## SNS COLLEGE OF ENGINEERING

Kurumbapalayam (Po), Coimbatore - 641107
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## DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING

COURSE NAME : 19IT405 DESIGN AND ANALYSIS OF ALGORITHMS
II YEAR /IV SEMESTER

Unit 2- BRUTE FORCE AND DIVIDE-AND-CONQUER
Topic :Brute force and Exhaustive search

## Brain Storming

1. What is Algorithm?
2. Why it is important?

## Brute Force

- A straightforward approach, usually based directly on the problem's statement and definitions of the concepts involved.
- Generally it involved iterating through all possible solutions until a valid one is found.
Examples - based directly on definitions:

1. Computing $a^{\mu}(a>0, n$ a nonnegative integer)
2. Computing $n$ !
3. Multiplying two matrices
4. Searching for a key of a given value in a list

## Sorting by Brute Force

## Use definition of sorted and obvious algorithm?

Selection Sort Scan the array to find its smallest element and swap it with the first element. Then, starting with the second element, scan the elements to the right of it to find the smallest among them and swap it with the second elements. Generally, on pass $i(0 \leq i \leq n-2)$, find the smallest element in $A[i, n-1]$ and swap it with $A[i]$ :

$$
A[0] \leq \ldots . \leq A[i-1] \mid A[i], \cdots, A[m i n], \ldots, A[n-1]
$$

in their final positions

Example: $7 \quad 325$

## Analysis of Selection Sort

## ALGORITHM SelectionSort(A[0..n-1])

## //Sorts a given array by selection sort

//Input: An array $A[0 . . n-1]$ of orderable elements //Output: Array $A[0 . . n-1]$ sorted in ascending order for $i \leftarrow 0$ to $n-2$ do

$$
\min \leftarrow i
$$

$$
\text { for } j \leftarrow i+1 \text { to } n-1 \text { do }
$$

$$
\text { if } A[j]<A[\min ] \quad \min \leftarrow j
$$

$$
\text { swap } A[i] \text { and } A[\mathrm{~min}]
$$

Time efificiency: $C(n)=$

Space efficiency: ?

## String Matching by Brute Force

- pattern: a string of $m$ characters to search for
- text: a (longer) string of $n$ characters to search in
- problem: find first substring in text that matches pattern

Brute-force: Scan text LR, compare chars, looking for pattern,
Step 1 Align pattern at beginning of text
Step 2 Moving from left to right, compare each character of pattern to the corresponding character in text until

- all characters are found to match (successful search); or
- a mismatch is detected

Step 3 While pattern is not found and the text is not yet exhausted, realign pattern one position to the right and repeat Step 2

## Examples of Brute-Force String Matching

Pattern: 001011<br>Text: 10010101101001100101111010

Pattern: happy
Text: It is never too late to have a happy childhood.

## Pseudocode and Efificiency

ALGORITHM BruteForceStringMatch (T[0..n-1], $P[0 . . m-1])$
//Implements brute-force string matching
//Input: An array $T[0 . . n-1]$ of $n$ characters representing a text and
// an array $P[0 . . m-1]$ of $m$ characters representing a pattern //Output: The index of the first character in the text that starts a
// matching substring or -1 if the search is unsuccessful
for $i \leftarrow 0$ to $n-m$ do
$j \leftarrow 0$
while $j<m$ and $P[j]=T[i+j]$ do
$j \leftarrow j+1$
if $j=m$ return $i$
return - 1
Efficiency:
(Basic op and dataset assumptions?)
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## Brute-Force Polynomial Evaluation

Problem: Find the value of polynomial

$$
p(x)=a_{n} x^{n}+a_{n-1} \cdot x^{n-1}+\ldots+a_{1} x^{1}+a_{0}
$$

at a point $x=x_{0}$
Brute-force algorithm

```
\(p \leftarrow 0.0\)
for \(i \leftarrow n\) downto 0 do
    power \(\leftarrow 1\)
        for \(j \leftarrow 1\) to \(i\) do \(\quad / /\) compute \(x^{i}\)
        power \(\leftarrow\) power *x
        \(p \leftarrow p+a[i] *\) power
```

