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Asymptotic notations

AP/IT

- O notation: asymptotic “less than”: $f(n) \leq g(n)$
- Ω notation: asymptotic “greater than”: $f(n) \geq g(n)$
- Θ notation: asymptotic “equality”: $f(n) = g(n)$

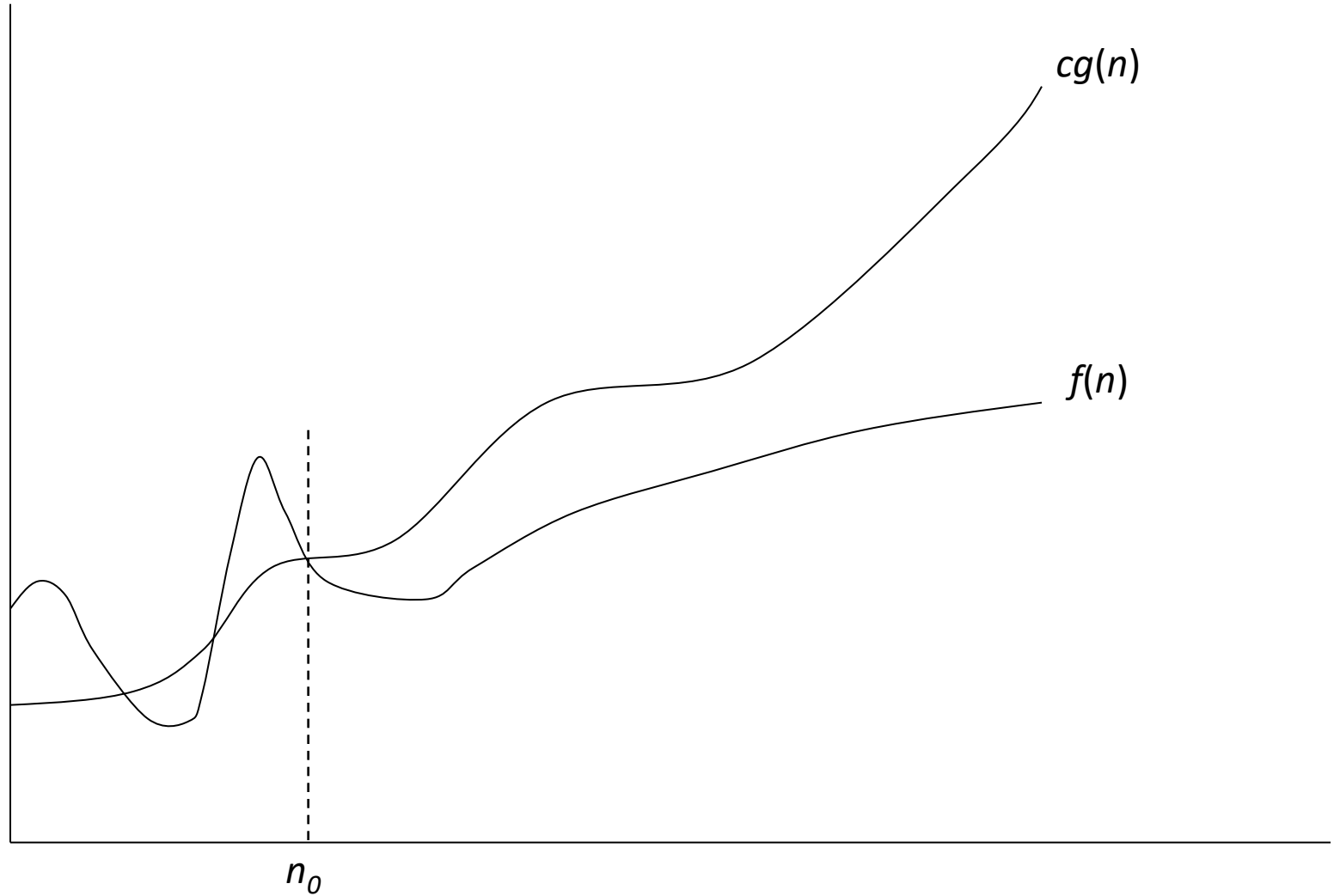
Big-O

$f(n) = O(g(n))$: there exist positive constants c and n_0 such that
 $0 \leq f(n) \leq cg(n)$ for all $n \geq n_0$

