## SNS COLLEGE OF ENGINEERING

Kurumbapalayam (Po), Coimbatore - 641107

## An Autonomous Institution

Accredited by NBA - AICTE and Accredited by NAAC - UGC with 'A' Grade Approved by AICTE, New Delhi \& Affiliated to Anna University, Chennai

## DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING

COURSE NAME : 19CS503 Cryptography and Network Security
III YEAR /V SEMESTER
Unit 1- Introduction
Topic: Substitution Techniques-02
$\square$


[^0]
## Recap : Classification of Cryptography



## Substitution Techniques

$\square$ A substitution technique is one in which the letters of plaintext are replaced by other letters or by numbers or symbols.
$\square$ Caesar Cipher
$\square$ Monoalphabetic Ciphers

- Playfair Cipher
$\square$ Hill Cipher
$\square$ Polyalphabetic Ciphers
- One-Time Pad


## Hill Cipher

$\square$ Multiletter Cipher
Lester Hill in 1929 - Mathematician
$\square$ Encryption

$\square \mathrm{m}$ successive plaintext - Substitutes to m cipher text Letters
$\square \mathrm{m}=$ linear
$\square$ Each character assigned with numeric values ( $a=0, b=1 \ldots . . \mathrm{z}=25$ )


## Hill Cipher

$\square$ If m = 3, General form

$$
\begin{aligned}
c_{1} & =\left(k_{11} p_{1}+k_{12} p_{2}+k_{13} p_{3}\right) \bmod 26 \\
c_{2} & =\left(k_{21} p_{1}+k_{22} p_{2}+k_{23} p_{3}\right) \bmod 26 \\
c_{3} & =\left(k_{31} p_{1}+k_{32} p_{2}+k_{33} p_{3}\right) \bmod 26
\end{aligned}
$$

Expressed in column vectors and matrices

$$
\begin{aligned}
& C=E(K, P)=K P \bmod 26 \\
& P=D(K, P)=K^{-1} C \bmod 26=K^{-1} K P=P
\end{aligned}
$$

$$
\left(\begin{array}{l}
c_{1} \\
c_{2} \\
c_{3}
\end{array}\right)=\left(\begin{array}{lll}
k_{11} & k_{12} & k_{13} \\
k_{21} & k_{22} & k_{23} \\
k_{31} & k_{32} & k_{33}
\end{array}\right)\left(\begin{array}{l}
p_{1} \\
p_{2} \\
p_{3}
\end{array}\right) \bmod 26
$$

## Hill Cipher

Consider $\mathrm{m}=3$, the plain text " paymoremoney

$$
P=\left(\begin{array}{cccc}
p & m & e & n \\
a & o & m & e \\
y & r & o & y
\end{array}\right) \quad P=\left(\begin{array}{cccc}
15 & 12 & 4 & 13 \\
0 & 14 & 12 & 4 \\
24 & 17 & 14 & 24
\end{array}\right)
$$

$\square$ Encryption Key

$$
K=\left(\begin{array}{ccc}
17 & 17 & 5 \\
21 & 18 & 21 \\
2 & 2 & 19
\end{array}\right)
$$

## Hill Cipher

$$
\begin{aligned}
& P . T_{1}=\left[\begin{array}{l}
p \\
a \\
y
\end{array}\right]=\left[\begin{array}{c}
15 \\
0 \\
24
\end{array}\right] \\
& C . T_{1}=\text { Key } x P . T_{1} \bmod 26=\left[\begin{array}{ccc}
17 & 17 & 5 \\
21 & 18 & 21 \\
2 & 2 & 19
\end{array}\right]\left[\begin{array}{c}
15 \\
0 \\
24
\end{array}\right] \bmod 26=\left[\begin{array}{c}
11 \\
13 \\
18
\end{array}\right]=\left[\begin{array}{l}
L \\
N \\
S
\end{array}\right] \\
& C . T_{2}=\text { Key } x P . T_{2} \bmod 26=\left[\begin{array}{ccc}
17 & 17 & 5 \\
21 & 18 & 21 \\
2 & 2 & 19
\end{array}\right]\left[\begin{array}{c}
12 \\
14 \\
17
\end{array}\right] \bmod 26=\left[\begin{array}{c}
7 \\
3 \\
11
\end{array}\right]=\left[\begin{array}{l}
H \\
D \\
L
\end{array}\right]
\end{aligned}
$$

## Find the Cipher for the rest of the Example

$$
P \cdot T_{3}=\left(\begin{array}{c}
e \\
m \\
o
\end{array}\right)
$$

$$
P \cdot T_{4}=\left(\begin{array}{l}
n \\
e \\
y
\end{array}\right)
$$



## Decryption using Hill Cipher

Decryption - inverse of $\mathrm{K}^{-1}$
We know that, $\mathrm{K} \mathrm{K}^{-1}=\mathrm{K}^{-1} \mathrm{~K}=\mathrm{I}$

$$
\begin{aligned}
K=\left(\begin{array}{ccc}
17 & 17 & 5 \\
21 & 18 & 21 \\
2 & 2 & 19
\end{array}\right) \quad K^{-1}= & \left(\begin{array}{ccc}
4 & 9 & 15 \\
15 & 17 & 6 \\
24 & 0 & 17
\end{array}\right) \quad K K^{-1}=\left(\begin{array}{ccc}
17 & 17 & 5 \\
21 & 18 & 21 \\
2 & 2 & 19
\end{array}\right)\left(\begin{array}{ccc}
4 & 9 & 15 \\
15 & 17 & 6 \\
24 & 0 & 17
\end{array}\right) \\
& =\left(\begin{array}{ccc}
443 & 442 & 442 \\
858 & 495 & 780 \\
494 & 52 & 365
\end{array}\right) \bmod 26=\left(\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right)
\end{aligned}
$$

