

## SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution)

#### **DEPARTMENT OF MATHEMATICS**

Total probability theorem :

If  $B_1, B_2, \dots B_n$  are mutually exclusive and exhaustive set of events of a Sample Space S and A be any event associated with the events  $B_1, B_2, \dots B_n$ . Then

 $P(A) = \sum_{i=1}^{n} P(B_i) P(A|B_i)$ 

If  $B_1, B_2, \cdots B_n$  are mutually exclusive and exhaustive events of a Sample Space S and A be any event associated with the events  $B_1, B_2, \cdots B_n$ . Then

$$P(Bi|A) = \frac{P(Bi) P(A|Bi)}{\sum_{i=1}^{n} P(B_i) P(A|B_i)}$$

Problems :

The content of bags I, I and I are as follows:
 (a) I white, 2 black, 3 red balls
 (b) 2 white, 1 black, 1 red balls
 (c) 4 white, 5 black, 3 red balls
 One bag is Chosen at random and two balls are drawn.
 They happen to be white and red balls. What is the Probability that they come from bag I, I and I ?

There are 3 bags. The probability of choosing One bag is 1/3.

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(c)  
Let B, be the event of choosing bag T  
Let B<sub>2</sub> be the event of choosing bag TT.  
Let B<sub>3</sub> be the event of choosing bag TT.  
i.e., P(B<sub>1</sub>) = 1/3, P(B<sub>2</sub>) = 1/3, P(B<sub>3</sub>) = 1/3.  
A be the event of getting 1 white ball and 1  
red ball. Then,  
P(A/B<sub>1</sub>) = 
$$\frac{1C_1 \times 3C_1}{6C_2} = 1/5$$
  
P(A/B<sub>2</sub>) =  $\frac{2C_1 \times 1C_1}{4C_2} = 1/5$   
P(A/B<sub>3</sub>) =  $\frac{4C_1 \times 3C_1}{12C_2} = 2/11$   
By Bage's theorem,  
P(B<sub>1</sub>|A) =  $\frac{P(B_1) P(A|B_1)}{\frac{5}{1}=1}$   
P(B<sub>1</sub>|A) =  $\frac{1}{3} \times \frac{1}{5} + \frac{1}{3} \times \frac{1}{3} + \frac{1}{3} \times \frac{1}{3} + \frac{1}{3} \times \frac{1}{5} + \frac{1}{3} \times \frac{1}{3} + \frac{1}{3} \times \frac{1}$ 

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(\*) In a bolt factory machines 
$$A \, B$$
 and  $C$  manufacture  
respectively  $25 \, A \, 35 \, A \, 40 \, A$  of the total of their  
output  $5 \, A \, 40 \, A \, 10 \, C$  are defective bolts.  $A$  bolt is  
drawn at random from the product and is found to  
defective. What are probabilities that it was  
manufactured by machine  $A, B, C$ ?  
Solution:  
Let  $B_1$  be the event that a bolt is  
manufactured by machine  $A \, B_2$  be the event that a  
bolt is manufactured by machine  $B \, B_3$  be the event  
that a bolt is manufactured by machine  $C$ .  
Let  $A$  be the event that a bolt is defective.  
 $P(B_1) = 0.25 \, P(A|B_1) = 0.05$   
 $P(B_2) = 0.40 \, P(A|B_3) = 0.02$   
By Baye's theorem,  
 $P(B_1|A) = \frac{P(B_1) P(A|B_1)}{\sum_{i=1}} P(B_i) P(A|B_i)$   
 $P(B_1|A) = \frac{P(B_1) P(A|B_1)}{P(B_1) P(A|B_1) + P(B_2) P(A|B_2) + P(B_3) P(A|B_3) = 0.02$   
 $P(B_1|A) = \frac{P(B_1) P(A|B_1)}{P(B_1) P(A|B_1) + P(B_2) P(A|B_2) + P(B_3) P(A|B_3) = 0.02$   
 $P(B_1|A) = \frac{P(B_1) P(A|B_1)}{P(B_1) P(A|B_1) + P(B_2) P(A|B_2) + P(B_3) P(A|B_3) = 0.02$   
 $P(B_1|A) = \frac{P(B_1) P(A|B_1)}{P(B_1) P(A|B_1) + P(B_2) P(A|B_2) + P(B_3) P(A|B_3) = 0.02$   
 $P(B_1|A) = \frac{P(B_1) P(A|B_1)}{P(B_1) P(A|B_1) + P(B_2) P(A|B_2) + P(B_3) P(A|B_3) = 0.02$   
 $P(B_1|A) = 0.35 \times 0.05 + 0.35 \times 0.04 + 0.4 \times 0.02$ 

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$$P(B_{2}|A) = \frac{P(B_{2}) \cdot P(A|B_{2})}{P(B_{1})P(A|B_{1}) + P(B_{2})P(A|B_{2}) + P(B_{3})P(A|B_{2})}$$

$$= \frac{0.35 \times 0.04}{0.25 \times 0.05 + 0.35 \times 0.04 + 0.4 \times 0.02}$$

$$P(B_{2}|A) = \frac{0.4057}{P(B_{3})P(A|B_{3})}$$

$$P(B_{3}|A) = \frac{P(B_{3}) \cdot P(A|B_{3})}{P(B_{1})P(A|B_{1}) + P(B_{2})P(A|B_{2}) + P(B_{3})P(A|B_{3})}$$

$$= \frac{0.40 \times 0.02}{0.25 \times 0.05 + 0.35 \times 0.04 + 0.4 \times 0.02}$$

$$P(B_{3}|A) = 0.2318$$

Solution:  
Let 
$$B_1$$
,  $B_2$  &  $B_3$  be the event of selecting  
A, B and C as manager of a Company.

$$P(B_1) = \frac{3}{12} = \frac{1}{4}$$

$$P(B_2) = \frac{5}{12} = \frac{5}{12}$$

$$P(B_3) = \frac{4}{12} = \frac{1}{3}$$

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Let A be the event of introducing special bonus scheme.  $P(A|B_1) = 0.6$  $P(A|B_2) = 0.4$  $P(A|B_3) = 0.5$ By Baye's theorem,  $P(B_2|A) = P(A|B_2).P(B_2)$  $P(A|B_1) P(B_1) + P(A|B_2) P(B_2) + P(A|B_3) P(B_3)$ = (0.4) (5/12) (0.6) (1/4) + (0.4) (5/12) + (0.5) (1/3) = 0.1667 = 0.3449 = 34.49.7. 0.4833(4) A company has two plants . Plant I manufactures 25% of the items. Plant I manufactures 75% of the items. 3.1. and 5.1. of the items manufactured by plant I and I respectively are known to be defective. What is the Chance that it was generated by Plant I. Solution : Let B, & B2 be the event manufactured by Plant I and I respectively. P(B,) = 25 1/ = 0,25 P(B2) = 75 1. = 0.75 Let A be the event that the item is defective.  $P(A | B_1) = 3! = 0.03$ P(A/B2) = 5 1/ = 0.05 Scanned by CamScanner