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Topic: 1.2 – EIGEN VALUES AND EIGEN VECTORS

Eigen-values (or) Proper values (or) latent noons (or) Characteristic Loots:

Let A= [aij] be square matrix. The Characteristic equ. of A is IA-221=0. The rook of the characteristic egg. are called

Eigen values of A.

Eigen Vector (or) Latent Vector:

Corresponding to each characteristic look 2, there corresponds non-zero vector & which Satisfies the egr. (A-Az) x=0. The non-zero vector X are called Characteristic vectors (55)

eigen vedox.

Working Rule to find Eigenvalues & Eigenvectors: Step 1: To find the characteristic equ. 1A-AII 1=0. Step2: To solve the Characteristic Equ. We get Characteristic roots. They are called Eigenbluer.

Step3: To find Ergen vectors, Solve (A-XI) X=0 for the different values of ?.





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Find the Eigenvalues and Eigen Vectors of the matrix [1 17]

8alu: Let A = [1 17]

Step 1: To find the characteristic equ.

The chana equ. of A is $\chi^2 = 5$, $\chi + S_2 = 0$ Where $S_1 = 8$ un of main diagonal elements

= 1+1-17 =0.

S2 = 1A1 = 1 1 1 = -1-3 = -4

The Chair equ. is $\Omega^2 - 0\lambda - \mu = 0$.

(2) $\Omega^2 - \mu = 0$ 8 Eep: 2: To solve the Chair equ.

A=4 Q=+2

Hence the Eigenvalues are -2,2





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8 Eqp. 3. To find the Eigenvectors some (A-21)
$$\alpha = 0$$

$$\begin{bmatrix} \left(\frac{1}{3} - \frac{1}{4}\right) - \lambda \left(\frac{1}{6} - \frac{1}{4}\right) - \frac{1}{3} \\ 3 - 1 - \lambda \end{bmatrix} \begin{bmatrix} \chi_1 \\ \chi_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

Case(i):

If
$$N = -2$$
 then 0 becomes

$$\begin{pmatrix} 3 & 1 \\ 3 & 1 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$3x_1 + x_2 = 0$$
We get only one equ. $3x_1 + x_2 = 0$

$$3x_1 = -x_2$$

$$\frac{x_1}{1} = + \frac{x_2}{-3}$$
The Corresponding Eigenvector 0

$$x_1 = \begin{bmatrix} -1 \\ -3 \end{bmatrix}$$

Care (it)

If
$$x = 2$$
 then equ. (1) become

$$\begin{bmatrix}
-1 & 1 \\
3 & -3
\end{bmatrix}
\begin{bmatrix}
x_1 \\
x_2
\end{bmatrix} = \begin{bmatrix}
0 \\
0
\end{bmatrix}$$

$$-x_1 + x_2 = 0$$

$$3x_1 - 3x_2 = 0$$





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ctes we get only one equ. x1-12=0

$$\frac{x_1}{1} = \frac{x_2}{1}$$

Hence the corresponding Elgen vector is $X_2 = [1]$

Result:

- 1. Eigen values of A are (-2,2)
- 2. Eigen reators: 1 = -2 => x1= (-3)

Find the Eigenvalues & Eigenvectors of

$$A = \begin{bmatrix} 7 & -2 & 0 \\ -2 & 6 & -2 \\ 0 & -2 & 5 \end{bmatrix}$$

80lu.

Sts Step 1. To find the Charac. egu.

The Charac. Egu. of A 15 No- 8, No+ So N-So = 0

S, = 8um of its leading diagonal elements

-7+6+5=18





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$$82 = 8um \text{ of the minors of its leading}$$

$$diagonalu.$$

$$= \begin{vmatrix} b & -2 \\ -2 & 5 \end{vmatrix} + \begin{vmatrix} 7 & 0 \\ 0 & 5 \end{vmatrix} + \begin{vmatrix} 7 & -2 \\ -2 & 6 \end{vmatrix}$$

$$= (30-4) + (35-0) + (42-4)$$

$$= 2b + 35 + 38 = 99$$

$$83 = |A| = \begin{vmatrix} 7 & -2 & 0 \\ -2 & 6 & -2 \\ 0 & -2 & 5 \end{vmatrix}$$

$$= 7[30-4] + 2[-10-0] + 01$$

$$= 7(2b) - 20$$

$$= 182 - 20 = 162$$

: The Charact Page 15 =0.

Step: 2 To Solve the Charac equ.

$$\lambda^3 - 18\lambda^2 + 99\lambda - 162 = 0$$
 = 0

If $\lambda = 1$ | then $0 = 1 - 18 + 99 - 162 = 0$.

If $\lambda = -1$ | then $0 = 1 - 1 - 18 - 99 - 162 = 0$.

If $\lambda = -1$ | then $0 = 1 - 1 - 18 - 99 - 162 = 0$.

If $\lambda = 2$ | then $0 = 18 - 12 + 198 - 162 = 0$.

If $\lambda = -2$ | then $0 = 18 - 12 - 198 - 162 = 0$.

If $\lambda = 3$ | then $24 - 162 + 294 - 162 = 0$.

 $\lambda = 3$ | to a root





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By synthetic
$$3 = 1 - 18 - 99 - 162$$

$$(\lambda - 3) (\lambda^2 - 15\lambda + 54) = 0$$

$$(\lambda - 3) (\lambda - 6) (\lambda - 9) = 0$$

$$(\lambda - 3) (\lambda - 6) (\lambda - 9) = 0$$

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$$(\lambda - 3) (\lambda - 6) (\lambda - 9) = 0$$

$$(\lambda - 3) (\lambda - 9) = 0$$

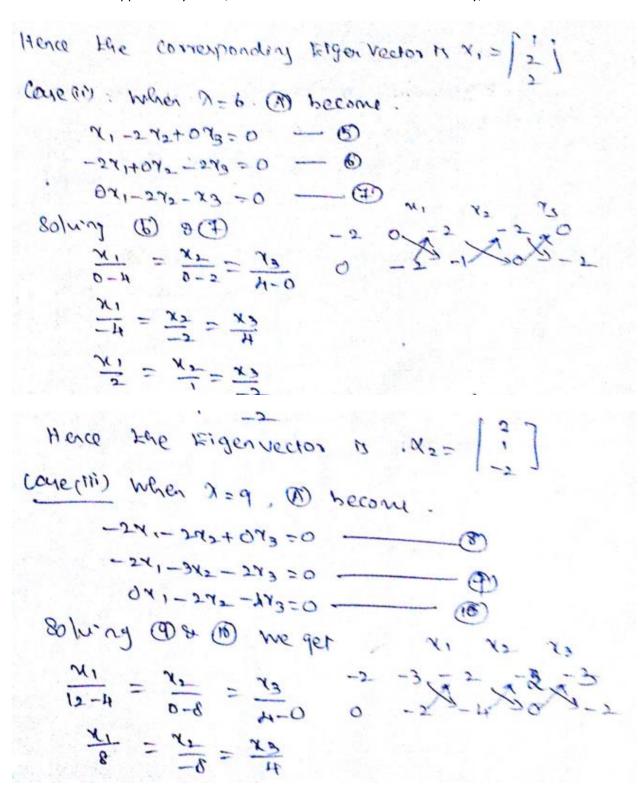
$$(\lambda - 3) (\lambda - 9) = 0$$

$$(\lambda - 1) (\lambda - 9) =$$





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