If $f(n) = O(n^2)$, then:

- $f(n)$ can be larger than n^2 sometimes, **but...**
- I can choose some constant c and some value n_0 such that for **every** value of n larger than n_0 : $f(n) < cn^2$
- That is, for values larger than n_0 , $f(n)$ is never more than a constant multiplier greater than n^2

Visualization of $O(g(n))$



Big Omega – Notation

$\Omega()$ = A **lower** bound

$f(n) = \Omega(g(n))$: there exist positive constants c and n_0 such that

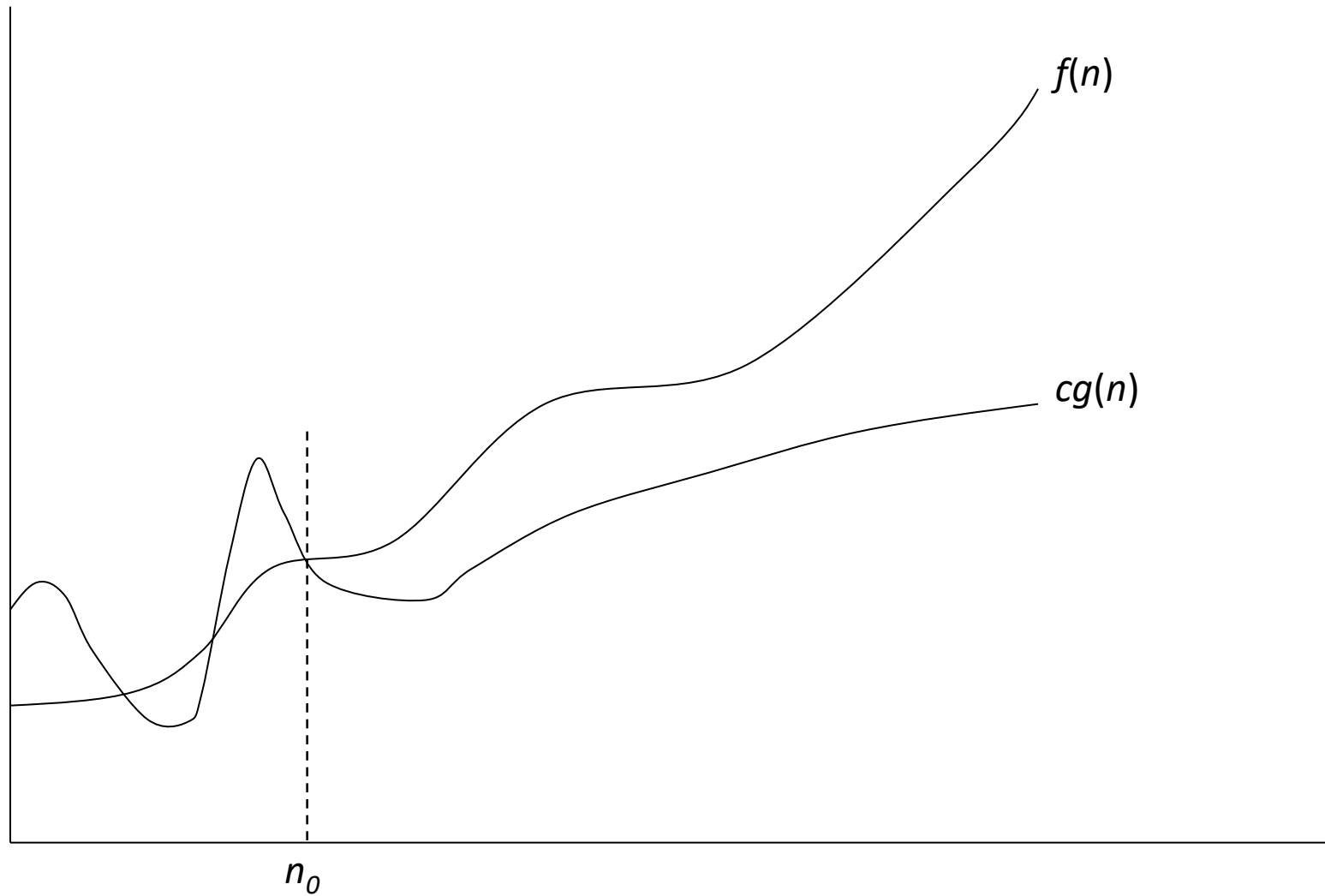
$$0 \leq f(n) \geq cg(n) \text{ for all } n \geq n_0$$

