

Brute Force

→ Straight forward approach to solving a problem. usually directly based on problem statement & definitions of concepts involved.

→ "force"

→ "just do it"

closest-pair & convex-hull problems

↳ straight forward

→ problems deals with finite set of points

→ areas: - computational, geometry & OR

closest-pair problem

→ finding 2-closest points in set of n points.

Points are (x, y)

Cartesian co-ordinates

↳ distance point b/w 2 points

$$P_i = (x_i, y_i) \text{ \& \ } P_j = (x_j, y_j)$$

Std Euclidean distance

$$d(P_i, P_j) = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}$$

Algorithm - Brute force closest points (P)

It finds 2 closest points in plane by brute force

I/P : list P of n ($n \geq 2$) points $p_1 = (x_1, y_1)$
 \dots $p_n = (x_n, y_n)$

O/P : indicate index 1 & index 2 of closest pair

$dim \leftarrow \infty$

for $i \leftarrow 1$ to $n-1$ do

for $j \leftarrow i+1$ to n do

$d \leftarrow \text{sqrt}((x_i - x_j)^2 + (y_i - y_j)^2)$

if $d < \text{min}$

$\text{min} \leftarrow d$; $\text{index}_1 \leftarrow i$; $\text{index}_2 \leftarrow j$

return $\text{index}_1, \text{index}_2$

$$C(n) = \sum_{i=1}^{n-1} \sum_{j=i+1}^n 2 = 2 \sum_{i=1}^{n-1} (n-i)$$

$$= 2[(n-1) + (n-2) + \dots + 1] = (n-1)n \in \Theta(n^2)$$