CE short circuit current gain using hybrid- π model:

Figure 4.6.1 shows the Hybrid- π model for a single transistor with a resistive load $R_{L.}$

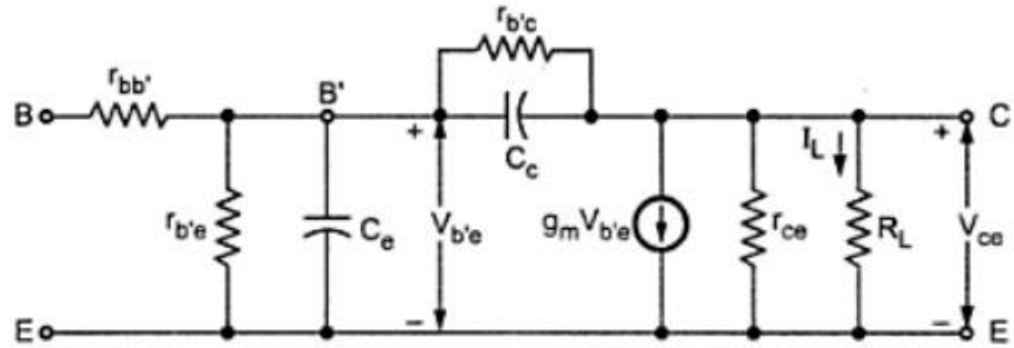

Figure 4.6.1 Hybrid- π model for a single transistor with a resistive load RL

Miller capacitance is $C_M = C_{b'c}\ (1 + g_m\ R_L)$

Here, $R_L = 0$

$\therefore \quad C_M = C_{b'c}\ (C_c)$

Parallel combination of $r_{b'e}$, and $(C_e + C_c)$ is given as

$$Z = \frac{r_{b'e} \times \dfrac{1}{j\omega(C_e + C_c)}}{r_{b'e} + \dfrac{1}{j\omega(C_e + C_c)}}$$

$$= \frac{r_{b'e}}{1 + j\omega\, r_{b'e}\,(C_e + C_c)}$$

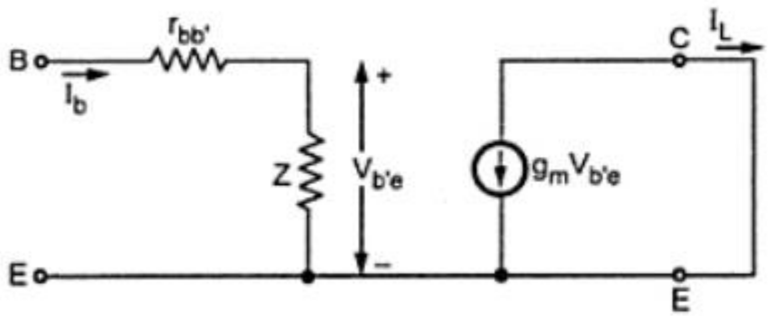

Figure 4.6.2 Simplified Hybrid pi model

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$$V_{b'e} = I_b Z$$

$$Z = V_{b'e} / I_b$$

The current gain for the circuit figure 4.6.2 is,

$$A_i = \frac{I_L}{I_b} = \frac{-g_m V_{b'e}}{I_b} \quad \because I_L = -g_m V_{b'e}$$

$$A_i = -g_m Z$$

$$= \frac{-g_m r_{b'e}}{1 + j\omega r_{b'e}(C_e + C_c)}$$

$$A_i = \frac{-h_{fe}}{1 + j\omega r_{b'e}(C_e + C_c)}$$

Figure 4.6.3 shows the Frequency Vs Current Gain

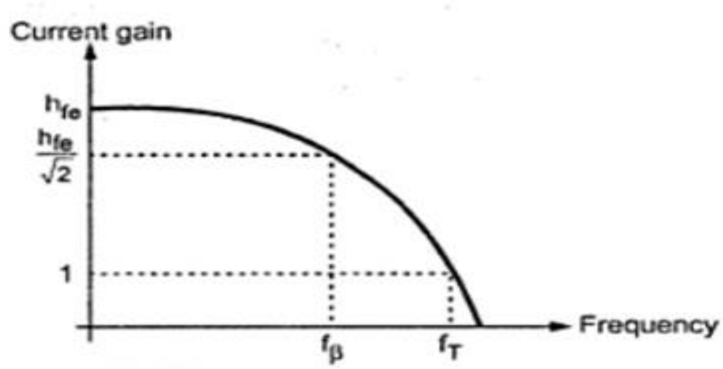

Figure 4.6.3 Frequency Vs Current Gain

$$f_\beta = \frac{1}{2\pi r_{b'e}(C_e + C_c)}$$

$$A_i = \frac{-h_{fe}}{1 + j\frac{f}{f_\beta}}$$

$$|A_i| = \frac{h_{fe}}{\sqrt{1 + \left(\frac{f}{f_\beta}\right)^2}}$$

f_β (Cutoff frequency):

It is the frequency at which the transistor short circuit CE current gain drops by 3dB or 1/√√2 times from its value at low frequency. It is given as,

$$f_\beta = \frac{1}{2\pi r_{b'e}(C_e + C_c)}$$

or

$$= \frac{g_{b'e}}{2\pi(C_e + C_c)}$$

or

$$= \frac{1}{h_{fe}} \frac{g_m}{2\pi(C_e + C_c)} \quad \because g_{b'e} = \frac{1}{r_{b'e}} = \frac{g_m}{h_{fe}}$$

f_α (Cut-off frequency):

It is the frequency at which the transistor short circuit CB current gain drops by 3dB or 1/√√2 times from its value at low frequency.