$$n^2 = \Omega(n)$$

$$\text{Let } c = 1, n_0 = 2$$

$$\text{For all } n \geq 2, n^2 > 1 \times n$$

Visualization of $\Omega(g(n))$



Θ -notation

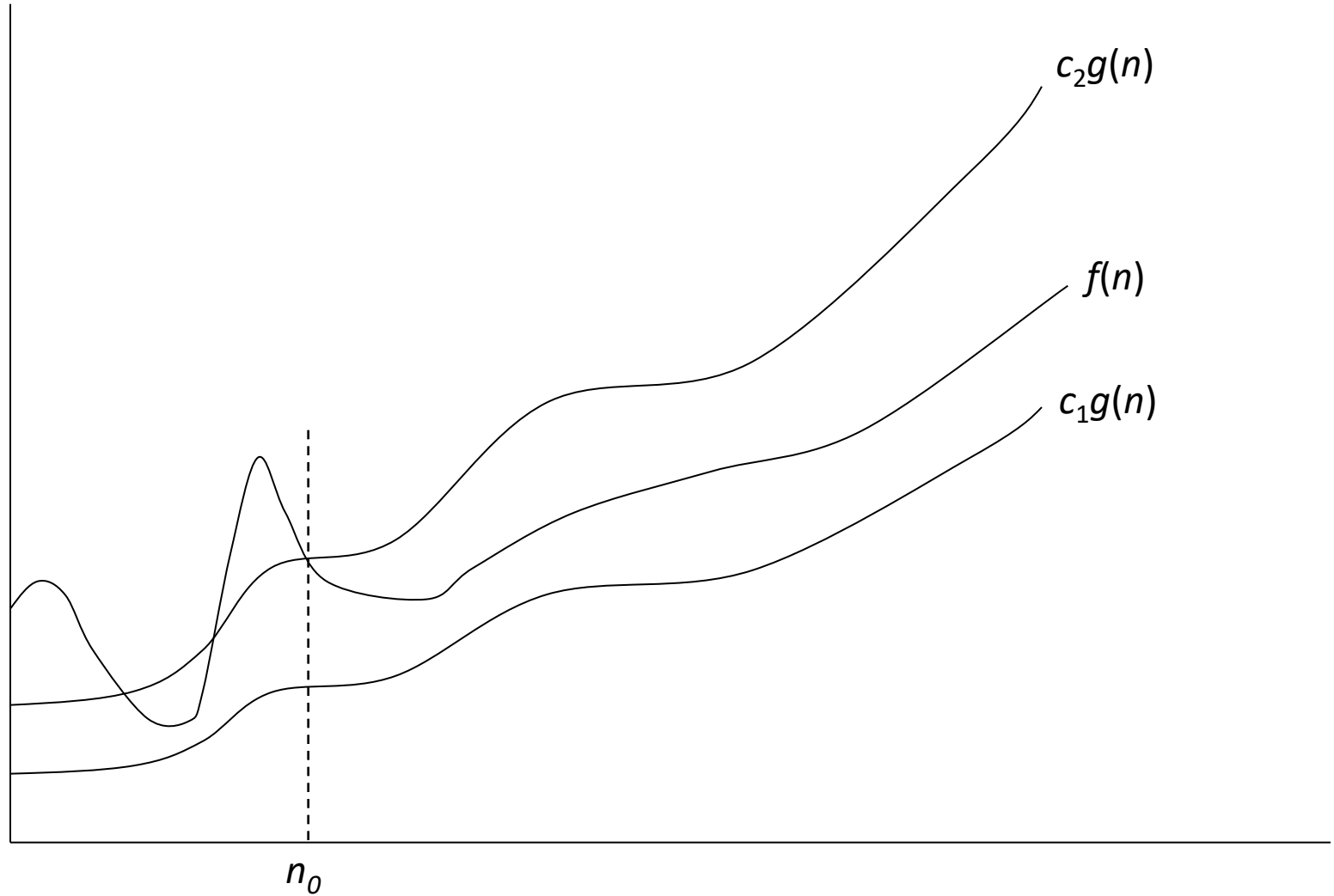
Big- O is not a tight upper bound.