return $p$

Efficiency: $\mathrm{A}(\mathrm{n})=? \mathrm{M}(\mathrm{n})=\sum_{i=}$

## Polynomial Evaluation: Improvement

Improve by evaluating from right to left (Horner's Method):

$$
a x^{3}+b x^{2}+c x+d=x(x(x(a x+b)+c)+d
$$

Better brute-force algorithm

$$
p \leftarrow a[0]
$$

$$
\text { power } \leftarrow 1
$$

$$
\text { for } i \leftarrow 1 \text { to } n \text { do }
$$

$$
\text { power } \leftarrow \text { power } * x
$$

$$
p \leftarrow p+a[i] * \text { power }
$$

return $p$
Efifeiency: $\mathrm{A}(\mathrm{n})=$ ?. $\mathrm{M}(\mathrm{n})=\sum_{i=}$

## Closest-Pair Problem

Find the two closest points in a set of $n$ points (in the twodimensional Cartesian plane).

Brute-force algorithm
Compute the distance between every pair of distinct points and return the indexes of the points for which the distance is the smallest.

## Closest-Pair Brute-Force Algorithm (cont.)

## ALGORITHM BruteForceClosestPoints $(P)$

//Input: A list $P$ of $n(n \geq 2)$ points $P_{1}=\left(x_{1}, y_{1}\right), \ldots, P_{n}=\left(x_{n}, y_{n}\right)$ //Output: Indices index1 and index2 of the closest pair of points
$d \min \leftarrow \infty$
for $i \leftarrow 1$ to $n-1$ do for $j \leftarrow i+1$ to $n$ do
$d \leftarrow \operatorname{sqrt}\left(\left(x_{i}-x_{j}\right)^{2}+\left(y_{i}-y_{j}\right)^{2}\right) / / s q r t$ is the square root function if $d<d$ min
$d \min \leftarrow d$; index $1 \leftarrow i$; index $2 \leftarrow j$
return index1, index2

$$
\begin{aligned}
C(n) & =\sum_{i=1}^{n-1} \sum_{j=i+1}^{n} 2=2 \sum_{i=1}^{n-1}(n-i) \\
& =2[(n-1)+(n-2)+\cdots+1]=(n-1) n \in \Theta\left(n^{2}\right) .
\end{aligned}
$$

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## Convex Hrull

## DEFINITION: Convex

- A set of points (finite or infinite) in the plane is called convex if for any two points $p$ and $q$ in the set, the entire line segment with the endpoints at $p$ and $q$ belongs to the set.


## DEFINITION: Convex hull

- The convex hull of a set S of points is the smallest convex set containing S . (The "smallest" requirement means that the convex hull of S must be a subset of any convex set containing $\mathrm{S}_{\mathrm{S}}$ )


## Uses

- Convex hulls are used in computing accessibility maps produced from satellite images by Geographic Information Systems.
- They are also used for detecting outliers by some statistical techniques.


## Convex Hull


(a)


FIGURE 3.4 (a) Convex sets. (b) Sets that are not convex.
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## Convex Hull



FIGURE Rubber-band interpretation of the convex hull.
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## Convex Hull

## CONVEX HULL

- Given a set of pins on a pinboard
- And a rubber band around them
- How does the rubber band look when it snaps tight?
- We represent the convex hull as
 the sequence of points on the convex hull polygon, in counterclockwise order.


## Complex Hull

Pseudocode

## Convex Frull

* Time efficiency of this algorithm.
* Time efficiency of this algorithm is in $O(n 3)$ :
for each of $n(n-1) / 2$ pairs of distinct points,
* we may need to find the sign of $a x+b y-c$ for each of the other $n-2$ points.


## Exhaustive Search

Many Brute Force Algorithms use Exhaustive Search

- Example: Brute force Closest Pair


## Approach:

1. Enumerate and evaluate all solutions, and
2. Choose solution that meets some criteria (eg smallest)

## Frequently the obvious solution

But, slow (Why?)

## Exhaustive Search - More Detail

A brute force solution to a problem involving search for an element with a special property, usually among combinatorial objects such as permutations, combinations, or sulbsets of a set.

