



Unit-1

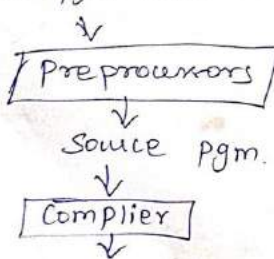
Formal language & Regular expression:-

Languages:-

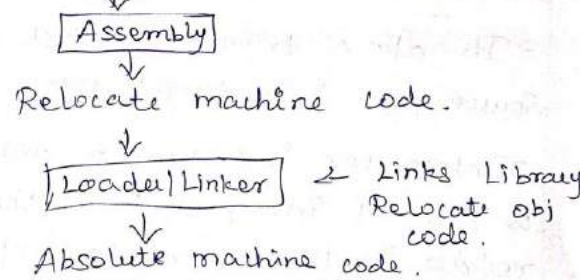
- A source pgm is divided into modules stored in separate files.
- The preprocessor collects the source pgm, expands shorthands called source pgm statements.
- The target pgm from compiler is then translated into assembly code & is then translated using assembler into machine code.

→ A linker in turn, links the library routines with machine code & is then into primary using loader.

source pgm with assembler directives

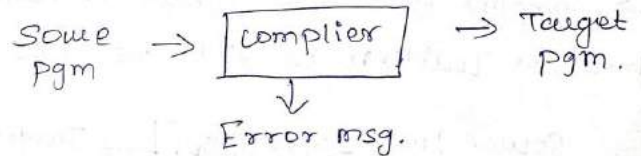


target assembly pgm



Compiler:

→ A compiler is a pgm that reads a pgm written in one language. The source language into equivalent program in another language the target pgm.



→ The source pgm may be developed using any programming lang known such as C, C#, Fortran.

→ The target pgm may be another programming language or the machine lang of any computers.



Interpreters:-

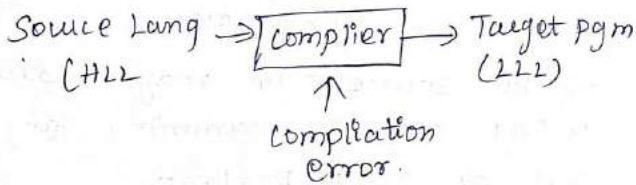
→ Its also a translator which converts the source pgm into target pgm.

→ Interpreter is a pgm in which the code is directly interpreted by the microcode resides in the control memory of a machine and executes the code line by line.

→ This microcode generates the control signals for executions.

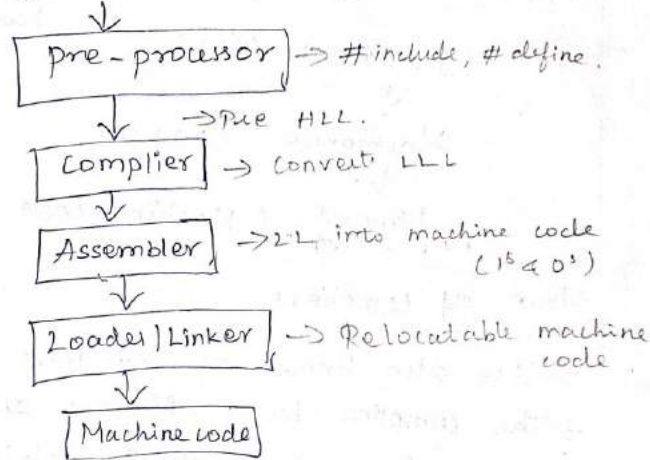
Compiler design:-

→ Compiler is a sw which converts a program written in HLL into LLL.



Language processing sly:-

Source code (HLL):



Ex:-

C-program {HLL}

- ↓
- C compiler translate pgm into LLL (assembly lang)
- ↓
- Assembly translate LLL into machine code.
- ↓
- Linker used to link all parts of pgm together for execution.
- ↓
- Loader loads all them into memory & then the pgm is executed.



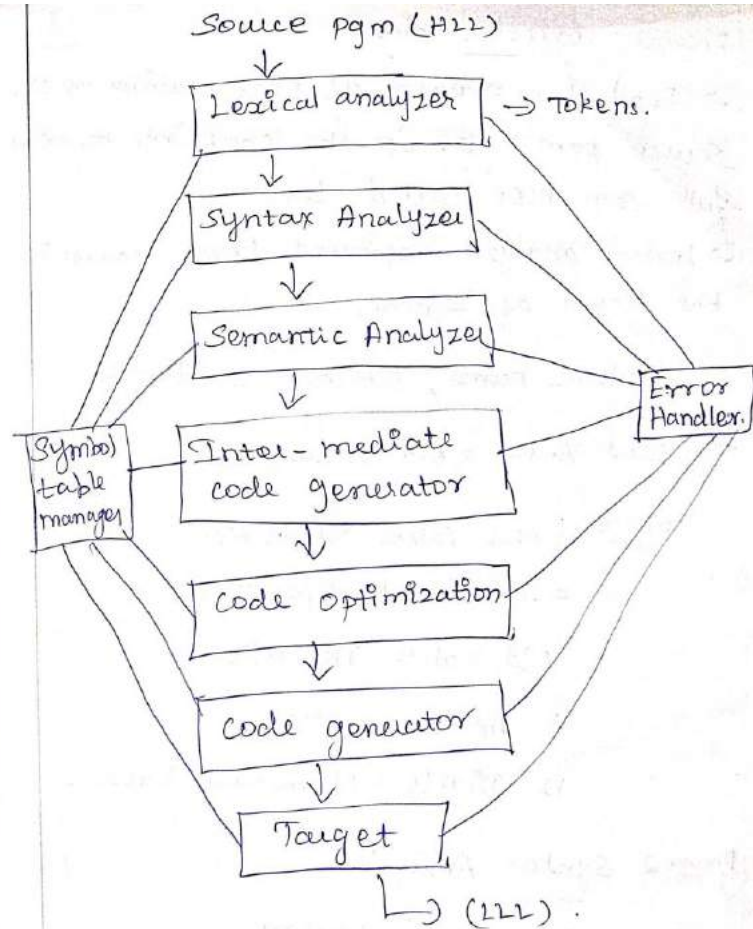
→ Compiler converts HLL to LLL
→ Assembler converts LLL to machine level language.
Statement (HLL)
↓
Mnemonics (LLL)
↓
Binary (Machine code or MLL)

