

I A E - I Answer key

Statistics and Numerical Methods

Part A.

Type I Error: Acceptance of H_0 when it is false.

Type II Error: Rejection of H_0 when it is true.

It is used to test the significance of the difference between two sample means.

To test the significance of an observed sample correlation coefficient and sample regression coefficient

$$E(a) = \frac{(a+b)(a+c)}{N}$$

$$E(b) = \frac{(a+b)(b+d)}{N}$$

$$E(c) = \frac{(a+c)(c+d)}{N}$$

$$E(d) = \frac{(c+d)(b+d)}{N}$$

$$N = \frac{(a+b+c+d)(ad-bc)^2}{(a+c)(b+d)(a+b)(c+d)}$$

Randomization

Replication

Local control.

5. Completely Randomized Design
Randomized Block Design
Latin Square Design.

Part B.

$$6) a) n_1 = 6 \quad n_2 = 7$$

$$\bar{x}_1 = 22.3 \quad \bar{x}_2 = 34.42$$

$$\sum (x_1 - \bar{x}_1)^2 = 81.34$$

$$\sum (x_2 - \bar{x}_2)^2 = 133.72$$

$$S_1^2 = \frac{\sum (x_1 - \bar{x}_1)^2}{n_1 - 1} = \frac{81.34}{5} = 16.27$$

$$S_2^2 = \frac{133.72}{6} = 22.29$$

$$H_0: \sigma_1^2 = \sigma_2^2$$

$$H_1: \sigma_1^2 \neq \sigma_2^2$$

$$\text{LOS: } 5-1. \quad \text{Dof: } v_1 = 5 \quad v_2 = 6$$

$$T.V (6, 5) = 4.95$$

Test Statistics.

$$S_2^2 > S_1^2$$

$$F = \frac{S_2^2}{S_1^2} = \frac{22.29}{16.27} = 1.37$$

$$C.V < T.V$$

$$1.37 < 4.95 \quad H_0 \text{ accepted}$$

6) $\bar{x} = 97.2$
 b) $(x - \bar{x})^2 = 1833.6$
 i) $S^2 = \frac{\sum (x_i - \bar{x})^2}{n-1} = 203.78$

$S = \sqrt{203.78} = 14.27$

$H_0: \mu = 100$

$H_1: \mu \neq 100$

LOS: $\alpha = 5\%$ Dof = $10 - 1 = 9$

T.V = 1.833

Test Statistics

$t = \frac{\bar{x} - \mu}{S/\sqrt{n-1}}$

$t = -0.588$

$|t| = 0.588$

C.V < T.V

H_0 accepted

O	E	(O-E)	(O-E) ²
30	20	10	100
25	20	5	25
18	20	-2	4
10	20	-10	100
22	20	2	4
15	20	-5	25
120	120		258

C.V T.V

12.9 > 11.07

H_0 is rejected

7) a) $n = 900$ $\sigma = 2.61$
 $\bar{x} = 3.4$ $\mu = 3.25$

$H_0: \mu = 3.25$

$H_1: \mu \neq 3.25$

LOS: 5% T.V = 1.96

Test Statistics:

$z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}} = \frac{3.4 - 3.25}{2.61/\sqrt{900}}$

$z = 1.72$

$|z| = 1.72$

Conclusion: C.V T.V

1.72 < 1.96

H_0 accepted

ii) $n = 6$

H_0 : The die is biased

H_1 : The die is unbiased

LOS: 5% dof = $n - 1 = 5$

Test Statistics

$\chi^2 = \sum \frac{(O-E)^2}{E}$

$= \frac{258}{20} = 12.9$

D) ii)

H_0 : Attributes are independent.

H_0 : Attributes are not independent.

LOS $\alpha = 5\%$.

$$\text{Dof: } (r-1)(c-1) = 1$$

$$\text{T.V} = 3.841$$

$$E(620) = 585$$

$$E(380) = 415$$

$$E(550) = 585$$

$$E(450) = 415$$

O	E	(O-E)	(O-E) ² /E
620	585	35	2.09
380	415	-35	2.95
550	585	-35	2.09
450	415	35	2.95
			$\chi^2 = 1.08$

$$C.V > \text{T.V}$$

H_0 Rejected.

Part: B.

$$n_1 = 10 \quad n_2 = 8$$

$$\bar{x}_1 = 6.4 \quad \bar{x}_2 = 5$$

$$\sum (x_1 - \bar{x}_1)^2 = 102.4$$

$$\sum (x_2 - \bar{x}_2)^2 = 82$$

$$H_0: \mu_1 = \mu_2$$

$$H_1: \mu_1 \neq \mu_2$$

LOS: $\alpha = 5\%$

$$\text{Dof } V_1 = 9, V_2 = 7$$

$$\text{T.V}(7,9) = 3.29$$

Test statistics.

$$F = \frac{S_2^2}{S_1^2} = \frac{11.71}{11.37} = 1.029$$

$$C.V < \text{T.V}$$

H_0 is accepted.

b) H_0 : There is no significant difference

H_1 : There is significant difference

$$N = 10$$

$$\bar{T} = 40$$

$$\frac{\bar{T}^2}{N} = 160$$

$$\begin{aligned} \text{TSS} &= \sum X_1^2 + \sum X_2^2 + \sum X_3^2 - \frac{\bar{T}^2}{N} \\ &= 40 \end{aligned}$$

$$\begin{aligned} \text{SSC} &= \frac{(\sum X_1)^2}{10} + \frac{(\sum X_2)^2}{10} + \frac{(\sum X_3)^2}{10} - \frac{\bar{T}^2}{N} \\ &= 6 \end{aligned}$$

$$\text{SSE} = \text{TSS} - \text{SSC} = 34$$

$$\text{MSC} = \frac{\text{SSC}}{c-1} = 3$$

$$\text{MSE} = \frac{\text{SSE}}{N-c} = 4.86$$

Source of Variation	Sum of Squares	df	MSS	Variance ratio	Table Value
B+ Columns	SSC = 6	$C-1$ = 2	MST = 3	$F_c = \frac{MSE}{MST}$ = 1.62	$F_T(7, 2)$ = 19.35
Error	SS.E = 34	$N-C$ = 7	MSE = 4.86		

H_0 accepted $C.V < T.V$.