

Mathematical Analysis for Non-recursive

→ It is executed only once to solve the Problems.

General plan:-

- ① Decide on a I/P size.
- ② Identify the basic operations.
- ③ Check the no. of times basic operation is executed depend only on the size of I/P.
- ④ Sum No. of times basic operation is executed.
- ⑤ Simplify the sum of using standard formula & Rules.

Ex-1:

Finding the value of the largest element in a list of 'n' numbers

Alg:-

Algorithm max element ($A[0 \dots n-1]$)

// Problem Description: This alg. is for finding max - element in array.

// I/P : Array $A[0 \dots n-1]$

// O/P : returns the largest elements.

```
max ← A[0]
for i ← 1 to n-1 do
{
  if (A[i] > max) then
  }
  max ← A[i]
}
return max;
```

Mathematical Analysis:

Step 1: The I/P size is 'n', the total no. of elements in array.

Step 2: The basic operation is comparison in loop for finding large values.

Step 3: The comparison is executed on each repetition of the loop. As the comparison made for each value of 'n'. There is no need to find best Avg, worst case.

Step 4: Let $C(n)$ be the no. of times comparison is executed. The alg makes comparison each time the loop executes.

Hence, for $i=1$, to $n-1$ times, the comparison made,

$$C(n) = \sum_{i=1}^{n-1} 1 \rightarrow \text{One comparison made for each value of } i.$$

Step 5: Simplify:

$$C(n) = \sum_{i=1}^{n-1} 1$$

$$C(n) = n-1 \in O(n).$$

Thus the time complexity of finding maximum elements in an array is

$$O(n).$$