub>m</sub>=2πN/60 where N is the speed in rpm.

Flux density distribution in the air gap is as shown in fig 4.14. At t=0 (it is assumed that the axis of the coil coincides with the axis of the permanent magnet at time t=0).

Let at ω<sub>mt</sub>=0, the centre of N-pole magnet is aligned with x-axis.

At ω<sub>mt</sub>=0, x-axis is along PM axis.

Therefore flux enclosed by the coil is

$$\Phi_{\max} = B \times 2\pi r / p \times l \quad \dots\dots\dots(4.1)$$

= flux/pole

$$\Phi_{\max} = r \int_0^{\pi} B(\theta) d\theta$$

$$= B_g r [\theta]_0^{\pi}$$

$$= B_g r [\pi]$$

At ω<sub>mt</sub>=0, the flux linkage of the coil is

$$\Lambda_{\max} = (B_g \times 2\pi r / p \times l) T_c \omega_b - T \quad \dots\dots\dots(4.2)$$

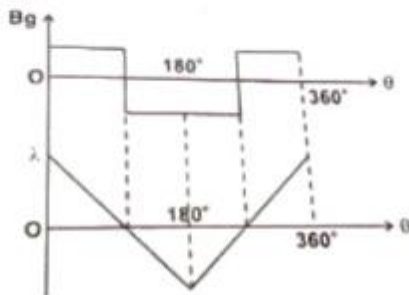


Fig 4.14 Magnetic Flux Density around the Air gap.

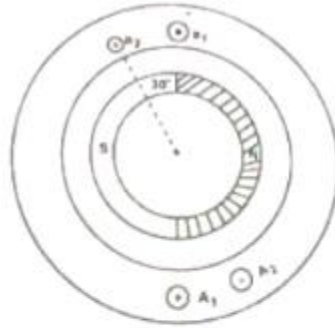


Fig 4.15 Motor Showing two Coils of One Phase.

Let the rotor rotating in ccw direction and when  $\omega_{ml} = \pi/2$ , the flux enclosed by the coil  $\Phi$ ,  
Therefore  $\lambda = 0$ .

The flux linkages of the coil vary with  $\theta$  variation of the flux linkage is as shown above.

The flux linkages of the coil changes from  $B_g r l T c \pi / p$  at  $\omega_{ml} = 0$  (i.e)  $t = 0$  to  $\theta$  at  $t = \pi / p \omega_m$ .

Change of flux linkage of the coil (i.e)  $\Delta \lambda$  is

$\Delta \lambda / \Delta t = \text{Final flux linkage} - \text{Initial flux linkage} / \text{time}$ .

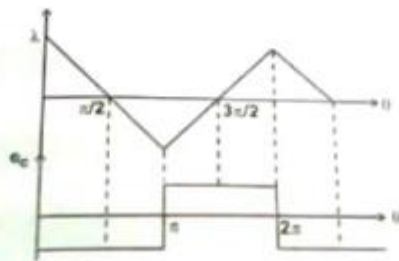
$$= 0 - (2B_g r l T c \pi / p) / (\pi / p \omega_m)$$

$$= -(2B_g r l T c \omega_m) \dots \dots \dots (4.3)$$

The emf induced in the coil  $e_c = -d\lambda / dt$

$$e_c = 2B_g r l T c \omega_m \dots \dots \dots (4.4)$$

Distribution of  $e_c$  with respect to  $t$  is shown in fig 4.16



Consider two coils a1A1 and a2A2 as shown in fig 5.15. Coil a2A2 is adjacent to a1A1 is displaced from a1A1 by an angle  $30^\circ$  (i.e.) slot angle  $\gamma$ .

The magnitude of emf induced in the coil a1A1

$$e_{c2} = B_g r l T c \omega_m \text{ volts} \dots\dots\dots(4.6)$$

The magnitude of emf induced in the coil a2A2

$$e_{c2} = B_g r l T c \omega_m \text{ volts} \dots\dots\dots(4.7)$$

Its emf waveform is also rectangular but displaced by the emf of waveform of coil  $e_{c1}$  by slot angle  $\gamma$ .

If the two coils are connected in series, the total phase voltage is the sum of the two separate coil voltages.

$$e_{c1} + e_{c2} = 2B_g r l T c \omega_m \dots\dots\dots(4.8)$$

Let  $n_c$  be the number of coils that are connected in series per phase  $n_c T_c = T_{ph}$  be the

number of turns/phase.

$$e_{ph} = n_c [2B_g r l T c \omega_m] \dots\dots\dots(4.9)$$

$$e_{ph} = 2B_g r l T_{ph} \omega_m \text{ volts} \dots\dots\dots(4.10)$$