## Activity

## Polyalphabetic Cipher

- The first known polyalphabetic cipher was the Alberti Cipher invented by Leon Battista Alberti in around 1467.
- Vigenère Cipher $\mathrm{C}_{\mathrm{i}}=\mathrm{P}_{\mathrm{i}}$ XOR $_{\mathrm{K}} \mathrm{P}_{\mathrm{i}}=\mathrm{C}_{\mathrm{i}}$ XOR $\mathrm{K}_{\mathrm{i}}$



## Vigenère Cipher Table

|  | A | B | C | D | E | F | G | H | I | $J$ | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | Z |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | A | B | C | D | E | F | G | H | I | J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | $z$ |
| B | B | C | D | E | F | G | H | I | J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | z | A |
| C | C | D | E | F | G | H | I | J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | z | A | B |
| D | D | E | F | G | H | I | J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | $z$ | A | B | C |
| E | E | F | G | H | I | $J$ | K | L | M | N | $\bigcirc$ | P | Q | R | S | T | U | V | W | X | Y | z | A | B | C | D |
| F | F | G | H | I | J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | z | A | B | C | D | E |
| G | G | H | I | J | K | L | M | H | 0 | P | Q | R | S | T | U | V | W | X | $Y$ | $z$ | A | B | C | D | E | F |
| H | H | I | J | K | L | M | H | 0 | P | Q | R | S | T | U | V | W | X | Y | z | A | B | C | D | E | F | G |
| I | I | J | K | L | M | H | 0 | P | Q | R | S | T | U | V | W | X | Y | z | A | B | C | D | E | F | G | H |
| $\boldsymbol{J}$ | J | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | $z$ | A | B | C | D | E | F | G | H | I |
| K | K | L | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | z | A | B | C | D | E | F | G | H | I | J |
| L | L | M | H | 0 | P | Q | R | S | T | U | V | W | X | Y | z | A | B | C | D | E | F | G | H | I | J | K |
| M | M | N | 0 | P | Q | R | S | T | U | V | W | X | Y | 2 | A | B | C | D | E | F | G | H | I | J | K | L |
| N | N | 0 | P | $Q$ | R | S | T | U | V | W | X | Y | z | A | B | C | D | E | F | G | H | I | $J$ | K | L | M |
| O | 0 | P | $Q$ | R | 5 | T | U | V | W | X | Y | z | A | B | C | D | E | F | G | H | I | $J$ | K | L | M | N |
| P | P | $Q$ | R | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | 0 |
| Q | Q | R | S | T | U | V | W | X | Y | z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | 0 | P |
| R | R | S | T | V | V | W | X | Y | 2 | A | B | C | D | E | F | G | H | I | J | K | L | M | H | 0 | P | Q |
| S | S | T | U | V | W | X | Y | Z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | 0 | P | Q | R |
| T | T | U | V | W | X | Y | 2 | A | B | C | D | E | F | G | H | I | J | K | L | M | N | 0 | P | Q | R | S |
| U | U | V | W | X | Y | $z$ | A | B | C | D | E | F | G | H | I | J | K | L | M | N | 0 | P | Q | R | S | T |
| V | V | W | X | Y | $z$ | A | B | C | D | E | F | G | H | I | J | K | L | M | N | $\bigcirc$ | P | Q | R | S | T | U |
| W | W | X | Y | z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | $\bigcirc$ | P | Q | R | S | T | U | V |
| X | X | Y | z | A | B | C | D | E | F | G | H | I | J | K | L | M | H | 0 | P | Q | R | S | T | U | V | W |
| Y | $Y$ | z | A | B | C | D | E | F | G | H | I | J | K | L | M | N | $\bigcirc$ | P | Q | R | S | T | U | V | W | X |
| Z | $z$ | A | B | C | D | E | F | G | H | I | J | K | L | M | H | 0 | P | Q | R | S | T | U | V | W | X | $Y$ |

## Let's play a game of hiding the message using Polyalphabetic Cipher

We are discovered save yourself

## deceptive



| key | 3 | 4 | 2 | 4 | 15 | 19 | 8 | 21 | 4 | 3 | 4 | 2 | 4 | 15 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| plaintext | 22 | 4 | 0 | 17 | 4 | 3 | 8 | 18 | 2 | 14 | 21 | 4 | 17 | 4 |
| ciphertext | 25 | 8 | 2 | 21 | 19 | 22 | 16 | 13 | 6 | 17 | 25 | 6 | 21 | 19 |


| key | 19 | 8 | 21 | 4 | 3 | 4 | 2 | 4 | 15 | 19 | 8 | 21 | 4 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| plaintext | 3 | 18 | 0 | 21 | 4 | 24 | 14 | 20 | 17 | 18 | 4 | 11 | 5 |
| ciphertext | 22 | 0 | 21 | 25 | 7 | 2 | 16 | 24 | 6 | 11 | 12 | 6 | 9 |

## One Time Pad

- Each new message - requires new key of same length
- Unbreakable
- No relationship to plain Text



## Let's play a game of hiding the message using One Time Pad

## Mr Mustard with the candlestick in the hall



## Assessment

## Compute the Ciphertext using Playfair Cipher

Perform Encryption and decryption using Hill Cipher for the following Message PEN and Key: ACTIVATED

## REFERENCES

1. William Stallings, Cryptography and Network Security, 6 th Edition, Pearson Education, March 2013.

## THANK YOU


[^0]:    Polygram Substitution

