

SNS COLLEGE OF ENGINEERING Kurumbapalayam (Po), Coimbatore – 641 107



AN AUTONOMOUS INSTITUTION

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Topic: 3. 7 - PROPERTIES OF EVOLUTES

proposities of Evolute: 1. The normal at any point of a curve is a targent to its evolute touring at the corresponding centre of curvature. a. The difference blw the radius of curvature at two points of a curve is equal to the length of the arc of the evolute between the two corresponding points 3. There is one evolide but an infinite number of involutes. (i) the Normals to a curve are the targents to its Evolute.

(ii) The evolute of a family of curves touches at each of its points the corresponding



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The show that the evolute of the cycloid

$$x = a(\theta - \sin \theta); y = a(1 - \cos \theta) \text{ is another}$$
equal cycloid.

Sinon $x = a(\theta - \sin \theta); y = a(1 - \cos \theta)$

$$\frac{dy}{d\theta} = a(1 - \cos \theta); \frac{dy}{d\theta} = a \sin \theta.$$

$$\frac{dy}{d\theta} = a \sin \theta = \frac{\sin \theta}{1 - \cos \theta}$$

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$$\frac{dy}{d\theta} = a \sin \theta = \frac{\sin \theta}{1 - \cos \theta}$$

$$\frac{dy}{d\theta} = a \sin \theta = \frac{\cos \theta}{2}$$

$$\frac{d\theta}{d\theta} = a \sin \theta = \frac{\cos \theta}{2}$$

$$\frac{d\theta}{$$



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$$= a(\theta - \sin \theta) + 4a \sin \theta \cdot \cos \theta \cdot \frac{1}{2}$$

$$= a(\theta - \sin \theta) + 2a \sin \theta$$

$$= a(\theta - \sin \theta) + 2a \sin \theta$$

$$= a(\theta + \sin \theta) \rightarrow 0$$

$$y = y + \frac{1}{y}(1 + y^2)$$

$$= a(1 - \cos \theta) + (4a \sin^4 \theta) + (1 + \cot^2 \theta)$$

$$= a(1 - \cos \theta) - 4a \sin^4 \theta \cdot \frac{1 + \cot^2 \theta}{2}$$

$$= a(1 - \cos \theta) - 4a \sin^4 \theta \cdot \frac{1 - \cos \theta}{2}$$

$$= a(1 - \cos \theta) - 4a \left(1 - \cos \theta\right)$$

$$= a(1 - \cos \theta) - 2a(1 - \cos \theta)$$

$$= a(1 - \cos \theta) - 2a(1 - \cos \theta)$$

$$y = -a[1 - \cos \theta] \rightarrow 0$$
from 0 +0 we get
$$2 = a(\theta + \sin \theta) + y = a(1 - \cos \theta)$$
this supresents the equation of another cycloid.