

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution) Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Legendre's Linear Differential Equation

$$+\cdots + a_{n-1}(ax+b)\frac{dy}{dx} + a_n y = a(x) \rightarrow 0$$

Take
$$ax+b=e^{\frac{\pi}{2}}$$

$$\frac{\pi}{2} = \log (ax+b).$$

$$\frac{(ax+b)}{2} = ab'$$

$$\frac{(ax+b)^2}{2} = a^2 b' (b'-1)$$

$$\frac{(ax+b)^3}{2} = a^3 b' (b'-1) (b'-2)$$
and so on.

$$(2x+3)^{2}y'' - (2x+3)y' + 2y = 6x$$

(1)
$$\Rightarrow [4D'(D'-1) - 2D' + 2]y = 6[\frac{e^{x} - 3}{2}]$$

$$[4D'^{2} + D' - 2D' + 2]y = 3[e^{x} - 3]$$

$$[4D'^{2} 6D' + 2]y = 3e^{x} - 9 \text{ which is a linear equivariant}$$

2). Solve $(x+2)^3 \frac{d^2y}{dx^2} - (x+2) \frac{dy}{dx} + y = 3x + 4$

coeffectents.



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Soln.

Given
$$[(2H2)^2D^2 - (3(+2)D+1]y = 3x+4 \rightarrow (1)$$

Fake $x+2=e^{x} \Rightarrow x=e^{x}-2$
 $x = \log (x+2)$
 $(x+2)D = D^1$
 $(x+2)^2D^2 = D^1(D^1)$
 $(1) \Rightarrow [D^1(D^1-1) - D^1+1]y = 3e^{x}-6+4$
 $[D^1-D^1-D^1+1]y = 3e^{x}-2$
 $(m-1)(m-1) = 0$
 $(m-1)(m-1)$