

SNS COLLEGE OF ENGINEERING Kurumbapalayam (Po), Coimbatore – 641 107



AN AUTONOMOUS INSTITUTION

Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A' Grade Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

Topic: 3. 7 – PROPERTIES OF EVOLUTES

(8) 1. The normal at any point of a curve is a tangent to its evolute tourning at the concerponding centre of curvature. 2. The difference blue the radius of

to the length of the arc of the evolute between the two corresponding points.

3. There is one evolute but an infinite number of involutes. (i) The Normals to a cuave are the targents to its Evolute.

to its Evolute. (ii) The evolute of a family of curves touches at each of its points the corresponding member of that family.



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1. Show that the evolute of the cycloid

$$x = a (0 - \sin \theta); \quad y = a(1 - \cos \theta) \quad zs \quad another
equal cycloid.
$$\frac{d n}{d \theta} = a (1 - \cos \theta); \quad y = a(1 - \cos \theta)$$

$$\frac{d n}{d \theta} = a (1 - \cos \theta); \quad \frac{d y}{d \theta} = a \sin \theta$$

$$\frac{d y}{d \theta} = \frac{a \sin \theta}{a(1 - \cos \theta)} = \frac{\sin \theta}{1 - \cos \theta}$$

$$\frac{y_1}{a \sin^2 \theta_2} = \frac{\sin \theta}{1 - \cos \theta}$$

$$\frac{y_2}{a \sin^2 \theta_2} = \cos \theta \frac{y_2}{a \sin^2 \theta_2}$$

$$\frac{y_2}{a \sin^2 \theta_2} = \frac{1}{a \sin^2 \theta_2}$$

$$\frac{z - \cos 2e^2 \theta}{a \sin^2 \theta_2} = -\frac{1}{a \sin^2 \theta_2}$$

$$\frac{z - \frac{y_1}{y_2} (1 + y_1^2)}{y_2}$$

$$= a (\theta - \sin \theta) - \frac{\cos \theta}{a \sin^2 \theta_2} (- \tan \sin^2 \theta_2) \frac{(1 + \cos^2 \theta_2)}{(\sin^2 \theta_2)}$$$$



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$$= a (0 - \sin \theta) + 4a \sin \theta_{2} \cdot \cos \theta_{2}$$

$$= a (\theta - \sin \theta) + 2a \sin \theta$$

$$= a [\theta - \sin \theta + 2 \sin \theta]$$

$$\overline{x} = a [\theta + \sin \theta] \rightarrow 0$$

$$\overline{y} = y + \frac{1}{y_{2}} (i + y_{1}^{2})$$

$$= a (1 - \cos \theta) + (4a \sin^{2} \theta_{2}) (1 + \cos^{2} \theta_{2})$$

$$= a (1 - \cos \theta) - 4a \sin^{2} \theta_{2} \left(\frac{\sin^{2} \theta + \cos^{2} \theta_{2}}{\sin^{2} \theta_{2}} \right)$$

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$$= a (1 - \cos \theta) - 4a (1 - \cos \theta)$$

$$= a (1 - \cos \theta) - 2a (1 - \cos \theta)$$

$$\overline{y} = -a [1 - \cos \theta] \rightarrow 0$$
From () $A = we get$

$$\lambda = a (\theta + \sin \theta) ; \quad y = a (1 - \cos \theta)$$
this supresents the equation of another cycloid.