

SNS COLLEGE OF ENGINEERING Kurumbapalayam (Po), Coimbatore – 641 107



AN AUTONOMOUS INSTITUTION

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Topic: 3. 6 - EVOLUTES

6. Find the evolute of the hyperbola
$$2^2 - y^2$$

The parametric equation of the hyperbola.

 $X = a \sec \theta$; $y = b \tan \theta$.

 $\frac{dx}{d\theta} = a \sec \theta \tan \theta$; $\frac{dy}{d\theta} = b \sec^2 \theta$.

 $y_1 = \frac{b \sec^2 \theta}{a \sec \theta + a \cos \theta} = \frac{1}{a \cos \theta} \cdot \frac{\cos \theta}{\sin \theta}$
 $y_2 = \frac{1}{a \cos \theta} \cdot \frac{\cos \theta}{a \cos \theta} = \frac{1}{a \cos \theta} \cdot \frac{\cos \theta}{\cos \theta} = \frac{1}{a \cos \theta} \cdot \frac{\cos \theta}{\cos \theta}$
 $y_3 = \frac{1}{a \cos \theta} \cdot \frac{\cos \theta}{a \cos \theta} \cdot \frac{1}{a \cos \theta} \cdot \frac{\cos \theta}{\cos \theta} = \frac{1$



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$$\frac{\pi}{1} = x - \frac{y_1}{y_2} (1 + y_1^2)$$

$$= a Sec \theta - b_1 casec \theta \left(\frac{-a^2}{b} \right) \frac{sin^3 \theta}{cos^3 \theta} \left(1 + \frac{b^2}{b^2} casec^2 \theta \right)$$

$$= a Sec \theta + a \frac{1}{sin^3 \theta} \frac{sin^3 \theta}{cos^3 \theta} \left[\frac{a^2 + \frac{b^2}{b^2} \frac{1}{sin^3 \theta}}{a^2 sin^2 \theta} \right]$$

$$= a Sec \theta + a \frac{sin^3 \theta}{cos^3 \theta} \left[\frac{a^2 sin^3 \theta + b^2}{a^2 sin^2 \theta} \right]$$

$$= a Sec \theta + \frac{1}{a cos^3 \theta} \left[\frac{a^2 - a^2 cos^2 \theta + b^2}{a^2 cos^3 \theta} \right]$$

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$$= a^2 Sec \theta + a^2 Sec^3 \theta - a^2 cos^2 \theta + b^2 \right]$$

$$= a^2 Sec \theta + a^2 Sec^3 \theta - a^2 cos^2 \theta + b^2 \right]$$

$$= a^2 Sec \theta + a^2 Sec^3 \theta - a^2 cos^2 \theta + b^2 Sec^3 \theta$$

$$a \pi = (a^2 + b^2) Sec^3 \theta$$

$$(a \pi)^{\frac{3}{2}} = (a^2 + b^2)^{\frac{3}{2}} Sec^2 \theta$$



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