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Topic: 1.9 – REDUCTION TO QUADRATIC FORM TO CANONICAL FORM

Reduction of Quoductic form to Canonidal Born.
Northing Rule:
1. Writh the matrix of the given Q.F.
2. To find the Cha Eqn.
3. To Solve the Cha Eqn.
H. To find the Eigenvectors orthogonal to each
5. Form Normalised matrix N.
6. Find NT.
7. Find AN
8. Find D=NTAN
9. Canonical form [Y, Y2 Y3] [D] [Y2].
Reduce the Quadhatic form Q=bx2+3y2+3z²-hxy-2yz+hzx
into Canonical form by an orthogonal to cuyformatia.
Solution
Griven Q.F: 6x2+3y2+3z²-hxy-2yz+hzx
8tep: The matrix of the QFA
N= [6-2 2-]
2-1 3].
8tep: 2. To find the Cha Equates.
The Cha Eqn. of A is
$$\lambda^3 - s, \lambda^2 + s_2 - s_3 = 0$$
.





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= (9-1) + (18-4) + (18-4)

= 8 + 14 + 14 = 36 $8_3 \cdot 1 \land 1 = b(9 - 1) + 2(-b+3) + 2(2-6)$ = b(8) + 2(-b) + 2(-b) = 48 - 8 - 8 = 32 \therefore The charge $A_3 \land^3 - 12 \land^2 + 36 \land - 32 = 8$ $8 \ge 9 \times 3^3 - 12 \land^2 + 36 \land - 32 = 8$ $8 \ge 9 \times 3^3 - 12 \land^2 + 36 \land - 32 = 8$ $5 \ge 9 \times 3^3 - 12 \land^2 + 36 \land - 32 = 8 - 12 + 36 - 32 = 76$ $5 \Rightarrow 0 = 1, 0 = 1 - 12 - 36 - 32 = 1 - 12 + 36 - 32 = 76$ $5 \Rightarrow 0 = 1, 0 = 1 - 12 - 36 - 32 = 8$ $5 \Rightarrow 0 = 2, then 0 = 28 - 42 + 72 - 32 = 8$ $\therefore ? = 2 : 5 = 0 \ 3000t$ By Syntectic oblights

By synthetic ouvision

$$2 \frac{1}{2} \frac{1}{1} - \frac{12}{36} - \frac{32}{32} \frac{1}{1} - \frac{12}{1} \frac{36}{36} - \frac{32}{32} \frac{1}{1} - \frac{10}{16} \frac{16}{10} \frac{10}{16} \frac{10}{10} \frac{10}{16} \frac{10}{10} \frac{10}{16} \frac{10}{10} \frac{10}{16} \frac{10}{16$$





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to find the Eigenversed : Step H. Solve (A-X1) X=0 $b-\lambda -2 = 2 \quad [x, 7]$ -2 3-7 -1 $[x_2]$ 2 -1 3-7 [3.3] 97 2=8 the -24, - 242+ 243=0 3 -21,-5%,-23=0 24, - 42-543=0 Solving Db3 $\frac{\chi_1}{2+10} = \frac{\chi_2}{-4-2} = \frac{\chi_3}{10-4}$ $\frac{x_1}{12} = \frac{x_2}{-b} = \frac{x_3}{-b}$ $c(0) \frac{x_1}{2} = \frac{x_2}{2} = \frac{x_3}{1} = \frac{1}{2} = \frac{1}{2}$





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Care (11) when
$$X=2$$
, (b) becomes.

$$\begin{bmatrix} \lambda & -2 & 2 \\ -2 & 1 & -1 \\ 2 & -1 & 1 \end{bmatrix} \begin{bmatrix} \chi_1 \\ \chi_2 \\ \chi_3 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$$Hx_1 - 2x_2 + 2x_3 = 0$$

$$-3x_1 + x_2 - x_3 = 0$$

$$2x_1 - x_2 + x_3 = 0$$

$$3x_1 - x_2 + x_3 = 0$$

$$-x_2 + x_3 = 0$$

$$3x_1 - x_2 + x_3 = 0$$

$$-x_2 + x_3 = 0$$

$$3x_1 - x_2 + x_3 = 0$$

$$-x_2 + x_3 = 0$$

$$3x_1 - x_2 + x_3 = 0$$

$$-x_2 + x_3 = 0$$

$$x_1 - x_2 + x_3 = 0$$

$$x_2 - x_3 = -x_3$$

$$x_2 - x_3 = -x_3$$

$$x_1 - x_2 + x_3 = 0$$

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$$x_2 - x_3 + x_3 = 0$$

$$x_1 - x_2 + x_3 = 0$$

 X_3 is orthogonal to $X_1 \cup X_2$ $\Rightarrow X_1^T Y_3 = 0 \Rightarrow dl_m + n = 0 - (3)$ $\cup X_2^T X_3 = 0 \Rightarrow ol + m + n = 0 - (9)$

bet X3 =





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Solving 3 & D $\frac{1}{1} = \frac{m}{0-2} = \frac{n}{2-0}$ く12=12 $(io) \neq = \underbrace{m}_{1} = \underbrace{n}_{1} \implies x_{3} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$

Step: 5 Form Normalised matrix

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N-E	2/150 -1/50	1 VI	10 -13	
	上市	152	-3	

Find NT $N = \begin{bmatrix} 2/\sqrt{2} & -1/\sqrt{2} & 1/\sqrt{2} \\ 0 & 1/\sqrt{2} & 1/\sqrt{2} \\ 1 & 1/\sqrt{2} & 1/\sqrt{2} \end{bmatrix}$ Step: 6 :

Lep: 7 : FIND AN $AN = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix} \begin{bmatrix} -1/2 & 1/2 \\ -1/2 & 1/2 \\ -1/2 & 1/2 \end{bmatrix}$

SNSCE/ S&H/ UNIT 1/ 1.9 -Reduction of quadratic Form to Canonical form/S. GOWSALYADEVI/AP/MATHS





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$$\frac{SLOP:8}{D=N^{T}AN=} \begin{bmatrix} 2/\pi & -\sqrt{\pi} & \sqrt{\pi} \\ 0 & \sqrt{\pi} & \sqrt{\pi} \\ \sqrt{\pi} & \sqrt{\pi} & \sqrt{\pi} \\ \end{bmatrix} \begin{bmatrix} 16/\pi_{0} & 0 & 2/\pi_{0} \\ -8/\pi_{0} & 2/\pi_{0} & 2/\pi_{0} \\ -8/\pi_{0} & 2/\pi_{0} & 2/\pi_{0} \\ 8/\pi_{0} & 2/\pi_{0} & 2/\pi_{0} \\ 8/\pi_{0} & 2/\pi_{0} & -\sqrt{\pi} \\ 8/\pi_{0} & 2/\pi_{0} & -\sqrt{\pi} \\ \end{bmatrix}$$

$$= \begin{bmatrix} 32+8+8 & 0 + 12+2 & 4-2-2 \\ \sqrt{18} & 0+2+2 & \sqrt{18} \\ 0 - 8+8 & 0+2+2 & 0+2-2 \\ 16-8-8 & 0+2-2 & \sqrt{18} \\ 16-8-8 & \sqrt{18} \\ 16-8-8 & \sqrt{18} &$$