

Merge sort :-

- Merge sort is a sorting algorithm that uses divide and conquer strategy
- Merge sort an input array with n elements consists of 3 steps.

① Divide

partition array into two sub-lists S_1 & S_2 with ' $n/2$ ' elements each.

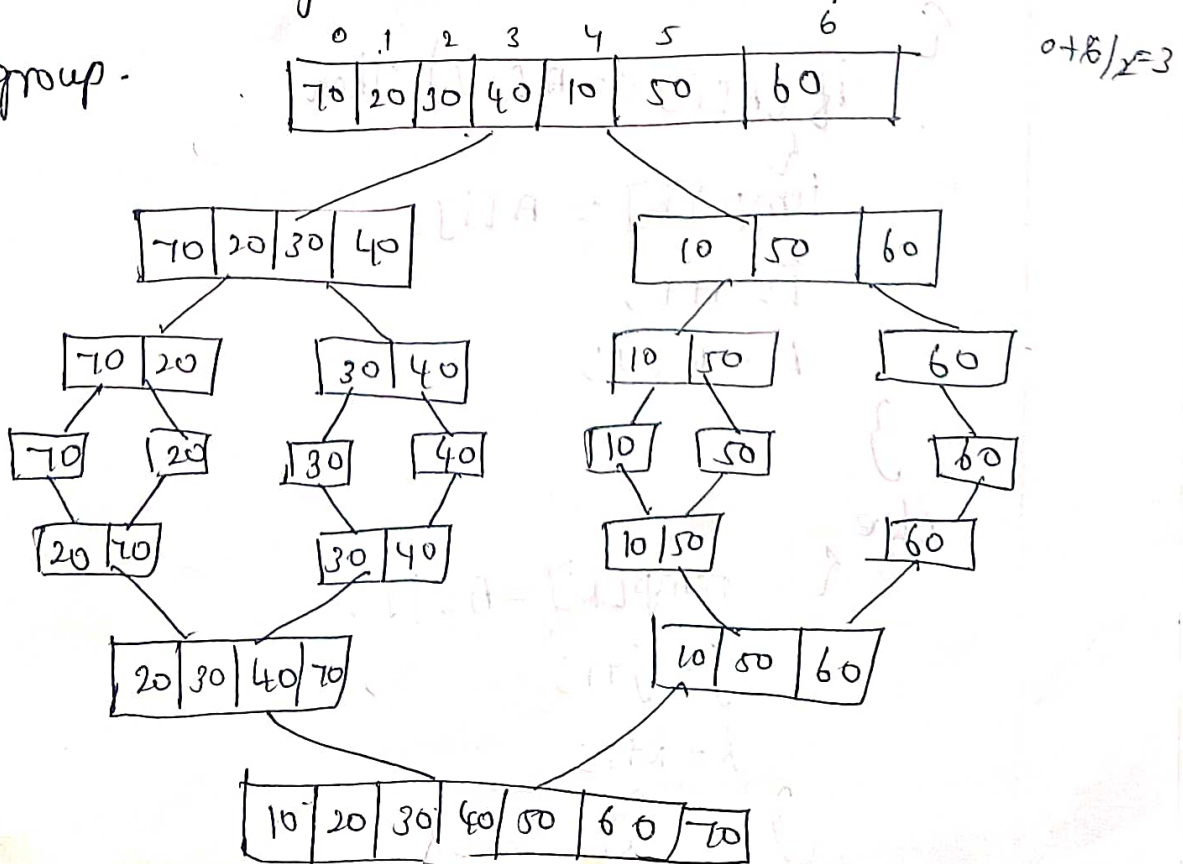
② Conquer :-

sort sublists S_1 & S_2

③ Combine :-

Merge S_1 & S_2 into unique sorted

group.



Algorithm mergesort (int A[0..n-1], low, high)

```
{  
  if (low < high) then  
  {  
    mid ← (low+high)/2;  
    mergesort (A, low, mid);  
    mergesort (A, mid+1, high);  
    combine (A, low, mid, high);  
  }  
}
```

Algorithm combine (A[0..n-1], low, mid, high)

```
{  
  k = low;  
  i = low;  
  j = mid+1;
```

while (i ≤ mid & j ≤ high)

```
{  
  if (A[i] ≤ A[j]) then
```

```
  {  
    temp[k] = A[i];
```

```
    i = i+1;
```

```
    k = k+1;
```

```
  }  
  else
```

```
  {  
    temp[k] = A[j];
```

```
    j = j+1;
```

```
    k = k+1;
```

```
  }  
}
```

while (i <= mid) do

{

temp [k] = A [i];

i = i + 1;

k = k + 1;

}

while (j <= high) do

{

temp [k] = A [j];

j = j + 1;

k = k + 1;

}

Complexity Analysis of Merge Sort

* Best case $O(n \log n)$

* worst case $O(n \log n)$

* Average case $O(n \log n)$

0 1 2 3 4 5 6

70 20 30 40 10 50 60

① low = 0 high = 6

low < high ok

mid = $(0+6) / 2$

mid = $6 / 2 = 3$

mid = 3

mergesort (A, 0, 3)

mergesort (A, 3+1, 6)

Combine (A, low, mid, high)

Mergesort (A, 0, 3)

mid = $(0+3)/2 = 1.5 = 1$

Mergesort (A, 0, 1)

Mergesort (A, 2, 3)

Mergesort (A, 0, 1)

mid = $(0+1)/2 = 0.5$

Mergesort (A, 0, 0)

Mergesort (A, 1, 1)

Mergesort (A, 0, 0)

low = 0 high = 0 mid = 0

k = 0

i = 0

j = 0 + 1 = 1

while (0 <= 0 & 1 <= 0)

A[0] <= A[1]

temp[0] = A[1]

20	
0	