## Tutorial-1

1. A random variable $x$ has the following probability distribution

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $P(x)$ | 0 | $K$ | $2 K$ | 2 K | 3 K | $\mathrm{~K}^{2}$ | $2 \mathrm{~K}^{2}$ | $7 \mathrm{~K}^{2}+\mathrm{K}$ |

(i) Find the value of K
(ii) Evaluate $\mathrm{P}[\mathrm{X}<6]$ and $\mathrm{P}[\mathrm{X} \geq 6$ )
(iii) If $\mathrm{P}[\mathrm{X} \geq \boldsymbol{C})>1 / 2$ find minimum value of C
(iv) Evaluate $\mathrm{P}[1.5<\mathrm{x}<4.5 / \mathrm{x}>2$ ]
2. A random variable $X$ has the following probability distribution.

| x | -2 | 1 | 0 | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{P}(\mathrm{x}$ <br> $)$ | 0.1 | K | 0.2 | 2 K | 0.3 | 3 K |

(i) Find K
(ii) Evaluate $\mathrm{P}(\mathrm{x}<2)$ and $\mathrm{P}(-2<\mathrm{x} \leq 2)$
(iii) Find the Cumulative distribution of $x$.

Evaluate the mean of $x$
3. A bolt is manufactured by 3 machines A, B, and C. A turns out twice as many items as B and machines B and C produce equal number of items. $2 \%$ of bolts produced by A and B are defective and $4 \%$ of bolts produced by C are defective. All bolts are put into 1 stock pile and 1 is chosen from this pile. What is the probability that it is defective?
4. An urn contains 10 white and 3 black balls. Another urn contains 3 white and 5 black balls. Two balls are drawn at random from the first urn and placed in the second urn and then 1 ball is taken at random from the latter. What is the probability that it is a white ball?

