

SNS College of Technology, Coimbatore-35.

(An Autonomous Institution)

Internal Assessment - I

Academic Year 2023-2024 (Odd)

Third Semester

19MAT201- TRANSFORMS AND PARTIAL DIFFERENTIAL EQUATIONS

(REGULATION 2019)

Answer Key

B

Time: 1.30 Hours

Maximum Marks: 50

		PART - A (5 x 2 = 10 MARKS) ANSWER ALL QUESTIONS	Blooms
1.		$a_0 = \frac{\pi}{2}$	(App)
2.		The process of find the Fourier series for the function given by the numerical value is known as Harmonic analysis	(Rem)
3.		$f(x) = \frac{\pi^2}{\sqrt{5}}$	(Und)
4.		$F(s) = \sqrt{\frac{2}{\pi}} \left(\frac{\sin as}{s} \right)$	(App)
5.		$\int_{-\infty}^{\infty} f(s) ^2 ds = \int_{-\infty}^{\infty} f(x) ^2 dx$	(Rem)
		PART -B (13+13+14 = 40 MARKS) ANSWER ALL QUESTIONS	
6.	a) i)	$a_0 = \frac{2}{3} l^2, a_n = \frac{4l^2}{n^2 \pi^2}, b_n = 0$	(App) (7)
	ii)	$f(x) = \frac{l^2}{3} + \frac{4l^2}{\pi^2} \sum_{n=1}^{\infty} \frac{1}{n^2} \cos \frac{n\pi x}{l}$ $b_n = \begin{cases} 0 & n \text{ is even} \\ \frac{8}{\pi n^3} & n \text{ is odd} \end{cases}$ $f(x) = \frac{8}{\pi} \left[\frac{1}{1^3} \sin \pi + \frac{1}{3^3} \sin 3\pi + \frac{1}{5^3} \sin 5\pi \right]$	(App) (6)

	b)	$f(s) = \frac{2}{\sqrt{2\pi}} \left(\frac{1 - \cos as}{s^2} \right)$ <p>Using Fourier Inverse formula sub $x=0, a=2$ set we get $\int_0^\infty \left(\frac{\sin t}{t} \right)^2 dt = \pi/2$ Apply Parseval's identity $\int_0^\infty \left(\frac{\sin t}{t} \right)^4 dt = \frac{\pi}{3}$</p>	(App) (13)
7.	a)	$a_0 = \frac{2\pi^2}{3} \quad a_n = \frac{1}{n^2} (-1)^n \quad b_n = 0$ $f(x) = \frac{\pi^2}{3} + 4 \sum_{n=1}^{\infty} \frac{(-1)^n}{n^2} \cos nx$ <p>Put $x=0 \Rightarrow \frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots = \frac{\pi^2}{6}$ Put $x=\pi \Rightarrow \frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \dots = \frac{\pi^2}{12}$ Adding above two $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}$</p>	(App) (13)
	b) i)	$b_n = \frac{8}{n^2 \pi^2} \sin\left(\frac{n\pi}{2}\right)$ $f(x) = \sum_{n=1}^{\infty} \frac{8}{n^2 \pi^2} \sin\left(\frac{n\pi}{2}\right) \sin\left(\frac{n\pi x}{2}\right)$	(App) (7)
	ii)	$b_n = \frac{-2(-1)^n}{n}$ $f(x) = \sum_{n=1}^{\infty} \frac{(-2)(-1)^n}{n} \sin nx$	(App) (6)
8.	a)	$F(s) = \frac{4}{\sqrt{2\pi}} \left[\frac{-a s \cos sa + \sin sa}{s^3} \right]$ <p>Apply Fourier Inverse Transform & deduce $\int_0^\infty \left(\frac{\sin t - t \cos t}{t^3} \right) dt = \frac{\pi}{4}$ Using Parseval's identity $\int_0^\infty \left(\frac{\sin t}{t} \right)^2 dt = \frac{\pi}{2}$</p>	(App) (14)
	b)	$a_0 = 2 \left(\frac{\sum y}{N} \right) = 2 \left(\frac{0.7}{6} \right) = 2.4 \quad b_1 = 2 \left(\frac{\sum y \sin x}{N} \right)$ $a_1 = 2 \left(\frac{\sum y \cos x}{N} \right) = 2 \left(\frac{-1.1}{6} \right) = -0.37 \quad = 2 \left(\frac{0.5796}{6} \right) = 0.17$ $b_2 = -0.06$ $f(x) = 1.45 - 0.37 \cos x - 0.1 \cos 2x + 0.17 \sin x - 0.06 \sin 2x$	(Ana) (14)