Method:

- generate a list of all potential solutions to the problem in a systematic manner (see algorithms in Sec. 5.4)
- evaluate potential solutions one by one, disqualifying infeasible ones and, for an optimivation problem, keeping track of the best one found so far
- when search ends, announce the solution(s) found


## Exhaustive Search - More Examples

## Traveling Salesman Problem (TSP)

## Knapsack Problem

## Assignment Problem

## Graph algorithms:

Depth First Search (DIS)
Breadth First Search (BIS)

## Better algorithms may exist

## Example 1: Traveling Salesman Problem

- Given $n$ cities with known distances between each pair, find the shortest tour that passes through all the cities exactly once before returning to the starting city
- More formally: Find shortest Hamiltionian circuit in a weighted connected graph
- Example:



## ISP by Exhaustive Search

> Tour
> $a \longrightarrow b \longrightarrow c \longrightarrow d \longrightarrow a$
> $\mathrm{a} \longrightarrow \mathrm{b} \longrightarrow \mathrm{d} \longrightarrow \mathrm{c} \longrightarrow \mathrm{a}$
> $a \longrightarrow c \longrightarrow b \longrightarrow C \longrightarrow a$
> $a \longrightarrow c \longrightarrow d \longrightarrow b \longrightarrow a$
> $\mathrm{a} \longrightarrow \mathrm{d} \longrightarrow \mathrm{b} \longrightarrow \mathrm{c} \longrightarrow \mathrm{a}$
> $a \longrightarrow d \longrightarrow c \longrightarrow b \longrightarrow a$

Cost
$2+3+7+5=17$
$2+4+7+8=21$
$8+3+4+5=20$
$8+7+4+2=21$
$5+4+3+8=20$
$5+7+3+2=17$

Have we considered all tours?
Do we need to consider more?
Any way to consider fewer?

## Efficiency: Number of tours = number of $\ldots$

## TSP by Exhaustive Search

$$
\begin{gathered}
\text { Toulr } \\
a \longrightarrow \mathrm{~b} \longrightarrow \mathrm{c} \longrightarrow \mathrm{~d} \longrightarrow \mathrm{a} \\
\mathrm{a} \longrightarrow \mathrm{~b} \longrightarrow \mathrm{~d} \longrightarrow \mathrm{c} \longrightarrow \mathrm{a} \\
\mathrm{a} \longrightarrow \mathrm{c} \longrightarrow \mathrm{~b} \longrightarrow \mathrm{~d} \longrightarrow \mathrm{a} \\
\mathrm{a} \longrightarrow \mathrm{c} \longrightarrow \mathrm{~d} \longrightarrow \mathrm{~b} \longrightarrow \mathrm{a} \\
\mathrm{a} \longrightarrow \mathrm{~d} \longrightarrow \mathrm{~b} \longrightarrow \mathrm{c} \longrightarrow \mathrm{a} \\
\mathrm{a} \longrightarrow \mathrm{~d} \longrightarrow \mathrm{c} \longrightarrow \mathrm{~b} \longrightarrow \mathrm{a}
\end{gathered}
$$

Cost

$$
2+3+7+5=17
$$

$$
2+4+7+8=21
$$

$$
8+3+4+5=20
$$

$$
8+7+4+2=21
$$

$$
5+4+3+8=20
$$

$$
5+7+3+2=17
$$

Have we considered all tours? Start elsewhere: b-c-d-a-b
Do we need to consider more? No Any way to consider fewer? Yes: Reverse

Efficiency: \#tours $=0(\#$ permutations of $b, c, d)=O(n!)$

## Example 2: Knapsack Problem

Given $n$ items:

- weights: $w_{1} w_{2} \ldots w_{n}$
- values: $\nu_{1} \quad \nu_{2} \ldots v_{n}$
- a knapsack of capacity W

