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# **Topic: 1.9 – REDUCTION TO QUADRATIC FORM TO CANONICAL FORM**

Reduction of Quochatri form to Canonidal Born.  
Northing Rule:  
1. Writh the matrix of the given Q.F.  
2. To find the Cha Equ.  
3. To Solve the Cha Equ.  
4. To find the Eigenvectors orthogonal to each  
5. Form Normalised matrix N.  
6. Find NT.  
7. Find AN  
8. Find D=NTAN  
9. Canonical form [Y, Y2 Y3] [D] 
$$\begin{bmatrix} Y_1 \\ Y_2 \end{bmatrix}$$
.  
Reduce the Quadhatic form Q=bx2+3y2+3z<sup>2</sup>-hxy-2yz+hzx  
into Canonical form by an orthogonal to cuyformatia.  
Solutions  
Griven Q.F: 6x2+3y<sup>2</sup>+3z<sup>2</sup>-hxy-2yz+hzx  
8tep1: The matrix of the Q:Fin  
 $N = \begin{bmatrix} 6 -2 & 2-7 \\ -2 & 3-1 \\ 2 & -1 & 3 \end{bmatrix}$ .





2

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9-1) + (18-4) +(18-4)

= 
$$8 + 14 + 14 = 36$$
  
 $8_3 \cdot 1 \land 1 = b(9 - 1) + 2(-b+3) + 2(2-6)$   
 $= b(8) + 2(-b) + 2(-b)$   
 $= 48 - 8 - 8 = 32$   
 $\therefore$  The chareque  $A_3 \times 3^{-12} \times 2 + 36 \times - 32 = 0$   
 $8 \pm 29 \cdot 3$ : To solve the chareque  
 $\Lambda^{2} - 12 \Lambda^{2} + 36 \Lambda - 32 = 0$   
 $S \pm 29 \cdot 3 = 10$   
 $S \pm 3 - 12 \Lambda^{2} + 36 \Lambda - 32 = 0$   
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By synthetic obvision  

$$2 | 1 - 12 36 - 32$$
  
 $2 | 0 2 - 20 32$   
 $1 -10 16 10$   
 $(3 - 2) (3 - 2) (3 - 20) + 167 = 0$   
 $(3 - 2) (3 - 2) (3 - 2) (3 - 10) + 167 = 0$   
 $(3 - 2) (3 - 2) (3 - 2) (3 - 6) = 0$   
 $3 = 2, 2, 8$ 





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find the Eigenvector Step H. 50 Solve (A-X1) X=0  $b-\lambda -2 = \frac{1}{2}$ -2 3-7 -1  $\frac{1}{2}$ 2 -1 3-7 33 2=8 26 tue (1) -2 - 2 2  $x_1$ -2 - 5 - 1  $x_2$  $x_3$ 2 -24, - 242+ 243=0 3 -21,-5%,-23=0 24, - 12-513=0 Solving Db3  $\frac{\chi_1}{2+10} = \frac{\chi_2}{-4-2} = \frac{\chi_3}{10-4}$  $\frac{x_1}{12} = \frac{x_2}{-b} = \frac{x_3}{-b}$  $c(0) \frac{x_1}{2} = \frac{x_2}{2} = \frac{x_3}{1} = \frac{x_3}{1} = \frac{2}{1}$ 





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bet x3 = [m] i

 $X_3$  is orthogonal to  $X_1 \cup X_2$   $\Rightarrow X_1^T V_3 = 0 \Rightarrow dl_m + n = 0 = 10$  $\cup X_2^T X_3 = 0 \Rightarrow 0 l + m + n = 0 = 10$ 





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Solving 3 60  $\frac{1}{1} = \frac{m}{0-2} = \frac{n}{2-0}$ くし = デーイ  $(io) \neq = \underbrace{m}_{1} = \underbrace{n}_{1} \implies x_{3} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$ 

Step: 5 Form Normalised matrix

N-	12	0	访了	
N-=	2/10 -1/50	1 12	5-15	
	上市	152	-3	

Step: 6 :  $N^{T} = \begin{bmatrix} 2/\sqrt{2} & -\sqrt{36} & \sqrt{6} \\ 0 & \sqrt{52} & \sqrt{52} \\ V & V & -\sqrt{52} \end{bmatrix}$ 

Lep: 7: FIND AN  $AN = \begin{bmatrix} 6 - 2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix} \begin{bmatrix} -1/2 & 1/2 \\ -1/2 & 1/2 \end{bmatrix}$ 

SNSCE/ S&H/ UNIT 1/ 1.9 - Reduction of quadratic Form to Canonical form/D. SHILA/AP/MATHS





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FIND NAN SLep:8  $D = N^{T}AN = \begin{cases} 2/r_{0} & -1/r_{0} & 1/r_{1} \\ 0 & 1/r_{2} & 1/r_{2} \\ 1/r_{3} & 1/r_{3} & 1/r_{3} \\ 1/r_{3} & 1/r_{3} & 1/r$ 16-8-8 0+2-2  $= \begin{pmatrix} 8 & 0 & 0 \\ \sigma & 2 & 0 \\ 0 & 0 & 2 \end{pmatrix}$ <u>Step:</u>9 <u>canonical</u> form:  $(y, y_2 y_3)$  (D)  $\begin{pmatrix} y_1 \\ y_2 \end{pmatrix}$  $\begin{pmatrix} y, y_2 y_3 \end{pmatrix} \begin{pmatrix} 8 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{pmatrix} \begin{pmatrix} y_1 \\ y_2 \\ y_3 \end{pmatrix} = 8y_1^2 + 2y_2^2 + 2y_3^2$ Step: 10 Natur of the Q.F since all the Eigenvalues of Given matrix A one the, i. Q. F is the definite