Phase of Compilers:

→ Its also known as structures compilers
→ The compiler have different phase.
→ Phases is a logically interrelated operations that takes some pgm in one representation & produce o/p in another representation.

2 - major phase

- ① Analysis phase → M/c independent & Lang dependent.
- ② Synthesis phase → M/c dependent & Lang independent.





Phase 1: Lexical analyzer:

→ Read the stream of char making up the source pgrm & group the char into meaningful full sequences called lexeme.

→ Lexical analyzer represents them lexemes in the form of tokens.

< token_name, attribute_value >

Eg: new Value := old value := + 12.

Tokens: → new value identifier

= Assignment operators

old value identifier

+ Add operator.

12 Digits | Numerical Values.

Phase 2 Syntax Analysis:

→ It's also called parsing.

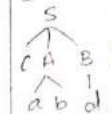
→ It takes token produced by lexical as I/P & generates a parse tree or Syntax Analyzer.

id₁ = id₂ + id₃ = 60

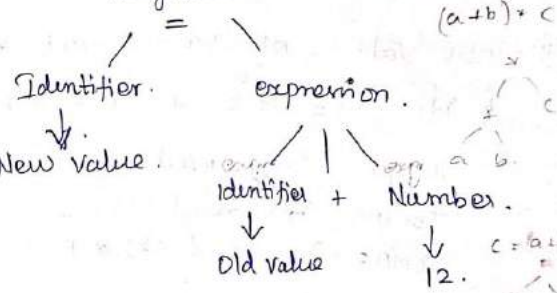


Eg:

S → CAB
A → ab
B → d



Assignment



Phase 3 Semantic Analyzer:

→ It checks whether the parse tree constructed followed the rules of lang. or not

→ Semantics works just check the Syntax.

Eg: Sum = a + b.

int a;
double sum;
char b;

Semantic record.

a: int.
sum: double
b: char.

→ Syntax is correct.

←→ Data type mismatch.

→ semantically not correct.

Phase 4: Intermediate code generation:

→ It's the representation of final m/c lang code is produced.

→ This phase bridges the analysis and



Synthesis phase of translation.

Eg: $new\ val := old\ val + fact * 1$
 $id_1 := id_2 + id_3 * 1$

Temp1 = int read (1)

Temp2 = int read (2)

Temp3 = int read (3) * 1

Temp3 = id2 + Temp2;

$id_1 = Temp3$

Phase B: Code optimisation:

The o/p runs faster & takes less space.

Temp1 = id3 * 1

id1 = id2 + Temp1

Phase C: Code generation:

Translate the intermediate code into sequence of relocatable in a machine code.

Eg: $id_1 := id_2 + id_3 * 1$

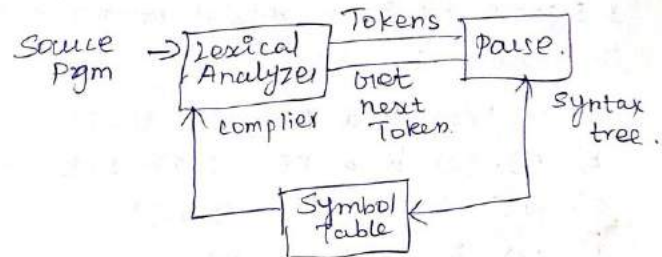
Mov R1, Id3 } Assembly lang
MUL R1, #1 } (LLL)

Compiler converts HLL to LLL.

Lexical Analyzer:

→ Its the first phase of compiler also called as linear or scanning.

→ In this phase of stream of characters making up the pgm is read from left to right & grouped into tokens that are seq of characters having collective machine.



Language:

→ A set of strings all of which are chosen from some Σ^* where Σ is a particular alphabet, is called language.

Eg: Lang over the alphabet $\Sigma = \{a, b\}$ that consists of all strings ending with abb.

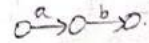
$L = \{abb, aabb, baab, abaabb, \dots\}$

R.E:

Union - $a + b$ (or) $a|b$



Concatination - ab or $a.b$



Closure - Kleen closure - a^* = $\{\epsilon, a, aa, \dots\}$
Positive " - a^+ = $\{a, aa, aaa, \dots\}$



Regular Expression:

→ A regular Expression is built out of simpler R.E using a set of definite rules

→ Each rule (R.E) r denotes a language L(r).

- 1) ϵ is a regular expression denotes the lang $\{\epsilon\}$
- 2) If 'a' is a symbol in Σ , then a is the regular expression denotes the lang $\{a\}$.
- 3) Suppose r & s are regular expression denoting the lang $L(r)$ & $L(s)$.

