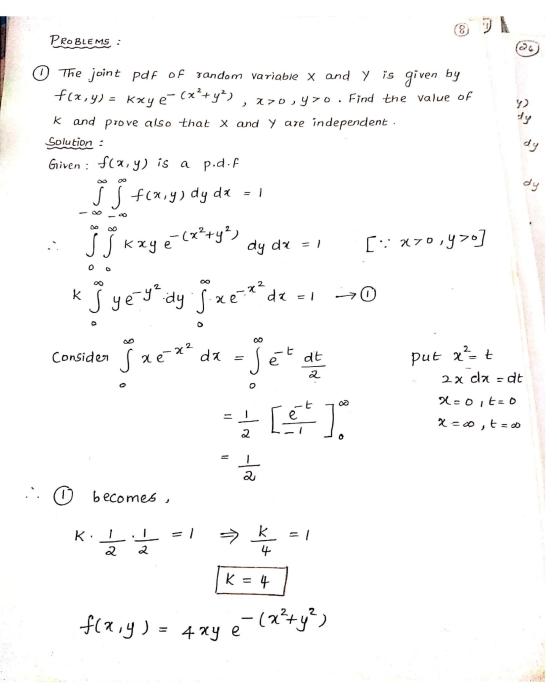


SNS COLLEGE OF TECHNOLOGY





DEPARTMENT OF MATHEMATICS



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To prove x and y are independent :

$$f(x) \cdot f(y) = f(x,y)$$
Now, $f(x) = f_x(x) = \int_{-\infty}^{\infty} f(x,y) dy$

$$= \int_{-\infty}^{\infty} + xy e^{-(x^2+y^2)} dy$$

$$= + x e^{-x^2} \int_{y}^{\infty} y e^{-y^2} dy$$

$$= + x e^{-x^2} \cdot \frac{1}{a}$$

$$f(x) = ax e^{-x^2}$$

$$f(x) = ax e^{-x^2}$$

$$f(x) = ay e^{-y^2}$$

$$\therefore f(x) \cdot f(y) = (2x e^{-x^2})(2y e^{-y^2})$$

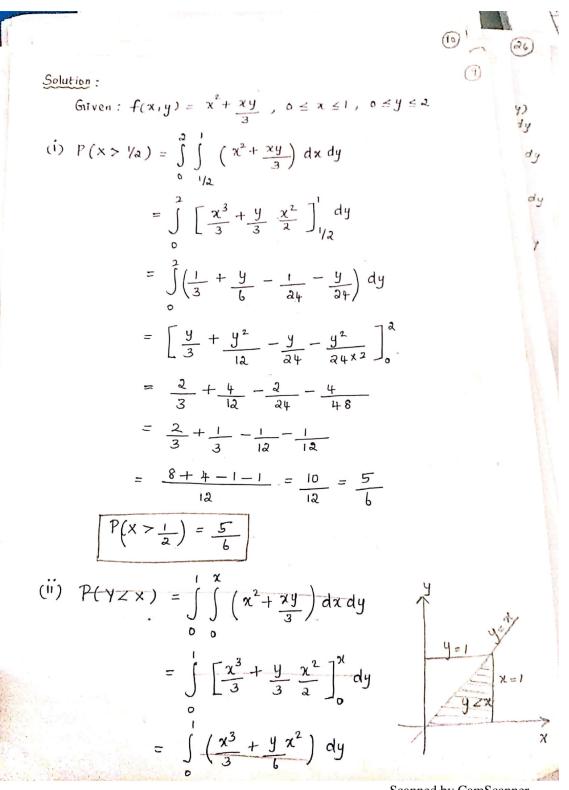
$$= 4x y e^{-(x^2+y^2)}$$

$$\boxed{f(x) f(y)} = f(x,y)$$

$$\therefore x \& y \text{ are independent}$$

$$\boxed{a} \quad If \text{ the joint pdf of a random Variable (X, Y) is given by, } f(x,y) = \begin{cases} x^2 + \frac{xy}{3} ; 0 \le x \le 1, 0 \le y \le a \\ 0 ; 0 \text{ therwise} \end{cases}$$
Find (i) $P(x > 1/a)$ (ii) $P(Y \le 1/a)(x) = f(x - 1/a)$
(iv) check whether the conditional densities of X on Y and Y on X are Valid.

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$$P(\frac{4}{2} \times \frac{1}{2} = \int_{-\frac{\pi^{3}}{2}}^{\frac{\pi^{3}}{2}} + \frac{\pi^{4}}{2} + \frac{y^{2}}{2} \int_{0}^{1}$$

$$= \frac{\pi^{3}}{3} + \frac{\pi^{3}}{12}$$

$$P(\frac{4}{2} \times 1) = \int_{0}^{1} \int_{0}^{\pi} (\pi^{2} + \frac{\pi^{3}}{3}) dy dx$$

$$= \int_{0}^{1} \left[\pi^{2} y + \frac{\pi}{3} + \frac{y^{2}}{3} \right]_{0}^{\pi} dx$$

$$= \int_{0}^{1} \left[\pi^{3} + \frac{\pi^{3}}{24} \right]_{0}^{1} = \frac{1}{4} + \frac{1}{44} = \frac{6 + 1}{24}$$

$$P(\frac{4}{2} \times 1) = \frac{7}{44}$$

$$P(\frac{4}{2} \times 1) = \frac{1}{4} + \frac{1}{44} = \frac{6 + 1}{24}$$

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