In other words $n = O(n^2)$

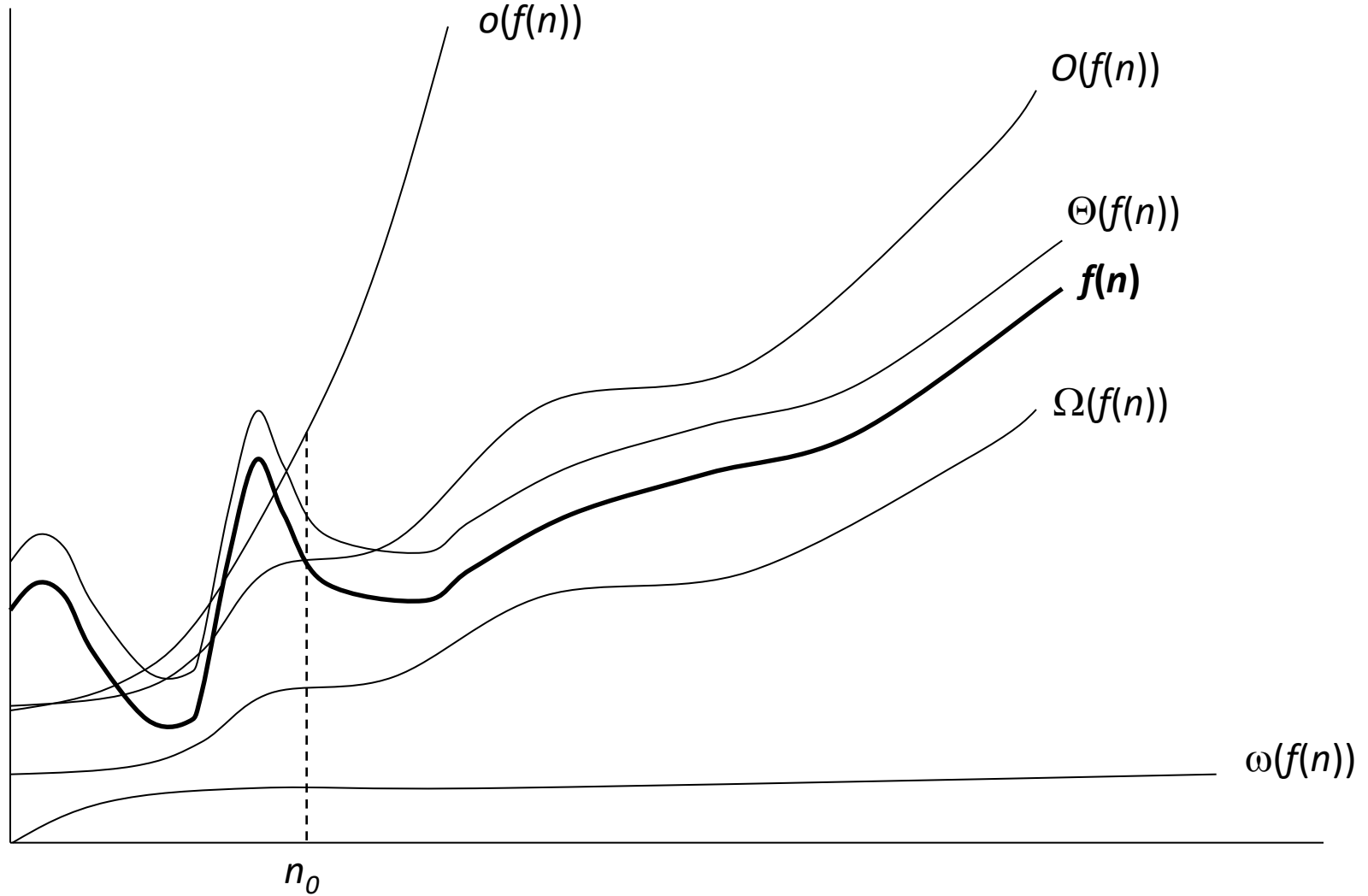
Θ provides a tight bound

$f(n) = \Theta(g(n))$: there exist positive constants c_1, c_2 , and n_0 such that
 $0 \leq c_1 g(n) \leq f(n) \leq c_2 g(n)$ for all $n \geq n_0$

Visualization of $\Theta(g(n))$



Visualization of Asymptotic Growth