- a) $(r) | (s)$ is a RE $L(r) \cup L(s)$ Union.
- b) $(r) \cdot (s)$ is a RE $L(r) \cdot L(s)$ concatenation.
- c) $(r)^*$ is a RE $(L(r))^*$ Kleen closure.
- d) (r) is a RE $L(r)$.

The precedence & associativity of operators.

- 1) Unary operator (*) has highest precedence & is left associative
- 2) Concatenation operator has 2nd highest precedence & its left associ
- 3) | has the lowest precedence & its left associatives.

Finite automata or automata: NFA
DFA

A finite automata has (5-tuples)

$M = (Q, \Sigma, \delta, q_0, F)$

When $Q =$ Finite set of states.

$\Sigma =$ Finite set of Symbols called I/P alphabet

$\delta: Q \times \Sigma \rightarrow Q =$ Transition function (or) mapping fun.

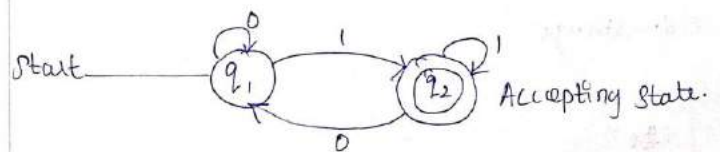
$q_0 \in Q =$ Initial state (or) Start state

$F \subseteq Q =$ Set of final state.

Transition Diagram:

→ A transition diagram is a directed graph associated with the vertices of the graph corresponds to the states of finite automata.

→ The transition from state 'p' to state 'q'.





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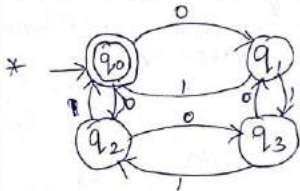
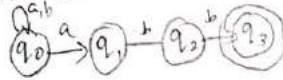
Language Acceptance by Finite automata:

Eg: Given $M = (Q, \Sigma, \delta, q_0, F)$.

$Q = \{q_0, q_1, q_2, q_3\}$. [abb]

$\Sigma = \{0, 1\}$

$F = \{q_0\}$.



String 110101 is accepted by FA or not.

Sol:

$\rightarrow q_0$	0	1
q_1	q_1	q_2
q_2	q_0	q_3
q_3	q_3	q_0
	q_1	q_2

strings.

✗

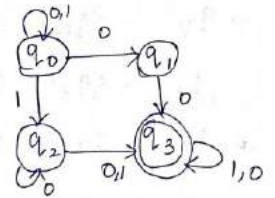
Finite automata can be classified as,

- ① NFA - Non-deterministic finite automata
- ② DFA - Deterministic finite automata.

NFA:

Ex: Design NFA function, with using Transition Table.

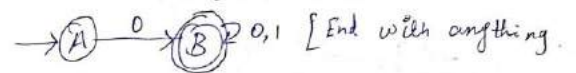
State	0	1
$\rightarrow q_0$	q_0, q_1	q_0, q_2
$\rightarrow q_1$	q_3	ϵ
$\rightarrow q_2$	q_2, q_3	q_3
$\rightarrow q_3$	q_3	q_3



Ex: Construct NFA, $L = \{ \text{Set of all strings that start with } 0 \}$

$\Sigma = \{0, 1\}$. Min length = 1.

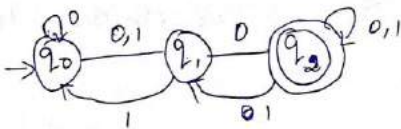
$L = \{0, 01, 001, 0001, 0101, \dots\}$





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Ex3: $Q = \{q_0, q_1, q_2\}$
 $\Sigma = \{0, 1\}$ $q_0 = \{q_0\}$ $F = \{q_2\}$

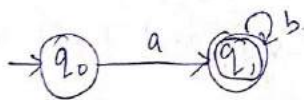


States	0	1
$\rightarrow q_0$	$\{q_0, q_1\}$	$\{q_1\}$
q_1	$\{q_2\}$	$\{q_0\}$
$* q_2$	$\{q_2\}$	$\{q_2, q_1\}$

Ex4: Construct NFA where language is given as strings with 'a'.

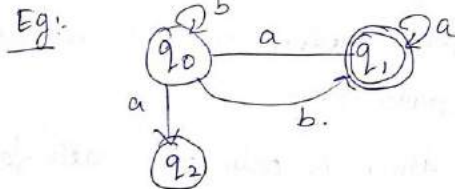
$\Sigma = \{a, b\}$

Sol: $L = \{a, ab, aa, aab, aabab, \dots\}$



NFA - many paths for specific I/P.
 → The FA are called NFA, when there exist many paths for specific I/P from the current state to the next state.
 → It's easy to construct NFA than DFA for a given RL.
 → Every NFA is not DFA, but each NFA can be translated into DFA.
 → NFA is defined in the same way as DFA but with two exceptions.

- ↳ It contains multiple next state.
- ↳ It contains ϵ transitions.



Formal definition of NFA:

→ NFA also have five states same as DFA, but with different transition function.



current state → I/P → multiple state

$$S: Q \times \Sigma \rightarrow 2^Q$$

- where,
- Q: Finite set of states
 - Σ : Finite set of I/P symbol.
 - q_0 : ^{initial} Final state
 - F: Final state
 - S: Transition function.

DFA:

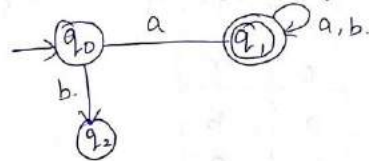
→ The finite automata are called deterministic finite automata if the m/c is read an I/P string one symbol at a time.

