



(An Autonomous Institution)
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DEPARTMENT OF MATHEMATICS

UNIT - IV FUNCTIONS OF SEVERAL VARIABLES

METHOD OF LAGRANGIAN'S MULTIPLIERS

We can find an extreme value of the function f(x,y,3) subject to the constrained y(x,y,3)=0

Define $F(x,y,z) = \int (x,y,z) + \lambda g(x,y,z)$ where λ is an undetermined constant called the Lagrangian multipliers.

By solving the egn.

 $\frac{\partial F}{\partial x} = 0$, $\frac{\partial F}{\partial y} = 0$, $\frac{\partial F}{\partial z} = 0$, we get the Values of x, y, z and y. Tusing x value find x, y, z, find the Values either maximum or minimum by substituting x, y, z in f(x, y, z).

Tind the minimum value of n2+ y2+ z2, exiven that an + by+ Cz = P

Let $J = n^2 + y^2 + z^2$ and g = an + by + cz - p F(n,y,z) = J(n,y,z) + Jg(n,y,z) $= n^2 + y^2 + z^2 + J[an + by + cz - p]$





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$$\frac{\partial f}{\partial x} = 2x + \alpha \lambda$$

$$\Rightarrow \frac{\partial F}{\partial x} = 0 \Rightarrow 2x + \alpha \lambda = 0$$

$$\Rightarrow x = -\frac{\lambda \alpha}{2}$$

$$\frac{\partial F}{\partial y} = 2y + b\lambda$$

$$\Rightarrow \frac{\partial F}{\partial y} = 0 \Rightarrow 2y + b\lambda = 0$$

$$\Rightarrow y = -\frac{\lambda b}{2}$$

$$\frac{\partial F}{\partial x} = 0 \Rightarrow 2x + c\lambda = 0$$

$$\Rightarrow \frac{\partial F}{\partial x} = 0 \Rightarrow 2x + c\lambda = 0$$

$$\Rightarrow 3 = -\lambda c$$

$$\frac{\partial F}{\partial \lambda} = \alpha x + b y + c z - P$$
=) $\frac{\partial F}{\partial \lambda} = 0$ =) $\alpha x + b y + c z = P$
=) $\alpha x - \lambda_2^{\alpha} + b x - \lambda_2^{\alpha} + c x - \lambda_2^{\alpha} = P$
=) $-\frac{\lambda}{2} \int a^2 + b^2 + c^2 \int = P$
=) $\lambda = -\frac{2P}{a^2 + b^2 + c^2}$





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3) A sectangular bon open at the top is to have a volume of 32 cc. Final the climension of the box, that dequire the least material for its construction. Let the climension of the bon be 21,4,3 Volume = xyz. Surface are = xy+293+23x surface = eb+2/10. eliven volume = 32 cc $\Rightarrow xy3=32$ (a) xy3-32=0· · 9 = xy3-32 & 7 = ny + 243 + 23 n. : F(n,y,3)= ny+243+ 23x+ 7/my 3-327 OF = y+23+743 => y+23+743=0 [: OF=0] 3.F = x + 23 + 123 3F = 0 = > 21+2 7 22 = 0 - 0 OF = 29+23+724 # $\frac{\partial F}{\partial \beta} = 0 \implies \partial y + \partial \hat{\beta} + \partial ny = 0 \quad --- \quad \boxed{3}$





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Sub
$$n = y = 23$$
 in (2)
 $n + 23 + 3 (n3) = 0$
 $y + 2 \frac{y}{2} + 3 \frac{y}{2} = 0$
 $\Rightarrow y = -4/3$
Sub $n = y = 23$ in (3)
 $2y + 2n + 3ny = 0$
 $2(23) + 2(23) + 3(23)(23) = 0$
 $2(23) + 2(23) + 3(23)(23) = 0$
 $2 + 43 = 0$
 $3 = -2/3$
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Find the dimensions of the rectangedous box without top of mani capacity with surface and 432 Squ. metre.

Ans: $\alpha = 4 = 23$, 12, 12, 6. $\beta = 864$ cubic metres.