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TOPIC: 2.2 – SERIES: TYPES AND CONVERGENCE

Saies Infinite Series 15 anasi anno be an infinite sequence of real numbers then a, + a + a + ... + a + ... o is called an infinite series. An Infinite keries is denoted by 2 as and the sum of its first 'n' terms is denoted by Sn. Convergent, Dirergent & Oscillatory of a series consider the infinite series. = an = a, + a + ... + an + ... 00. Lot the sum of first's' learns be Sn = Q1+ Q2+ Qn. The convergence or divergence of the reaser Ean is defined in terms of the convergence on direegence of the sequence { sny. a. Zan is said to converge if the requerce & sny converger.





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ozan is said to be diverge if the Domence { sn } diverger. O. Z an in said to oscillatory if the sequence of say alose not lead to a unique semit as n+00. O. Examine the convergence of the series. 1+2+3+ 40 + 00. Griven. Zan: 14243+...+ n4.... 00. Sohe. 101 So = 1+2+ 3+ ...+ 0. Sn = n(nai) $\lim_{n \to \infty} S_n = \lim_{n \to \infty} \frac{n(n+1)}{2}$ · L lim n(n+1) fin Sn = 00. :. The Sn divergent . Zan is also divergent.





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2). 1+ 3+5+ 7+....00. som Gin. 1+3+5+4+.... are in A.P to = at co-i)d. a: 1, d: 2, +== 1+(--1)2 = 8n-1. Sn = 1+ 3+5+ ... + (2n-1) = = [aa + cn. i)d] = = [2+(n-1)2] = n 8. $lim Sn = lim n^2 = 00$. $n \rightarrow 00$:. So is divergent, So Zoncading 3. 1 + 1 + 1 + ····· (HOJO \$n = _1





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 $S_n = Z - n(n-1)$ = = - - -----Here u1 = 1 - 1-() = <u>1</u> - <u>1</u> un = 1 - 1 Sn = 41142+431 = 1 - - 1 sum so = sum. (1 - ----= 1 - 0 = · finite . The scales is convergent.