→ Deterministic refers to the uniqueness of the computation.

→ In DFA, there is only one path for specific I/P from the current state to the next state.

→ DFA does not accept the null move, is DFA cannot change state any I/P character.

→ DFA can contain multiple final states, its used in lexical analysis in compiler.



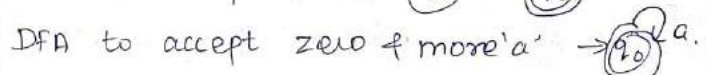
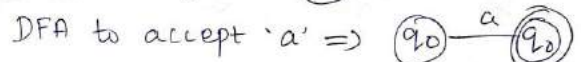
Formal definition of DFA:

- Q: finite set of state.
- Σ : Finite set of I/P symbol
- q_0 : initial state
- F: Final "
- S: Transition Function → $S: Q \times \Sigma \rightarrow Q$.

Accepting Language:

Eg: $L = \{ \emptyset \} \Rightarrow q_0$

$L = \{ \epsilon \} \Rightarrow q_0$



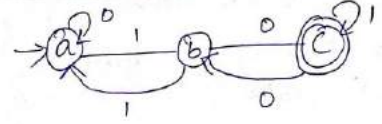
$L = \{ \epsilon, a, aa, aaa, \dots \}$



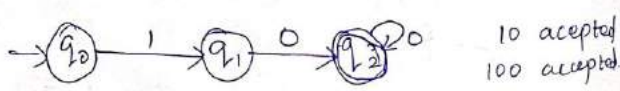
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Ex1: Construct DFA. $\Sigma = \{a, b, c\}$ $Q_0 = \{a\}$
 $\Sigma = \{0, 1\}$ $F = \{c\}$

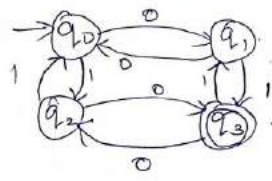
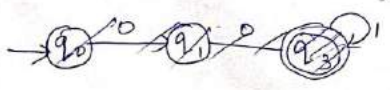
Present state	0	1
$\rightarrow a$	a	b
b	c	a
* c	b	c



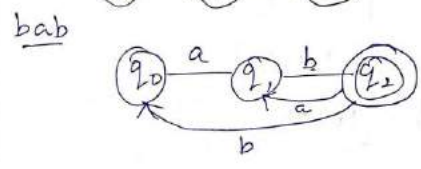
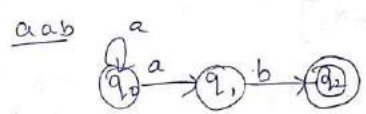
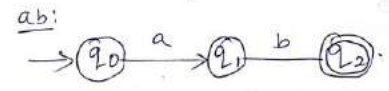
Ex2: Design DFA with $\Sigma = \{0, 1\}$ accepts those string which starts with 1 & ends with 0.
 $L = \{10, 100, 1010, 11110, \dots\}$



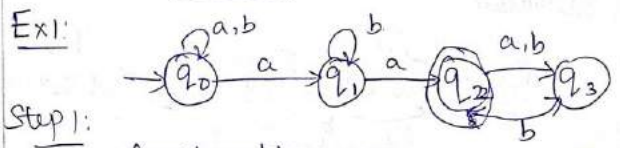
Ex3: Design FA with $\Sigma = \{0, 1\}$ accepts even no. of 0's & Even no. of 1's.
 $L = \{00, 11, 0011, 1100, \dots\}$



Ex4: Construct DFA accepting all strings over $\{a, b\}$ ending with 'ab'.
 $L = \{ab, aab, bab, bbab, aaab, \dots\}$



Conversion of NFA to DFA:



Step 1: Constructing Transition Table.



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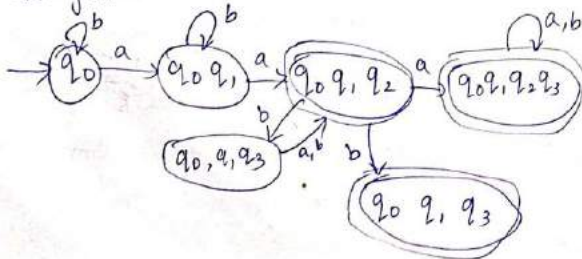
NFA Transition Table:

S	a	b
→ q ₀	{q ₀ , q ₁ }	q ₀
q ₁	q ₂	q ₁
* q ₂	q ₃	q ₃
* q ₃	-	q ₂

DFA Table:

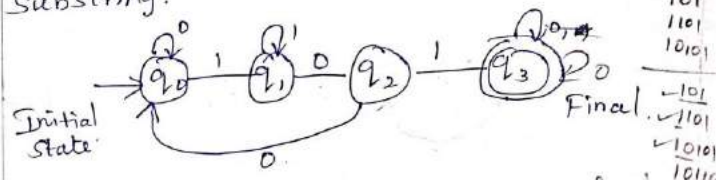
S	a	b
→ q ₀	[q ₀ , q ₁]	q ₀
[q ₀ , q ₁]	[q ₀ , q ₁ , q ₂]	[q ₀ , q ₁]
[q ₀ , q ₁ , q ₂]	[q ₀ , q ₁ , q ₂ , q ₃]	[q ₀ , q ₁ , q ₃]
[q ₀ , q ₁ , q ₂ , q ₃]	[q ₀ , q ₁ , q ₂ , q ₃]	[q ₀ , q ₁ , q ₃ , q ₂]
[q ₀ , q ₁ , q ₃]	[q ₀ , q ₁ , q ₂ , q ₃]	[q ₀ , q ₁ , q ₂]

DFA Diagram:

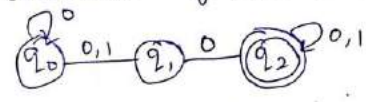


Write/expand/convert DFA. Grate Question:

Design a DFA that accepts '101' as substring.



