

SNS COLLEGE OF ENGINEERING Kurumbapalayam (Po), Coimbatore – 641 107



AN AUTONOMOUS INSTITUTION

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Topic: 1.7 – DIAGONALIZATION OF MATRICES

Working Rule For Diagonalisation:
* To find the characteristic equation
* To robe the characteristic equation
* To find the Figer values
* Normalised forms is
$$N = \begin{bmatrix} \pi/2 \\ \pi/2 \\ \pi/2 \end{bmatrix}$$
 where $l = \sqrt{\pi^2 + 2\pi^2 + \pi^2}$
* Ford N^T
* Calculate AN
* Calculate AN
* Calculate D = N^TAN
Problems:
1. Diagonalise the maturi $\begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ \pi/2 & -4 & 3 \end{bmatrix}$
Let $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ \pi/2 & -4 & 3 \end{bmatrix}$
Characteristic equation $\Rightarrow \lambda^2 - 18\lambda^2 + 45\lambda = 0$
Figer values are 0,3,15
Figer values are 0



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To find the Egen vectors are orthogonal to each other.

$$X_{1}^{T}X_{2} \Rightarrow 2+2-4 = 0$$

$$X_{2}^{T}X_{3} \Rightarrow 2-4+2=0$$

$$They are orthogonal to each other.$$
To from the Normalised Matrix:

$$N = \begin{bmatrix} Y_{3} & Y_{3} & Y_{3} \\ Y_{3} & Y_{3} & -Y_{3} \\ Y_{3} & -Y_{3} \end{bmatrix} \Rightarrow \frac{1}{3} \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1-2 \\ 2 & -2 & 1 \end{bmatrix}$$
To find the transpose of normalised matrix:

$$N^{T} = \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1-2 \\ 2 & -2 & 1 \end{bmatrix} \frac{1}{3}$$
Calculate AN

$$AN = \frac{1}{3} \begin{bmatrix} 8-6 & 2 \\ -6 & 7-4 \\ 2 & -2 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1-2 \\ 2 & -2 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 2 & 10 \\ 0 & 1 & -10 \\ 0 & -2 & 5 \end{bmatrix}$$
Calculate Diagonised Matrix D

$$D = NAN^{T}$$

$$= \frac{1}{3} \begin{bmatrix} 8-6 & 2 \\ -6 & 7-4 \\ 2-4 & 3 \end{bmatrix} \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1-2 \\ 2-2 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 2 \\ 2 & 1-2 \\ 2-2 & 1 \end{bmatrix} = \frac{1}{3}$$

$$= \frac{1}{3} \begin{bmatrix} 1 & 2 & 2 \\ -7 & 4 \\ 2 & -2 & 1 \end{bmatrix} \begin{bmatrix} 0 & 2 & 10 \\ 0 & 1 & -10 \\ 0 & -2 & 5 \end{bmatrix}$$

$$= \begin{bmatrix} 0 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 15 \end{bmatrix}$$