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Topic: 3.3 – CENTRE OF CURVATURE

centre and Radius of worvature. circle & curvature:

The curvature at any point p' of a curve is equal to the unvature of the circle which passes through p and two close points on the curve on either side of p such a circle exists for each poind of the durive. It is called the circle of vervature of the curve at the point.

radius of curvature'. The radius of this circle is called the radius of curvature of the curve at that point,

centre of the eight;

The centre of the circle is called the centre of unvature of the curve at that point.

a) write the formula for centre of mavature. a point (x, y) on a wave $\bar{x} = x - \frac{y_1}{y_2} (1 + y_1^2); \bar{y} - y + \frac{(1 + y_1^2)}{y_2}$



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1. Find the centre of worvature at the
point
$$(am_{3}^{2}am)$$
 on the parabola $y^{2} = tax$.
Side: Given $x = am^{2}$, $y = 2am$.
 $\frac{dx}{dm} = 2am$; $\frac{dy}{dm} = 2a$
 $y_{1} = \frac{dy}{dm}$, $\frac{dm}{dx} = \frac{2a}{2am} = \frac{1}{m}$.
 $y_{2} = \frac{d}{dm} \left(\frac{dy}{dx}\right) \frac{dm}{dm} = \frac{d}{dm} \left(\frac{1}{m}\right) \frac{dm}{dm}$
 $= -\frac{1}{m^{2}} - \frac{1}{2am} = -\frac{1}{2am^{3}}$.
 $\overline{x} = x - \frac{y_{1}}{y_{2}} (1+y_{1}^{2})$.
 $= am^{2} + 2am^{2} (m^{2}+1)$
 $= 3am^{2} + 2a$
 $\overline{y_{2}} = 2am + (1+\frac{1}{m^{2}})$
 $= 2am + (\frac{m^{2}}{m^{2}} = 2am + (1+\frac{1}{m^{2}})$
 $\overline{y} = -2am^{3}$. The centre of wordsture is
 $(3am^{2}+2a, -2am^{3})$.



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prove that if the centre of the aurvature 2) of the ellipse m2+ y2 =1 at one end of the minor axis lies at the other orged, this eccentricity of the ellipse is 1. soln: 8(0,6) The ellipse is x + y2 = 1 + >(BB' is the minor axis. Bis (0,b) B'(0,-4) B' is (0, -b) Diff. I wirit or, we get an + 24 dy =0. $y_{1} = \frac{dy}{dx} = -\frac{2x}{a^{2}} \cdot \frac{b^{2}}{b^{2}} = -\frac{b^{2}x}{a^{2}y}$ $y_{2} = \frac{d^{2}y}{dx^{2}} = -\frac{b^{2}}{a^{2}} \left[\frac{y(1) - x \cdot dy}{\frac{dx}{y^{2}}} \right]$ 9, (0,b) = 0 $y_2(0,b) = -\frac{b^2}{2} \left(\frac{b}{b^2} \right) = -\frac{b}{R^2}$ let (ri, y) be the centre of curvature at (0,b) $\overline{x} = x - \frac{y_1}{y_2} (1+y_1^2) \text{ or } \overline{y} = \frac{y_2 + (1+y_1^2)}{y_2}$ Я(o,b) = 0 - 0 = 0



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y = b + a(1+0) = b - athe centre of curvature is (0, b-a), is given to be the point (0, -b) the or end B'. of the minor dxis. b-a2=-b=) b-a2=-b2 $a^{2}b^{2} = a^{2} \rightarrow \bigcirc$ $b^{2} = a^{2}(1-e^{2})$ where e is being excentricity using in (a) $a^2 = a^2(1-e^2)$ 1-e2=1/2=> e2= e=1/6 centre of curvature ; The centre of curvature (\bar{x}, \bar{y}) at any point $p(\bar{x}, \bar{y})$ on the curve y=f(x) are $\bar{x} = \pi - \frac{y_1}{y_2}(1+y_1^2)$ $\bar{y} = \frac{y_1+1}{y_2}(1+y_1^2)$.