Analogy to Arithmetic Operators

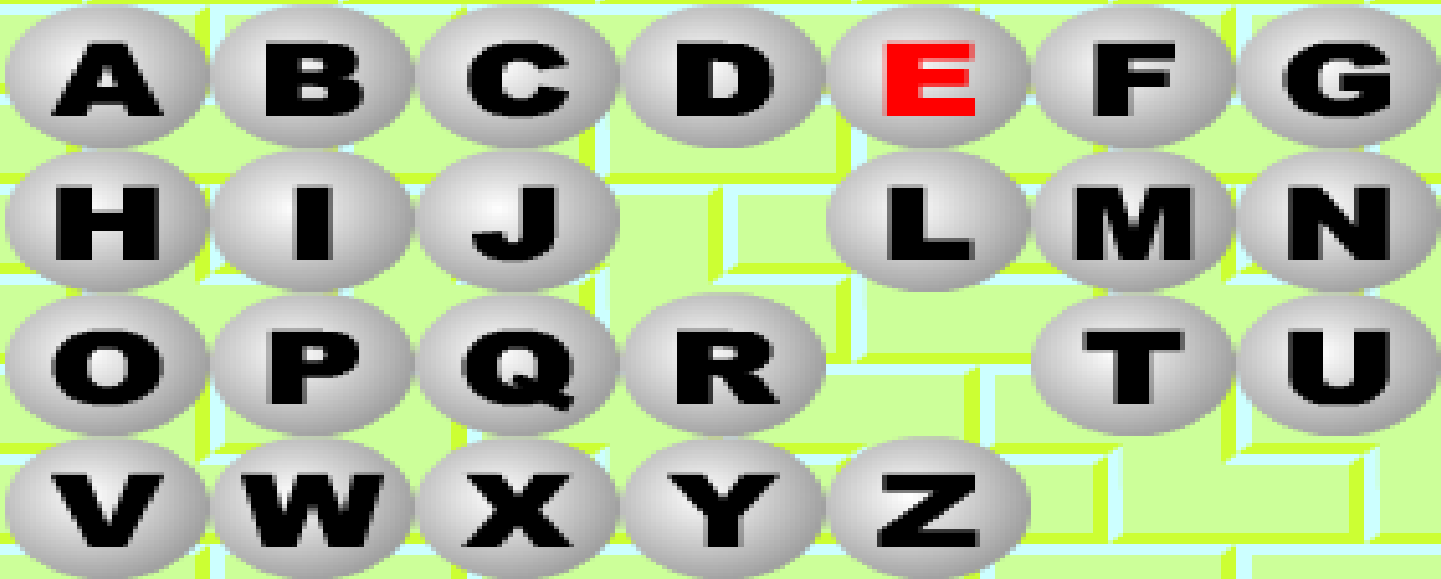
$$f(n) = O(g(n)) \quad \approx \quad a \leq b$$

$$f(n) = \Omega(g(n)) \quad \approx \quad a \geq b$$

$$f(n) = \Theta(g(n)) \quad \approx \quad a = b$$

BREAK

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M U S T

Answer:

2 3 1