



#### **TOPIC:3- Normal Forms**

If we write the given statement in a particular form (interms of  $\Lambda$ , V and  $\neg$ ), then it is called Normal form.

Elementry Product

A product of the statement variables and their negations in a formula is called Elementry products.

For example, let P and Q be any two atomic for example, let P and Q be any two atomic arriables. Then possible elementry products are

P, Q,  $\neg P$ ,  $\neg Q$ ,  $\neg P \land Q$ ,  $\neg Q \land P$ ,  $P \land \neg P$ ,  $Q \land \neg Q$ 

A sum of the two statement variables and their negation is called Elementry sum.

Let P and Q be any two atomic variables.

Then P, Q, PVQ, ¬PVQ, PV¬Q, PV¬PVQ

We some examples of elementry sum.





# Disjunctive Normal Form (DNF)

A statement formula which is equivalent to a given formula and which consists of a sum of elementry products is called a Disjunction Normal Form of the given formula

# Conjunctive Normal Form (CNF)

A statement formula which is equivalent to a given formula and which consists of a product of elementry sum is called a conjunction.
Normal Form of the given formula.

# Principal Normal Forms

Let P and Q be two statement variable then the minterms are PAQ, PATQ, TPAQ, TPATQ

The maxterms a are

pva, pva, pva, pva





Principal Normal Forms

Lit P and a be two statement variable

then the minterms are

PAQ, PATQ, TPAQ, TPATQ

The maxterms a are

PVa, PV-a, -PVa, -PV-a

Prinipal Disjunctive Normal Forms (PDNF)

For a given statement formula, an equivalent formula consisting of disjunction of minterms

is called a Prinipal Disjunctive Normal Forms

Primipal conjunctive Normal Forms (PCNF)

For a given statement formula, an equivalent formula consisting of conjunction of maxterms formula is known as its Principal conjuction only is form (PCNF).





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PCNF and /PDNF. for
(P) R \wedge (Q \leftrightarrow P) .

(P) R \wedge (Q \leftrightarrow P) .

(P) R \wedge (Q \leftrightarrow P) \wedge (P) \wedge (P) \wedge (P)

\Rightarrow (P) \wedge (P) \wedge (P) \wedge (P)

\Rightarrow (P) \wedge (P) \wedge (P) \wedge (P)

⇒ (PVRVF) ∧ [(¬QVPVF) ∧ (¬PVQVF)]

    (PVRV(Q∧¬Q)) Λ [(¬QVPV(R∧¬R)) Λ
                                 (-PVQV(RA-R))
1 (-PVQVR) 1 (-BVQV-R)

    (PVaVR) Λ'(PV¬QVR) Λ (PV¬QVR) Λ(PV¬QV)
    ¬R)

                     A (-PVQVR) A (-PVQMR)
 5 (PVQVR) 1 (PV-QV-R)
           1 (-PVQVR) 1 (-PVQV-R) (PCNF
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2. Obtain the principal disjunctive and conjunctive

normal forms (P -> (QAR)) A (¬P -> (¬QA¬R))

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5 \iff (P \rightarrow (QAR)) \land (\neg P \rightarrow (\neg QA \neg R))
(¬PV(QAR)) A (¬¬PV(¬QA¬R))
 (¬PVQ) A (¬PVR) A (PV¬Q) A (PV¬R)
 ( (PVQVF) A ( PVRVF) A (PV QVF) A (PV RVF)
(¬PVQV(RA¬R)) A (¬PVRV(QA¬Q))
  A (PV - QV (RA - R)) A (PV - RV (QA - Q))
( TPVQVR) A ( TPVQVTR) A (TPVRVQ) A (TPVRVTQ)
 M(PV-QVR) A (PV-QV-R) A (PV-RVQ) A (PV-RV-Q)
s (¬PVQVR) A (¬PVQV¬R) A (¬PVQVR) A (¬PV¬QVR)
  A (PV-QVR) A (PV-QV-R) A (PVQV-R) A (PV-QV-R)
           This is required PCNF
S⇔ (¬PVQVR) A (¬PVQV¬R) A (¬PV¬QVR)A(PV¬QVR)
 1 (PV-QV-R) 1 (PVQV-R) (PCNF)
75 ( TPV TQV TR) A (PVQVR)
T(TS) (PAQAR) V (TPATQATR)
 S (PAQAR) V (¬PA¬QA¬R) (PDNF)
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obtain the PDNF of (PAQ) V(-PAR) V(QAR).

P	a	R	Рла	¬P	-PAR	QAR	(PAQ) V(¬PAR) V(QAR)	Min term
Т	Т	Т	Т	F	F	T	T	PAQAR
т	T	F	Т	F	F	F	1	PA QA¬R
T	F	T	F	F	F	F	F .	
T	F	F	F	F	F ]	F	F	
F	T	T	F	T	T	T	1	- PAQAR
F	T	F	F	Т	F	F	F	
F	F	T	F	T	T	F	(f)	7PA7GAR
F	F	F	F	T	F	F	F	