Ex:2: conversion of NFA to DFA.

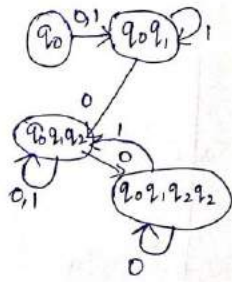


Transition Table for NFA.

S	0	1
→ q ₀	{q ₀ , q ₁ , q ₂ }	[q ₀ , q ₁]
q ₁	q ₂	-
* q ₂	q ₂	q ₂

DFA Table.

S	0	1
→ q ₀	[q ₀ , q ₁]	[q ₀ , q ₁]
[q ₀ , q ₁]	[q ₀ , q ₁ , q ₂]	[q ₀ , q ₁]
[q ₀ , q ₁ , q ₂]	[q ₀ , q ₁ , q ₂ , q ₂]	[q ₀ , q ₁ , q ₂]
[q ₀ , q ₁ , q ₂ , q ₂]	[q ₀ , q ₁ , q ₂ , q ₂]	[q ₀ , q ₁ , q ₂]





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Application of finite automata to lexical Analysis

LEX Tool:

→ Its main job is to break I/P an I/P stream into the token.

→ lex is a tool for automatically generating a lexer.

Step 1: lex source prog

lex.l

↓

lex
Compiles

→ lex.yy.c

Step 2:

lex.yy.c → C Compiler → a.out

↓
L.A.

Step 3:

I/P stream → a.out → seq of tokens

I/P → LA → tokens
↑
Lex

Structure of lex program:-

{ declaration } → Declare the variables.
% %.

{ translation rules } → have the pattern
{ Action }
% %.

{ auxiliary functions } ⇒ fns can be compiled separately.



Ex: lex program:

→ program to count the no. of vowels & constants in a given grammar.

```

% { #include <stdio.h>
  int vowels=0;
  int cons=0;
% }
%.*
[aeiou AEIOU] { vowels++; }
[a-zA-Z] { cons++; }
%.*
int yywrap()
{ return 1;
}
main() {
  Pf ("Enter the string at End press ^d\n");
  YY lex (); → lex tool.
  Pf ("no. of vowels = %d\n",
      no. of constants = %d\n",
      vowels, cons);
}

```

// stream
↓
Grammar

Unit-2

Context Free Grammar

CFG stands for context free grammar. It is a formal grammar which is used to generate all possible patterns of string in a given finite language (FL).

CFG can be defined as a tuple.

$G = (V, T, P, S)$

G - Grammar

V - Non-Terminal / Uppercase

T - Terminal / lowercase

P - set of production rules

S - non-terminal symbols (L.S production)

S - Terminal symbol (R.S production)

S - Start symbol. used to derive the string.

Ex 1: construct CFG for the language having any no. of a's over the set $\Sigma = \{a\}$.

Sol: $G = \{V, T, P, S\}$

$\Sigma \cup \{P \text{ symbol}\} = \{a\}$

$V = \{E, a, aa, aaa, aaaa, \dots\}$



R.E = a^* derive i/p = "aaaaaa"

Production rule:
 $S \rightarrow aS$ - (1)
 $S \rightarrow \epsilon$ - (2)

Diagram showing derivation of "aaaaaa":
 S
 aS
 aaS
 $aaas$
 $aaaaS$
 $aaaaaS$
 $aaaaaaS$

Ex2: construct a CFG for the lang $L = a^n b^{2^n}$ where $n \geq 1$.
 $L = \{ abb, aabbbb, aaabbbbb, \dots \}$

The grammar could be,
 $S \rightarrow asbb$
 $S \rightarrow abb$

aaabbbbb to derive.
 $S \rightarrow asbb$
 $S \rightarrow aasbb$ { $S \rightarrow asbb$ }
 $S \rightarrow aaabbbbb$ { $S \rightarrow abb$ }

$S \rightarrow aAB$
 $A \rightarrow aA$
 $B \rightarrow bB | b$

$V = \{V, T, P, S\}$
 $\Sigma = \{A, B, S\}, \{a, b\}, \{P, S\}$

Derivations:

Derivation is a seq of production rules. It is used to get i/p strings. During parsing we have to take two decisions:

- * we have to decide the non-terminal which is to be replaced.
- * we have to decide the production rule by which the non-terminal will be replaced.

→ we have two options to be decided, which non terminal to be replaced with production rule.

- ① Left most derivation.
- ② Right most derivation

Left most derivation: [Left to Right].
 → In the left most derivation, the i/p. is scanned & replaced with the production rule from left to right.
 → so we have to read i/p string from left to right.



