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#### **DEPARTMENT OF MATHEMATICS** UNIT – IV TESTING OF HYPOTHESIS

JEST OF SIGNIFICANCE OF LARGE SAMPLES; JEST JOR SINGLE MENN: Null Hypothesis, 110 : H= Ho Test statistics,  $z = \frac{\pi - \mu}{\sigma / v_n}$  (or)  $z = \frac{\pi - \mu}{s / v_n}$ 1) A sample of goo members is found to have a mean of 3.4 cm and s.D. 2.61 cms. Is the sample from a large population of mean 3.25 cm and 8.0. 2.61 cms. by the population & normal and its mean is untender find the 95% confidential (geducial) limits of true mean. Given: n= 900, n= 3.4, µ= 3.25, 0=2.61 Slepis Formulating Ho & H1: H6: H= 3.25 H1: H\$ 3.25 (two failed lest) Step 2: Level of rightficance = 5% = 0.05 slep 3 : Test statistic, z = 2-14 = 3.4 - 3.25 2.61 V900 =1.724 step 4: critical value at 5% is Za=1.96. steps: conclusion: since 121=1.724 < 1.96= 24, Ho & accepted at 5%. Level & significance. . The sample & taken from population where mean 3.25 cm.

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2) A random sample a 200 employees at a large corporation schowed theis average to be 42.8 years with a s.D.g 6.89 years. Test The hypotheses Ho: H= 40, HI: H>40 at a = 0.01 level & significant Sofn: given: n= 200, n= 42.8, H=40, J=689 step 1: Formulating Ho and H, : Ho: M= 40 H1: H>40 (one fail test - right) steps : Level of significance, x= 0.01. steps: Test statistic, Z = 51-H = 42.8 - 40 = 5.747 step 4: Critical value at 1.1. (one tailed - sight) \$ Z = 2.33 step 5: Conclusion: mace 121=5.444 > 2.33=2. : Ho & rejected at 1% Level 9 significance . The hypothenes, M, : H>40 is accepted.

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3) The mean height of college students in a city are normally distributed with 3.2.6 cms. A sample of 100 students has mean height of 158 cms. Test the hypothesis that the mean height of college students In the city the cone. Also obtain 99%. confidence limits for the true mean. Asto: Given: n= 100, 7 = 158, H= 160, J=6 step 1: Formulating Ho and HI, : Ho: H= 160 HI: H # 160 (two tailed test) steps : Level of significance, a =1/ slep 3 : Test statistec, Z = A-H = 158 - 160 6/100 = 3.33 Step 4: ceitical value at 1%. (two side test) is 20 = 2.58. steps: conductor; Sunce 121= 3.33 > 2.58 = 22 . Ho is sejected at 1% level of significance. . . The mean height of the college students in the city is 160 cms is not true.

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JEST JOR DIFFERENCE JOR TWO MEANS: Null thypothesis: Ho:  $H_1 = H_2$ test statistic,  $z = \frac{\overline{x_1} - \overline{x_2}}{\sqrt{\frac{\overline{x_1} + \overline{x_2}}{\overline{n_1} + \frac{\overline{n_2}}{\overline{n_2}}}}$   $\overline{v_1} = \overline{v_2} = \overline{v}$   $= \frac{\overline{n_1} - \overline{n_2}}{\overline{v_1} + \frac{\overline{n_2}}{\overline{n_2}}}$ (or)  $z = \frac{\overline{n_1} - \overline{n_2}}{\sqrt{\frac{\overline{n_1} + \frac{\overline{n_2}}{\overline{n_2}}}}$ . Whe means q two thingle large samples q locc or d: Ro oo members are  $b_T = s$  inches and  $b_S$  inches Resp. Can the samples be Regarded as drawn from the Can the samples be Regarded as drawn from the Same population q standard deviation q ses inches. Test at  $s \cdot J$ , level of Significance (Los)

Soln: -given:  $n_1 = 1000$ ,  $\overline{n_1} = 67.5$ ,  $n_2 = 2000$ ,  $\overline{n_2} = 68$ ,  $\vartheta = -\varphi.5$ 

step 1: Formulating Ho and H1: Ho: H. = H2 H1: H. # H2 (two tailed test) Step 2: Level 2 significance, a = 5% = 0.05

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Slép 3: Test statistie,  $z = \frac{\pi_1 - \pi_2}{\sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$ =  $\frac{67 \cdot 5 - 68}{2 \cdot 5\sqrt{\frac{1}{1000} + \frac{1}{2000}}}$ = -5.164  $1z_1 = 1 - 5.1641$ = 5.164Step 4: artical value, at 5%. Chuo anded tast)  $is \ z_{x} = 1.96$ . Step 5: conclusion;  $z = 5.164 > 1.96 = z_{x}$ . Ho is Agrictidat 5%. Los. . The samples cannot be regarded as deawn from The same population of g 3.D. 25 inches.

MA rimple sample q height q 6400 sailors has a mean q 67.85 inches and s.D. g 2.56 Inches while a simple sample q heights q 1600 sotoliers has a mean q 68.55 Inches and s.D. g 2.50 inches. Do The data, indicate that sotoliers are on the average talles than sailors? use 51. Los.

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<u>Soln:</u> Given: Spilors: n, = 6400, x,=67.85, 8,=2.56 Soldier: no = 1600, no= 68.55, So= 2.52 Step 1: Formulating Ho and H, Ho: HI = H2. H1: M1 < H2 Cone tailed test- Left) Step 2 : Los at 5 1. as x=0.05 step 3: Test statistic, Z = X1- X2  $\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}$ = 67.85-68-55 (2.56)2 + (2.52)2 6400 + (2.52)2 = -9.91 121=1-9.91) = 9.91 step 4: critical value at 5% (one tail tait) is xy = 1.645 step 5: Conclusion: z=9.91>1.645=zx . Ho is rejected at 5% g Los ... The data indicates that soldiers are on the average faller than sailors.

\* A somple sample of heights of 6400 English men thas a mean of 170 cm & s.D. of 64 cm, while a simple sample of theights of 1600 Americans that a mean of 172 cm & s.D. of 6.3 cm. No the data indicate that Americans are the arg. talks than the coolish men 2 [z = 11.32, H, < M. Americans are talke than English men]

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