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Topic: 3.1 – CURVATURE AND RADIUS OF CURVATURE

Curvature of a curve: The rate of charge of bending of the curve in the given interval is called Curvature of the curve. Note: (i) The curvature of a straight line is Zero. (ii) the curvature of a point is infinity. (iv) The curvature of a point is infinity. (iv) The curvature of a circle at any point on et is the same and is equal to the reciprocal of its radius. Curvature is denoted by $K\left(=\frac{d^2}{ds}\right)$



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Radius of curvature:
The reciprocal of the curvature of a
curve at any point is called the radius of
curvature at the point and is denoted by
$$\beta$$
.
hence $\beta = \frac{1}{2} = \frac{dS}{d\eta}$.
Note: the curvature of a circle of radius r
at any point is $\frac{1}{r}$.
cartesian formula for the radius of curvature
is $\beta = (1+y_1^2)^{\frac{3}{2}}$



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1. Find the Radius & curvature of
$$y = e^{X} at(0, 1)$$

solution: Given $y = e^{X}$.
 $y_1 = \frac{dy}{dx} = e^{X} \Rightarrow y_1(0,1) = e^{0} = 1$
 $y_2 = \frac{d^2y}{dx^2} = e^{X} \Rightarrow y_2(0,1) = e^{0} = 1$.
 $\therefore f = (1+y_1^2)^{3/2} = (1+1)^{3/2} = 3^{3/2}$
 $f = 2\sqrt{2}$.
2. find the values of curvature of the curve
 $\sqrt{X} + \sqrt{y} = \sqrt{a}$ at the point $(0x_1 \cdot 0x_1)$.
polution: Given $\sqrt{x} + \sqrt{y} = \sqrt{a} \rightarrow 0$
 $dift \cdot w \cdot x \cdot t \cdot x' \Rightarrow \frac{1}{\sqrt{2}\sqrt{x}} + \frac{1}{\sqrt{2}\sqrt{y}} \frac{dy}{dx} = 0$.
 $\frac{dy}{dx^2} = -\frac{\sqrt{y}}{\sqrt{2}\sqrt{x}}$
 $(\frac{dy}{dx})_{(2x_1, 0x_1)} = \frac{-\sqrt{3x}}{\sqrt{2}\sqrt{x}} = -1$
Again dift · w \cdot x \cdot t \cdot x'.
 $\frac{d^2y}{dx^2} = -\left[\sqrt{\frac{\sqrt{2}x}{\sqrt{2}\sqrt{y}}} + \frac{1}{\sqrt{2}\sqrt{y}} \frac{dy}{dx} - \sqrt{y} \cdot \frac{1}{\sqrt{2}\sqrt{x}}\right]$



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S= (1+4 Show that the radius of convature at (0, c) y=cosh 2 the curve 28+C . Solution y=goosh X $x \Rightarrow y_1 = \frac{dy}{dy} = c \sinh y_1$ 9, (o, c) $y_2 = \frac{d^2 y}{dx^2} = \cosh(\frac{x}{c}) - \frac{1}{c}$ Y2(0, c) = 1/c $f = (1+y_{1}^{2})$ Stc.