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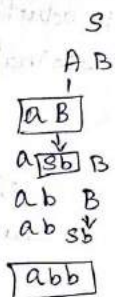


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Ex1: Derive the string "abb" for left most & Right most derivation using CFG given by:

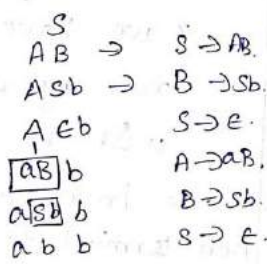
$S \rightarrow AB|E$
 $A \rightarrow aB$
 $B \rightarrow sb.$

Left most



$S \rightarrow AB.$
 $A \rightarrow aB.$
 $B \rightarrow sb.$
 $S \rightarrow E.$
 $B \rightarrow sb.$
 $S \rightarrow E.$

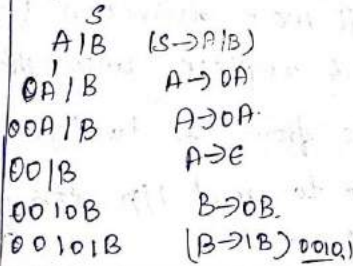
Right most derivation



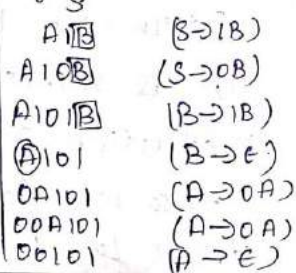
Ex2: Derive string '00101' L.M.D & R.M.D.

$S \rightarrow A|B$
 $A \rightarrow 0A|E$
 $B \rightarrow 0B|1B|E$

Left most derivation:



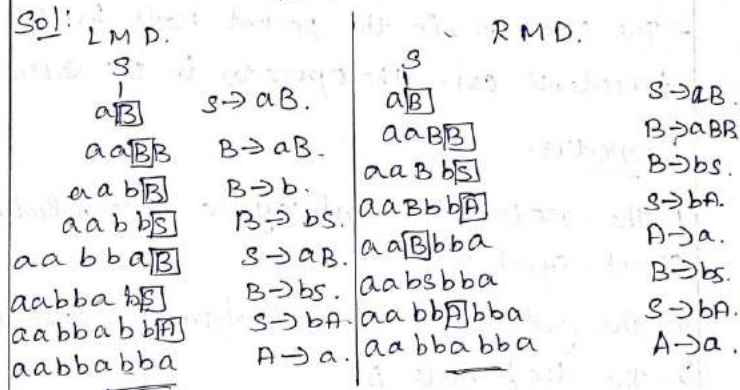
Right most derivation



Ex: String aabbabba LMD & R.M.D.

$S \rightarrow aB|BA$
 $A \rightarrow a|aA|bAA$
 $B \rightarrow b|bs|aBB.$

Sol:



Parse tree:-

→ It's a graphical representation for the derivation of the given production rules for a given CFG.

→ It's a simple way to show how the derivation can be done to obtain some string from a given set of production rules.

→ It's also called as parse tree.



- The parse tree follows the precedence of operators.
- The deepest subtree traversed first
- The operator in the parent node has less precedence over the operator in the subtree

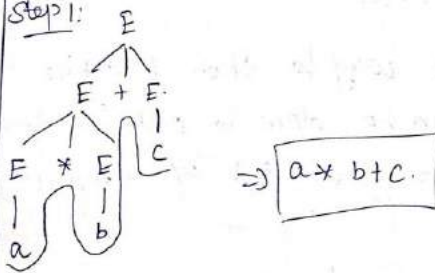
Properties:

1. The root node is always a node indicating start symbols.
2. The derivation is read from left to right.
3. The leaf node is

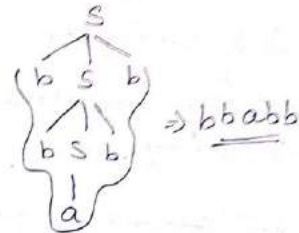
Ex: production Rules:

$$\begin{array}{l}
 E = E + E \\
 E = E * E \\
 E = a | b | c
 \end{array}
 \quad \text{||P:}
 \quad
 \begin{array}{l}
 a * b + c
 \end{array}$$

Step 1:

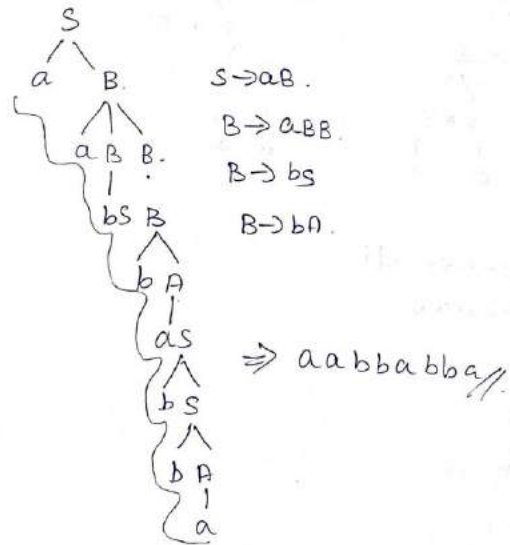


Ex1: parse tree for the string bbabb from the CFG given by, $S \rightarrow bsb | a | b$.



Ex2: parse tree for the string aabbabba

$$\begin{array}{l}
 S \rightarrow aB | bA \\
 A \rightarrow a | as | bAA \\
 B \rightarrow b | bs | aBB
 \end{array}$$



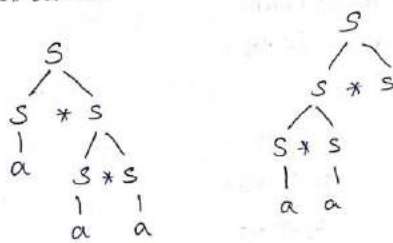


Ambiguity LL(k) grammars:

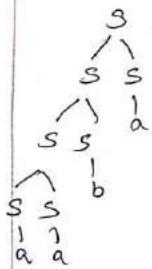
→ If two or more left derivation trees are possible is called ambiguity.

→ One or more than one tree can be generated for the same string.

