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Coimbatore – 35

DEPARTMENT OF MATHEMATICS UNIT – IV TESTING OF HYPOTHESIS

CHI - SQUARE TEST : $\chi^2 = \frac{\mathcal{Z}\left[0_i - E_i\right]^2}{E_i}$ where Oi -> Observed Jugarney Ei -> Emperimental frequency of Enpected frequence peques & freedom, v=n-1 properties : 1) The mean of X2 dist. is equal to the no. of clayees of freedom ii) The variance of 2° dist. is twice The degrees of preedom in 2 22 is a chi-equare variate with 2 degrees 3 freedom, theo 27/2 is a yanna variate with parameter 2/2. i) standard go variate tends to standard normal variate asnad 1) TO test of the hypothetical value of the population variance Applications ? la 52 = 50 2 11) 10 Test the yoodness of fit attributes in to lest the homogeniety of indep. estimates & the population variance Deques 5 freedom: NO. 3 values to a set which may be aniqued arbitractly.





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) The table below gives the number of aircraft accidents that occurred during the various days of the week test whether the accidents are uniformly distributed over the week. pays : Mon Tues Weel Thurs Fee sat No. q accidente: 14 18 12 11 15 14 Ssin: regiven, total no q accidente = 84 No. q days = 6 : Expected frequencies of the accidents = 84 $0^{\circ}_{i} \in (0^{\circ}_{i} - E^{\circ}_{i})^{2} (0^{\circ}_{i} - E^{\circ}_{i})^{2}$ 14 14 0 0/14 :0 $\frac{\mathcal{Z}\left(0i-E_{i}\right)^{2}}{E_{i}^{2}}=\frac{2.14285}{2.14285}$ Step1: Hoemilate Ho & H, : Ho: The accidents are uniformly distributed. H1: The accidents are not uniformly distributed. step 2 : Los at x = 5%. step 3 : Test statistic, $\chi^2 = \mathcal{Z}(\underline{q_1}-\underline{c_1})^2 = 2.1428$ 19MAT204 – PROBABILITY & STATISTICS S.SINDHUJA/AP/MATHS/SNSCT PAGE -2 OF 8





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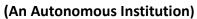
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step 4: Degrees & freedom, v = n-1 = 6-1 =5 Tab value is 11:04 = Xx Step 5: Conclusion: $\chi^2 = 2.428 < 11.04 = \chi^2_{\alpha}$. Ho is accepted at 5% los any the accident. are uniformly distributed. 2) A clie was thrown 498 times. Denoting n to be the number appearing on the top face of it, The obierved frequency of n is ywen below: n: 1 2 3 4 5 6 7: 69 78 85 82 86 98 what opinion you would form for the accuracy of The Soln: Criven, Expected frequency, E:= Total frequence = 4 98 = 83

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Gn	Ø;	G i (Oi	-E)2	(O2-E1)/E:
1	69	83	196	2.3614
2	78	83	25	0.3012
3	85	83	4	0.0481
4	82	83	- 1	0.0120
5	86	83	9	0-1084
6	98	83	225	2.4108
154			£ (0	$(-\epsilon_i)^2 = \frac{5 \cdot 5419}{1}$

step1: formulate Ho & H .:

Ho: A sie is unbranch H, : A sie is not unbiased is biased. step 2: Los at x = 5%. sty 3: Test statistic, $\chi^2 = \frac{\mathcal{E}(0i - E_i)^2}{E_i} = 5.542$. step 4 : Degrees g -freedom, v=n-1 =6-1 · · X2 = 11.04. stip 5: Conclusion; $\chi^2 = 5.542 \times 11.04 = \chi^2_{\chi}$. Ho is accepted at 5.1. Los as A die is unliand





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CHI SQUARE TEST JOR INDEPENDENCE of ATTRIBUTES.
X² = ∑[(0i-Ei)²] E[= [(0i-Ei)²] where Oi → Observed Juquency Ei → Expected Juquency Ei = (2000 bital)(culumn total) Ei = (2000 bital)(culumn total) Ei = (2000 bital)(culumn total) Aj whole total j=1 tot J=1 tot
One the basis g information noted below, find out whether the new treatment & comparatively superior

	Favourable	Not Favourable	Total
New	60	30	90
Conventional	40	70	110
n: total	100	100 -	200

	90 × 100	90× 100	a)	
	200 : 45	200 : 45		
(andreas)	10 × 100 200 : 55	110 × 100 : 55		





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Qt Ei Qi-Ei (Oi-Ei)/Ei 45 15 5 60 30 45 -15 5 40 55 -15 4.09 EL 18.18 step1: Formulating Ho & H ,: Ho: There is no difference believen new & conventioned treatment. Hi There is difference chetween mero & conventional treatment. step 2 · Los al a= 5.1. slep 3. Test statistics, $\chi^2 = \frac{\xi(0i - E_i)^2}{E_i}$ = 18.18 step 4: Degrees of Freedom, N = ((3-1) + (t-1)) V= (2-1 + 2-1) = 141 . . . tab value, Xx = 3.841 top 5 : Conclusion: X= 18.18>3.841= Xa 13 . Ho is rejected at 5 . 1. 205 a, there is difference between new & convertinial

treatment.





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2) Two research while rating techniques add Researchers: A	the stude opted by Below 40	them are avg. An 3.	. Can you xeey Aighificant rg. Above Avg. 3 25 25 0 44	2 100 10 200	
-to-tal	126	93	69	12 300	
Jo file			an a		
			31 109×69:23		
			62 <u>200x 69</u> :46 300	300 300 B	
Oi	Eĩ	Oc -Ei	(0:-Ei)/E:		
40	42	-2	0.0952		
33	31	2	0.129		
25	23	2	0.173		
2	4	-2	- 1		
86	84	2	0-04¥		
60	62	- २	0.064		
44	46	- 2	0.086		
10	8	2	0.5	and the second s	
		2 (Oi-	50)2 2 094		
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Step 1: Formulating Ho and H:: Ho: Finere & no difference Aretwaen the two rerearchers H: Three & difference Introven the two rerearchers (Step 2: Los at $\alpha = 5 \cdot /.$ Step 3: Test statuties, $\chi^2 = \frac{\sum (0! - \epsilon_i)^2}{E_i}$ = 2.097.Step 4: Degrees of freedom, v = ((4-1) * (2-1)) = (3 * 1)= 3

i Tab value is $\mathcal{R}^2_{\alpha} = 4.115$ glip 5: Conclusion. $\mathcal{X}^2 = 2.094 < 1.115 = \mathcal{X}^2_{\alpha}$ i Ho is accepted at 5.1. Los (a) Thue is no difference between The two screatchers, (a) Thue is no difference between The two screatchers,

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