

SNS COLLEGE OF ENGINEERING Coimbatore - 641 107



TOPIC:11.- Proof methods and strategy.

The Theory of Inference for Predicate calculus Universal Specification (US) If a statement of the form (∀x) [A(x) is assumed to be true, then the universal quantifier can be dropped to obtain A(y) is the for any arbitrary object 'y' in the universe. Existential Specification (ES) From Fr (A(2)) one can conclude A(y), provided that y is not free in any given premis and also not free in any prior step of the dirivation Universal Generalization (UG) Friom A (2) one can / con lude $A(y) \implies (\forall x)(A(x))$ Eaistential Gunnalization (EG) $A(y) \Rightarrow (\exists x)(A(x))$

SNS COLLEGE OF ENGINEERING Coimbatore - 641 107 1. Express The statement "Every student in this class as completed Assignment-I as a quantifiers. Let C(x) : x is in this class A(x): x has completed Assignment - I For all x, if x is in this class, then x has ompleted Assignment - 1. Its symbolic form $(\forall x) (C(x) \rightarrow A(x))$

2.

write each of the following in symbolic form. All men are good (b) No men are good Some men are good (e) Some men are not good Let M(x): x is a man G(x): x is good For all x, x is a man, thun x is good. $(\forall x)$ $(M(x) \rightarrow G(x))$





Show that
$$(\forall x)(P(x) \rightarrow Q(x)) \land (\forall x)(Q(x) \rightarrow R)$$

 $\Rightarrow (\forall x)(P(x) \rightarrow R(x))$
 $\exists i ? i)(\forall x)(P(x) \rightarrow Q(x))$
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 $\exists 1, 3 ? i)(x)(P(x) \rightarrow R(x))$



4)

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Show that $(\forall x)(P(x) \lor Q(x)) \Rightarrow (\forall x) P(x) \lor (\exists x)$ Q(x) We use indirect method, by assuming

 $P(x) P(x) V (\exists x)(Q(x))$ as an additional promise

513	$(\exists x) Q(x) \downarrow (\forall x) P(x) \lor (\exists x) Q(x)]$	Rule P
513	2) $(\exists x) \neg P(x) \land$ $(\forall x) \neg Q(x)$	Rule T (Demorgan's)
113	3) (3x) - p(x)	Rule T (PAQ ⇒ P)
517	4) (+1) - Q(1)	Rule T (PAQ ⇒ Q)
513	5) - P(y)	Rule ES
513	6) - Q(4)	Rule US
£13	7) - P(y) ~ - Q(y)	Rule T (P,Q ⇒ PAQ
513	8) - (P(y) VQ(y))	Rule T (Dumorgan's)
<u></u> <u></u> <u></u> <u></u> <u></u> <u></u> <u></u> <u></u> <u></u> <u></u> <u></u> <u></u> <u></u> <u></u>	9) $(\forall x) (P(x) \vee Q(x))$	Rule P

SNS COLLEGE OF ENGINEERING
Coimbatore - 641 107Rule US
$$\{93$$
 10 $P(y) \lor Q(y)$ $Rule US$ $\{1,93$ 10 $P(y) \lor Q(y)$ $Rule T(P, a \Rightarrow PAQ)$ $\{1,97$ 12 F

5) Verify the validity of the following argument. Find living thing is a plant or animal John's gold fish in alive and it is not a plant. All animals have hearts. Thurefore John's gold fish has a heart. L(x): x is a living thing P(x) : x is a plant A(x) : x is an animal Let

H(x) : x has a heart Then, the given premises are

- (1) $(\forall x) [L(x) \rightarrow (P(x) \lor A(x))]$
 - (2) L(j) A 7 P(j)

(3)
$$(\forall x) [A(x) \rightarrow H(x)]$$

Conclusion



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513	$1) (\forall x) \left[L(x) \rightarrow (P(x) \lor A) \right]$	(x)) Rule P
\$13	2) $L(j) \rightarrow P(j) \vee A(j)$	i) Rule US
{ 3 }	3) L(j) A7P(j)	Rule P
{ 3 }	4) L(j), ¬P(j)	Rule T (Pra ⇒P.a)
{1,3 }	5) P(j) V {A(j)	Rule T(P, P→a⇒a)
51,3}	$_{6)} \neg P(j) \rightarrow A(j)$	Rule T (P→a ⇒ ¬PVQ)
57}	$(\forall x) (A(x) \rightarrow H(x))$	Rule P
<u></u> ۲۲	8) $A(j) \rightarrow H(j)$	Rule US
יין 1,3,7	$q) \neg P(j) \rightarrow \mathbf{M}(j)$	Rule T (P→Q,Q→R ⇒ P→R)
1,3,7 }	10) H(j)	Rule T (P, P→a⇒Q)
800 10	18-5 H 12-12-12-12-12-12-12-12-12-12-12-12-12-1	0.1