Ex1: If G is the Grammar, $S \rightarrow S+S/S * S/a$
Show that G is ambiguous with the string $w = a * a * a$.



Ex2: P: $s \rightarrow ss|ab$
 $w = aaba$.



LL parser:

→ It accepts (L) grammar. It is denoted as LL(k).

→ The first L → represents the lp from left to right.

→ The second L → represents the left most derivation.

→ k represents the no. of look a heads (How many time you trag the list. generally k=1)

$\therefore LL(k) = LL(1)$.

→ A grammar G is LL(1), If there are two distinct production.

$A \rightarrow (a/B)$

Condition:

- ① For no terminal $\alpha < \beta$ derive string beginning with a.
- ② At most one of $\alpha & \beta$ can derive empty string.
- ③ If $B \rightarrow \epsilon$, then 'a' does not derive any string beginning with a terminal in Follow(A).

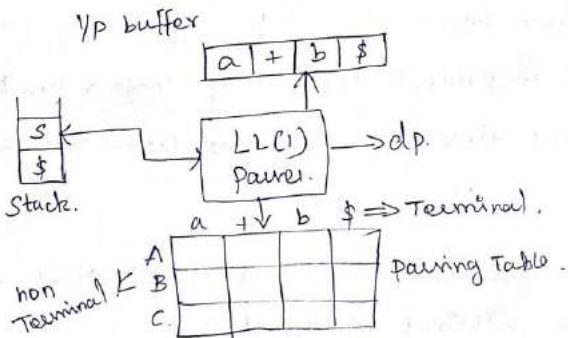


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→ LL(1) use data structure are,

- ↳ i/p buffer
- ↳ stack
- ↳ parsing table.

Structure of LL(1):



Construction of predictive LL(1)

- ① FIRST() / Leading().
- FOLLOW() / Trailing().
- ② Predictive parsing table by using first & follow functions.
- ③ Parse the i/p string with the help of the table.

Ex1: Construction of predictive parse LL(1)

$E \rightarrow TE'$
 $E' \rightarrow +TE' | \epsilon$
 $T \rightarrow *FT'$
 $T' \rightarrow *FT' | \epsilon$
 $F \rightarrow (E) | id$

- ① First & Follow.
- ② Parsing Table.
- ③ Stack Implementation.
- ④ parse tree.

Step 1: First function

$First(F) = \{ (, id \}$
 $First(T') = \{ *, \epsilon \}$
 $First(T) = \{ (, id \}$
 $First(E') = \{ +, \epsilon \}$
 $First(E) = \{ (, id \}$

Step 2: Follow function.

$Follow(E) = \{ \$,) \}$
 $Follow(E') = \{ \$,) \}$
 $Follow(T) = \{ First(E') - \epsilon \}$
 $\cup Follow(E) = \{ +, \$,) \}$
 $Follow(T') = \{ +, \$,) \}$
 $Follow(F) = \{ *, +,), \$ \}$

Step 3: Whenever no ϵ need to go follow fun construct the parsing Table.

	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow TE'$				$E' \rightarrow \epsilon$ $E' \rightarrow \$$
T				$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow id$			$F \rightarrow (E)$		



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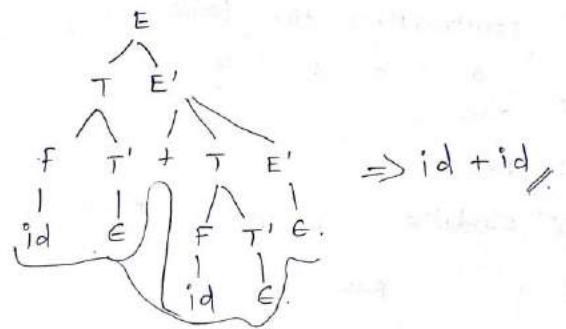


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Step 3: Implements the stack.

Stack	IP	Action.
$\leftarrow E \$$	idtid \$	$E \rightarrow TE'$
TE' \$	idtid \$	$T \rightarrow FT'$
FT'E' \$	idtid \$	$F \rightarrow id$
idT'E' \$	idtid \$	pop id.
T'E' \$	+id \$	$T \rightarrow E$
E' \$	+id \$	$E' \rightarrow +TE'$
+TE' \$	+id \$	pop +.
TE'	id \$	$T \rightarrow FT'$
FT'E'	id \$	$F \rightarrow id$
idT'E'	id \$	pop id.
T'E'	\$	$T \rightarrow E$
E' \$	\$	$E' \rightarrow E$
\$	\$	Accepted.

Step 4: parse tree:



Ex 2: LL(1) parsing, the given grammar.

IP string: abd \$
 $S \rightarrow A$
 $A \rightarrow aB + Ad$
 $B \rightarrow b$
 $C \rightarrow g$
 $S \rightarrow A$
 $A \rightarrow aBA'$
 $A' \rightarrow dA' | E$
 $B \rightarrow b$
 $C \rightarrow g$

Step 1:

First function:
 First (S) = First (A) = {a}
 First (A) = {a}
 First (A') = {d, e}
 First (B) = {b}
 First (C) = {g}

Follow function.

Follow (S) = { \$ }
 Follow (A) = Follow (S) = { \$ }
 Follow (A') = Follow (A) = { \$ }
 Follow (B) = Follow (A) = { \$ }
 Follow (C) = NA.