Find most valuable subset of the items that fit into the knapsack

| Example: Knapsack capa |  |  |  |
| :--- | :---: | :---: | :---: |
| item | weight | value |  |
| 1 | 2 | $\$ 20$ |  |
| 2 | 5 | $\$ 30$ |  |
| 3 | 10 | $\$ 50$ |  |
| 4 | 5 | $\$ 10$ |  |


| Subset | Total weight | Total value |  |
| :---: | :---: | :---: | :---: |
| \{1\} | 2 | \$20 | Efiliciency: how |
| \{2\} | 5 | \$30 | many sulbsets? |
| \{3\} | 10 | \$50 |  |
| \{4\} | 5 | \$10 |  |
| \{1,2\} | 7 | \$50 |  |
| $\{1,3\}$ | 12 | \$70 |  |
| \{1,4\} | 7 | \$30 |  |
| \{2,3\} | 15 | \$80 |  |
| $\{2,4\}$ | 10 | \$40 |  |
| $\{3,4\}$ | 15 | \$60 |  |
| $\{1,2,3\}$ | 17 | not feasible |  |
| \{1,2,4\} | 12 | \$60 |  |
| \{1,3,4\} | 17 | not feasible |  |
| \{ $2,3,4\}$ | 20 | not feasible |  |
| \{1,2,3,4\} | 22 | not feasible |  |

# Example 3: The Assignment Problem 

There are $n$ people who need to be assigned to $n$ jobs, one person per job. The cost of assigning person $i$ to $j o b j$ is $C[i, j]$. Find an assignment that minimizes the total cost.

|  | Job 0 | Job 1 | Job 2 | Job 3 |
| :--- | :--- | ---: | ---: | ---: |
| Person 0 | 9 | 2 | 7 | 8 |
| Person 1 | 6 | 4 | 3 | 7 |
| Person 2 | 5 | 8 | 1 | 8 |
| Person 3 | 7 | 6 | 9 | 4 |

Algorithmic Plan:
Generate all legitimate assignments
Compute costs
Select cheapest

## Assignment Problem: Exhaustive Search

$$
\begin{aligned}
& 9278 \\
& C=\begin{array}{llll}
6 & 4 & 3 & 7 \\
5 & 8 & 1 & 8
\end{array} \\
& \begin{array}{llll}
7 & 6 & 9
\end{array} \\
& \text { Assignment (col:\#ss) } \\
& 1,2,3,4 \\
& \text { 1, 2, 4, } 3 \\
& \text { 1,3,2, } 4 \\
& 1,3,4,2 \\
& \text { 1, 4, 2, } 3 \\
& 1,4,3,2 \\
& \text {... } \\
& \text { Total Cost } \\
& 9+4+1+4=18 \\
& 9+4+8+9=30 \\
& 9+3+8+4=24 \\
& 9+3+8+6=26 \\
& 9+7+8+9=33 \\
& 9+7+1+6=23
\end{aligned}
$$

(For this instance, the optimal assignment can be easily found by exploiting the specific features of the numbers given. It is:

## Assignment Problem: Exhaustive Search

$$
\begin{aligned}
& 9278 \\
& C=\begin{array}{llll}
6 & 4 & 3 & 7 \\
5 & 8 & 1 & 8
\end{array} \\
& \begin{array}{llll}
7 & 6 & 9
\end{array} \\
& \text { Assignment (col.\#s) } \\
& 1,2,3,4 \\
& \text { 1, 2, 4, } 3 \\
& \text { 1,3,2, } 4 \\
& 1,3,4,2 \\
& \text { 1, 4, 2, } 3 \\
& 1,4,3,2 \\
& \text {... } \\
& \text { Total Cost } \\
& 9+4+1+4=18 \\
& 9+4+8+9=30 \\
& 9+3+8+4=24 \\
& 9+3+8+6=26 \\
& 9+7+8+9=33 \\
& 9+7+1+6=23
\end{aligned}
$$

(For this instance, the optimal assignment can be easily found by exploiting the specific features of the numbers given. It is: $(2,1,3,4)$

## Example 3: The Assignment Problem

There are $n$ people who need to be assigned to $n$ jobs, one person per job. The cost of assigning person $i$ to $j o b j$ is $C[i, j]$. Find an assignment that minimizes the total cost.

|  | Job 0 Job 1 | Job 2 | Job 3 |  |
| :---: | :---: | ---: | ---: | ---: |
| Person 0 | 9 | 2 | 7 | 8 |
| Person 1 | 6 | 4 | 3 | 7 |
| Person 2 | 5 | 8 | 1 | 8 |
| Person 3 | 7 | 6 | 9 | 4 |

Algorithmic Plan: Generate all legitimate assignments, compute their costs, and select the cheapest one.
How many assignments are there?
Describe sol'n using cost matrix:

