

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)
Coimbatore-641035.

UNIT-II ORDINARY DIFFERENTIAL EQUATIONS

Cauchy's Linear Differential Equation

J. Solve
$$x^2y'' + 2xyy' = 0$$

Solve $(x^2 D^2 + 2xy)y = 0 \longrightarrow (1)$

Take $x = e^x$
 $x = log x$
 $x D = D'$
 $x^2 D^2 = D'(D' - 1) = D'^2 - D'$

Subs. the above $9n(1)$,

 $[D^2 - D' + 2D]y = 0$
 $[D^2 + D]y = 0$
 $[D^2 + D^2 + D^2]y = 0$
 $[D^2$

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Cauchy's Linear Differential Equation

$$CF = (A+BZ)e^{2X}$$

$$CF = [A+B\log x]x^{2}$$

$$PI = \frac{1}{b^{2}-AD^{2}+4} e^{X} S^{2}n X$$

$$= e^{X} \frac{1}{(D^{2}+1)^{2}-A(D^{2}+1)+4} S^{2}n X D^{2} + D^{2}+4$$

$$= e^{X} \frac{1}{D^{2}+1+2D^{2}-AD^{2}-A+4} S^{2}n X$$

$$= e^{X} \frac{1}{D^{2}-2D^{2}+1} S^{2}n X$$

$$= e^{X} \frac{1}{-1-2D^{2}+1} S^{2}n X$$

$$= e^{X} \frac{1}{-2D^{2}} S^{2}n X$$

$$= e^{X} \frac{1}{-2$$