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Step 2:

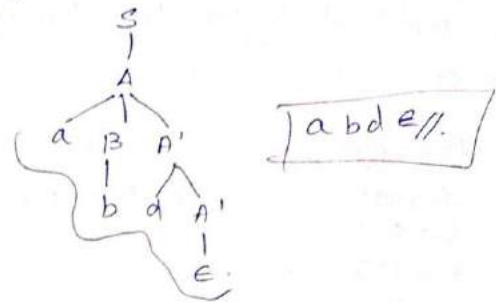
constructing the table.

	a	b	d	g	\$
S	$S \rightarrow A$				
A	$A \rightarrow aBA'$				
A'	$A' \rightarrow aA'$		$A' \rightarrow dA'$		$A' \rightarrow \epsilon$
B		$B \rightarrow b$			
C				$C \rightarrow g$	

Step 3 Implementation of stack by using parsing table.

Stack	I/P	Action
S\$	abd\$	$S \rightarrow A$
A\$	abd\$	$A \rightarrow aBA'$
aBA'\$	abd\$	pop a
BA'\$	bd\$	$B \rightarrow b$
Ba'\$	bd\$	pop b
A'\$	d\$	$A' \rightarrow dA'$
dA'\$	d\$	pop d
A'\$	\$	$A' \rightarrow \epsilon$
\$	\$	Accept (The I/P is properly parse)

Step 1: parse tree.



Bottom up parsing (Shift Reduce parsing):

→ Shift Reduce parsing is a process of reducing a string to the start symbol of a grammar.

→ It uses a stack to hold the grammar & an I/P to hold the string.

A string Reduce → the starting symbol.

→ Shift Reducing parsing perform two action:
① Shift ② Reduce.

→ Shift action, the current symbol in the I/P string is pushed on stack.

→ At each reduction, the symbol will be replaced by the non-terminals.



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→ The symbol is the right side of production & non-terminal is the left side of the production.

Ex1: Grammar
 $S \rightarrow s+s$
 $S \rightarrow S-S$
 $S \rightarrow (S)$
 $S \rightarrow a$

I/P string
 $a_1-(a_2+a_3)$

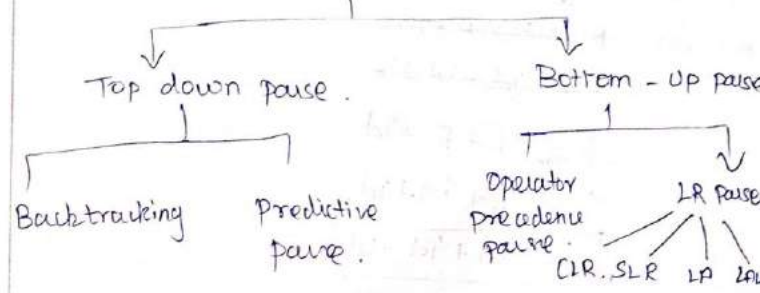
Stack	I/P string	Action
\$	$a_1-(a_2+a_3)$	shift a_1
$\$ a_1$	$-(a_2+a_3)$	reduce by $S \rightarrow a$
$\$ S$	$-(a_2+a_3)$	shift -
$\$ S-$	a_2+a_3	shift a_2
$\$ S-(a_2$	$+a_3)$	reduce by $S \rightarrow a$
$\$ S-(S$	$+a_3)$	shift +
$\$ S-(S+$	$a_3)$	shift a_3
$\$ S-(S+a_3$	$)$	steps reduced by $S \rightarrow S+S$
$\$ S-(S+S)$	$$	reduced by $S \rightarrow S$
$\$ S-(S)$	$$	reduced by $S \rightarrow S$
$\$ S-S$	$$	reduced $S \rightarrow S$
$\$$	$$	Accept parsing.

Ex2: $E \rightarrow 2E2$
 $E \rightarrow 3E3$
 $E \rightarrow 4$

I/P string 32423.

Stack	I/P string	Action
Empty stack $\$$	32423	shift 3.
$\$ 3$	2423	shift 2.
$\$ 32$	423	shift 4.
$\$ 324$	23	Reduce $E \rightarrow 4$.
$\rightarrow \$ 32E$	23	shift 2.
$\rightarrow \$ 32E2$	3	Reduce $E \rightarrow 2E2$
$\rightarrow \$ 3E$	3	shift 3.
$\rightarrow \$ 3E3$	$$	Reduce $E \rightarrow 3E3$.
$\rightarrow \$ E$	$$	Accept the string.

Types of parsing.





Handle parsing:

→ "Handle" is a string of substring that matches the right side of the production and we can reduce such string by a non-terminal on left hand side production

→ "Handle" of right sentential form α is production of β where the string B may be found & replaced by A to produce the previous right sentential form in RMD of β .

$$E \Rightarrow E + E$$
$$E \Rightarrow id$$

id+id+id in RMD

$$E \Rightarrow E + E$$

$$E \Rightarrow E + E + E$$

~~$$E \Rightarrow E + E + E + E$$~~

~~$$E \Rightarrow id + id + id$$~~

$$E \Rightarrow E + E + id$$

$$E \Rightarrow E + id + id$$

$$E \Rightarrow id + id + id$$

Right sentential form	Handle	production.
id + id + id.	id	$E \rightarrow id$
E + id + id	id	$E \rightarrow id$
E + E + id	id	$E \rightarrow id$
E + E + E	E+E	$E \rightarrow E+E$
E+E	E+E	$E \rightarrow E+E$
$E \rightarrow Root$		

LR Grammar parsing:

Various steps involved in parsing.

- For the given i/p string write context free grammar.
- check ambiguity of the grammar.
- Add augment production in the given grammar.
- create canonical collection of LR(0) items
- Draw a data flow diagram (DFA)
- Construct LR(0) parsing table.