## Example 3: The Assignment Problem

There are $n$ people who need to be assigned to $n$ jobs, one person per job. The cost of assigning person $i$ to job $j$ is $C[i, j]$. Find an assignment that minimizes the total cost.

|  | Job 0 | Job 1 | Job 2 | Job 3 |
| :--- | :--- | ---: | ---: | ---: |
| Person 0 | 9 | 2 | 7 | 8 |
| Person 1 | 6 | 4 | 3 | 7 |
| Person 2 | 5 | 8 | 1 | 8 |
| Person 3 | 7 | 6 | 9 | 4 |

Algorithmic Plan: Generate all legitimate assignments, compute their costs, and select the cheapest one.
How many assignments are there: permutations of $1 . . \mathrm{n}=\mathrm{n}$ !
Sol'n using cost matrix: select one from each row/col. Min sum.

## Final Comments on Exhaustive Search

- Exhaustive-search algorithms run in a realistic amount of time only on very small instances
- In some cases, there are much better alternatives!
- Euler circuits
- shortest paths
- minimum spanning tree
- assignment problem
- In many cases, exhaustive search or its variation is the only known way to get exact solution


## GRAPHS

Many problem solutions use a graph to represent the data:

- TSP
- Cities and roads
- Network nodes and connections among them
- People and friends

What is a graph? A graph is defined by two sets:

- Set of Vertices
- Set of Edges that connect the vertices

We look at two aspects of graphs:

- Standard graph algorithms (eg DES and BBS in this chapter)
- Solve some problems with graphs
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## Graph Traversal Algorithms

Many problems require processing all graph vertices (and edges) in systematic fashion

## Graph traversal algorithms:

- Depth-first search (DIS): Visit children first
- Breadth-first search (BIS): Visit siblings first


## GRAPHS - Definition Expanded

Graph consists of two sets:

- Set of vertices (aka nodes)
- Set of edges that connect vertices
- Edges may have weights
- Edges may have directions:
- Undirected graph: edges have no directions
- Directed graph: edges have direction
- AKA Digraph


## GRAPH TERMS (Chap 1)

Degree of a node: Number of edges from it (in deg and out deg)
Path: Sequence of vertices that are connected by edges
Cycle: Path that starts and ends at same node
Connected graph:

- every pair of vertices has a path between them

Complete graph:

- every pair of vertices has an edge between them

Tree: connected acyclic graph

- Tree with n nodes has n-1 edges
- Root need not be specified
- Regular terms: Parent, child, ancestors, descendents, siblings, ...

Forest: set of trees (ie not-necessarily-connected acyclic graph)
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## Graph Implementation

Adjacency matrix:

- Row and column for each vertex
- 1 for edge or 0 for no edge
- Undirected graph: What is true of the matrix?

Adjacency lists

- Each node has a list of adjacent nodes

Each has pros and cons. Performance:

- Check if two nodes are adjacent: ...
- List all adjacent nodes: ...


## Depth-First Search (DFS)

$\square$ Visits graph's vertices by always moving away from last visited vertex to unvisited one

- Backtracks if no adjacent unvisited vertex is available.
- Implements backtracking using a stack
- a vertex is pushed when it's reached for the first time
- a vertex is popped when it becomes a dead end, i.e., when there are no adjacent unvisited vertices
- Marks edges in tree-like fashion (mark edges as tree edges and back edges [goes back to already discovered ancestor vertex].
- In a DRS of an undirected graph, each edge becomes either a tree edge or a back edge (back to ancestor in tree)


## Pseudocode of DES

## ALGORITHM $\operatorname{DFS}(G)$

//Implements a depth-first search traversal of a given graph
//Input: Graph $G=\langle V, E\rangle$
//Output: Graph $G$ with its vertices marked with consecutive integers

## Stack?

//in the order they've been first encountered by the DFS traversal
mark each vertex in $V$ with 0 as a mark of being "unvisited"
count $\leftarrow 0$
for each vertex $v$ in $V$ do
if $v$ is marked with 0 $d f s(v)$

## $d f s(v)$

//visits recursively all the unvisited vertices connected to vertex $v$ by a path //and numbers them in the order they are encountered
//via global variable count
count $\leftarrow$ count +1 ; mark $v$ with count
for each vertex $w$ in $V$ adjacent to $v$ do
if $w$ is marked with 0
$d f s(w)$

