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Department of Artificial Intelligence and

Data Science

Course Name – Introduction to Artificial Intelligence

II Year / III Semester

Unit 2 Predicate Logic





Predicate Logic

Predicate: It tells something about the subject. sentence involving the predicates that describe the property of objects are denoted by $P(x)$ where
P – The Predicate
x – It is a variable denoting any object.

Characteristics of Predicate Logic:

1. Logical inferencing is allowed.
2. More accurate KR of facts of the real world.
3. Program designing is its application area.
4. Better theoretical foundation.
5. A predicate with no variable is called a Ground Atom.



Constants

- Names of specific objects – E.g. doreen, gord, william, 32
- Functions
- Map objects to objects – E.g. father(doreen), age(gord), max(23,44)
- Variables
- For statements about unidentified objects or general statements – E.g. x,y,z,...

Terms represent objects

- The set of terms is inductively defined by the following rules:
 - Constants: Any constant is a term
 - Variables: Any variable is a term
 - Functions: Any Expressions $f(t_1, \dots, t_n)$ of arguments (where each argument is a term and f is a function of arity n) is a term
- Terms without variables are called ground terms
- Examples:
 - c
 - $f(c)$
 - $g(x, x)$
 - $g(f(c), g(x, x))$



Rules of Predicate calculus symbols:

1. Set of letters (uppercase or lowercase) is allowed.
2. Set of digits (0-9) is allowed.
3. Underscore () is allowed.
4. Blanks and non-alphanumeric characters can't be used.
5. Special characters like \$, *, #, and / are not allowed.

Symbols:

1. Predicate Symbols: It denotes relations or functional mapping from the elements of a domain to the values true or false.
2. Function Symbols: It denotes relations defined on a domain.
3. Variable Symbols: Lowercase unsubscribed or subscribed letters like x, y, z, t, u, v, etc. It can assume different values over a given domain.

4. Constants: It is fixed value term. They are individual symbols which are names of objects like 1, 2, 3, etc.
5. Quantifiers: There are two types of Quantifiers:
 - i. Existential Quantifier (\exists): It means for some x or there is no x.
 - ii. Universal Quantifier (\forall): It means for all x.
6. Logical Operators: There are five type of logical operators such as – not(\sim), and (\wedge), or(\vee), implication, equivalence.

Two quantifiers: Universal (\forall) and Existential (\exists)

- Allow us to express properties of collections of objects instead of enumerating objects by name
 - Apply to sentence containing variable
- Universal \forall : true for all substitutions for the variable
 - “for all”: $\forall \langle \text{variables} \rangle \langle \text{sentence} \rangle$
- Existential \exists : true for at least one substitution for the variable
 - “there exists”: $\exists \langle \text{variables} \rangle \langle \text{sentence} \rangle$
- Examples:
 - $\exists x: \text{Mother}(\text{art}) = x$
 - $\forall x \forall y: \text{Mother}(x) = \text{Mother}(y) \rightarrow \text{Sibling}(x,y)$
 - $\exists y \exists x: \text{Mother}(y) = x$

The set of formulas is inductively defined by the following rules:

1. Preciate symbols: If P is an n -ary predicate symbol and t_1, \dots, t_n are terms then $P(t_1, \dots, t_n)$ is a formula.
2. Negation: If ϕ is a formula, then $\neg\phi$ is a formula
3. Binary connectives: If ϕ and ψ are formulas, then $(\phi \rightarrow \psi)$ is a formula. Same for other binary logical connectives.
4. Quantifiers: If ϕ is a formula and x is a variable, then $\forall x\phi$ and $\exists x\phi$ are formulas.
 - Atomic formulas are formulas obtained only using the first rule

Any occurrence of a variable in a formula not in the scope of a quantifier is said to be a free occurrence

- Otherwise it is called a bound occurrence
- Thus, if x is a free variable in ϕ , it is bound in $\forall x\phi$ and $\exists x\phi$
- A formula with no free variables is called a closed formula
- Example: x and y are bound variables, z is a free variable
 $\forall x\forall y(P(f(x)) \rightarrow \neg(P(x)) \rightarrow Q(f(y), x, z))$

$S := \langle \text{Sentence} \rangle \langle \text{Sentence} \rangle :=$
 $\langle \text{AtomicSentence} \rangle \mid \langle \text{Sentence} \rangle \langle \text{Connective} \rangle \langle \text{Sentence} \rangle \mid \langle \text{Quantifier} \rangle \langle \text{Variable} \rangle, \dots \langle \text{Sentence} \rangle$
 $\mid \neg \langle \text{Sentence} \rangle \mid (\langle \text{Sentence} \rangle)$
 $\langle \text{AtomicSentence} \rangle := \langle \text{Predicate} \rangle (\langle \text{Term} \rangle, \dots) \langle \text{Term} \rangle := \langle \text{Function} \rangle (\langle \text{Term} \rangle, \dots)$
 $\mid \langle \text{Constant} \rangle$
 $\mid \langle \text{Variable} \rangle \langle \text{Connective} \rangle := \wedge \mid \vee \mid \rightarrow \mid \leftrightarrow$
 $\langle \text{Quantifier} \rangle := \mid$
 $\langle \text{Constant} \rangle := "c" \mid "x1" \mid "john" \mid \dots$
 $\langle \text{Variable} \rangle := "a" \mid "x" \mid "s" \mid \dots$
 $\langle \text{Predicate} \rangle := "before" \mid "hasColor" \mid "raining" \mid \dots \langle \text{Function} \rangle := "mother" \mid "leftLegOf" \mid \dots$