# Example: DFS traversal of undirected graph 



DHS traversal stack:

## DIS tree:

## Example: DFS traversal of undirected graph

e

h
Nodes pushed: a b fegcd h Nodes popped: e f h d c g b a

Tree Edges: each v in difis(v) defines a tree edge
Back Edge: encountered edge to previously visited ancestor
What nodes are on the stack?
Complexity:

- DFS can be implemented with graphs represented as:
- adjacency matrices: $O\left(V^{2}\right)$
- adjacency lists: $\Theta(|V|+|\mathbb{E}|)$
- Yields two distinct ordering of vertices:
- order in which vertices are first encountered (pushed onto stack)
- order in which vertices become dead-ends (popped ofi stack)
- Orderings and edges used by various algorithms
- (eg scheduling / topological sort)
- Applications:
- checking connectivity, finding connected components
- checking acyclicity
- finding articulation points and biconnected components
- searching state-space of problems for solution (AI)


## Breadth-first search (BIES)

- Visits graph vertices by moving across to all the neighbors of last visited vertex
- BIS uses a queue (not a stack like DIS)
- Similar to level-by-level tree traversal
- Marks edges in tree-like fashion (mark tree edges and cross edges [goes across to an already discovered sibling vertex]
- In a BIS of an undirected graph, each edge becomes either a tree edge or a cross edge (to neither ancestor nor descendant in tree-common ancestor or other tree)


## Pseudocode of BIS

## ALGORITHM $B F S(G)$

//Implements a breadth-first search traversal of a given graph
//Input: Graph $G=\langle V, E\rangle$
//Output: Graph $G$ with its vertices marked with consecutive integers
//in the order they have been visited by the BFS traversal
mark each vertex in $V$ with 0 as a mark of being "unvisited"
count $\leftarrow 0$
for each vertex $v$ in $V$ do
if $v$ is marked with 0 $b f s(v)$
$b f s(v)$
//visits all the unvisited vertices connected to vertcx $v$ by a path //and assigns them the numbers in the order they are visited //via global variable count
count $\leftarrow$ count $+1 ;$ mark $v$ with count and initialize a queue with $v$ while the queue is not empty do
for each vertex $w$ in $V$ adjacent to the front vertex do
if $w$ is marked with 0
count $\leftarrow$ count +1 ; mark $w$ with count
add $w$ to the queue
A. Levitin "Int| remove the front vertex from the queue

## Example of BIS traversal of undirected graph



BIIS traversal queue:
BHS tree:

## Example of BIS traversal of undirected graph



C d


BIS traversal queue: a, bef,g, ch,d
Level:
$1,222,3,44,5$

Tree Edges: as difis
Cross Edges: encountered edge to previously visited sibling or sibling's descendent (eg hypothetical edge eg)
What nodes are on the queue?
Performance:

- BHS has same efficiency as DIS and can be implemented with graphs represented as:
- adjacency matrices: $\Theta\left(V^{2}\right)$
- adjacency lists: $\Theta(|V|+|E|)$
- Yields single ordering of vertices (order added/deleted from queue is the same)
- Applications: same as DIS, but can also find paths from a vertex to all other vertices with the smallest number of edges [How: mark depth from root]


## Brute Force: Review

- Based on problem statement and definitions
- Typically slow, but may be only known algorithm
- Useful to consider first
- better algorithm frequently known
- Examples:
- Sorting and Searching
- Exhaustive Search:
- Pattern Match, TSP, Knapsack, Assignment,
- Graph (DHS, BHS)


## Brute-Force Strengths and Weaknesses

- Strengths
- Wide applicability
- Simplicity
- Yields reasonable algorithms for some important problems (e.g., matrix multiply, sorting, searching, string matching)
- Algorithm may be good enough for small problem
- Improvement may be too hard
- Provides yardstick for comparison
- Weaknesses
- Rarely yields efficient algorithms
- Some brute-force algorithms are unacceptably slow
- Not as constructive as some other design techniques


## Assessment 1

1. What is algorithm?

Ans: $\qquad$
2. Why algorithm effectiveness is important?

Ans: $\qquad$

## References

## TEXT BOOKS

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## Thank You