The current gain for CB configuration is given as,

$$A_i = \frac{-h_{fb}}{1 + j\frac{f}{f_\alpha}}$$

where
$$f_\alpha = \frac{1}{2\pi r_{b'e}(1+h_{fb})C_e}$$

$$= \frac{1+h_{fe}}{2\pi r_{b'e} C_e} \approx \frac{h_{fe}}{2\pi r_{b'e} C_e}$$

$$|A_i| = \frac{h_{fb}}{\sqrt{1+\left(\frac{f}{f_\alpha}\right)^2}}$$

At
$$f = f_\alpha$$

$$|A_i| = \frac{h_{fb}}{\sqrt{2}}$$

Parameter f_T:

It is the frequency at which short circuit CE current gain becomes unity.

at $f = f_T$,

$$1 = \frac{h_{fe}}{\sqrt{1+\left(\frac{f_T}{f_\beta}\right)^2}}$$

The ratio of f_T / f_β is quite large compared to 1.

$$f_T = g_m / 2\pi C_e$$

Current gain with resistive load:

$$C_{eq} = C_e + C_c\,(1 + g_m R_L)$$

For further simplification in figure 4.6.4,

At output circuit value of C_c can be calculated as,

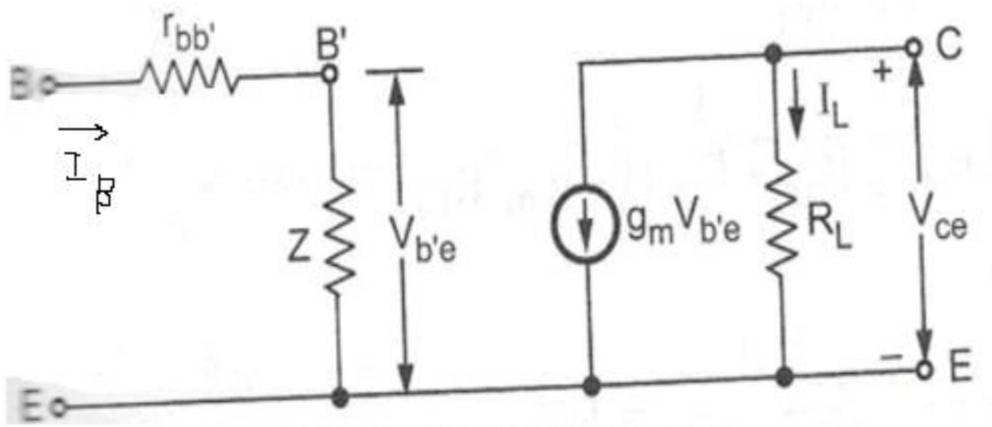

Figure 4.6.4. Simplified hybrid – π model for CE with R_L

Diagram Source Brain Kart

$$\frac{1}{\dfrac{j\omega C_c}{\dfrac{k-1}{k}}} \approx \frac{1}{j\omega C_c}$$

$$C_c\left(\frac{k}{k-1}\right) \approx C_c$$

$$Z = \frac{V_{b'e}}{I_b}$$

$$A_i = \frac{-h_{fe}}{1 + j\left(\frac{f}{f_H}\right)}$$

$$|A_i| = \frac{h_{fe}}{\sqrt{1+\left(\frac{f}{f_H}\right)^2}}$$

At $f = f_H$

$$A_i = \frac{h_{fe}}{\sqrt{2}}$$

f_H is the frequency at which the transistor gain drops by 3dB or 1/√2 times from its value at low frequency in figure 4.6.5. It is given as

$$f_H = \frac{1}{2\pi r_{b'e} C_{eq}}$$

$$= \frac{1}{2\pi r_{b'e} [C_e + C_c (1+g_m R_{L)}]}$$

At $R_L = 0$

$$f_H = \frac{1}{2\pi r_{b'e} [C_e + C_c]} = f_\beta$$

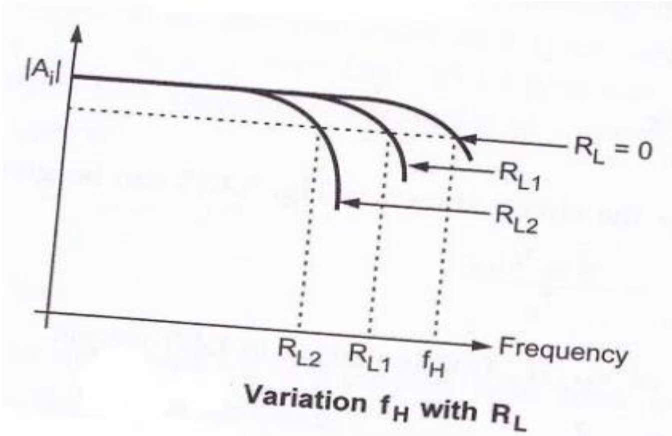

Figure 4.6.5. Variation f_H with R_L

Diagram Source Brain Kart

Current gain including source resistance:

Figure 4.6.6. shows hybrid pi Equivalent circuit with current source

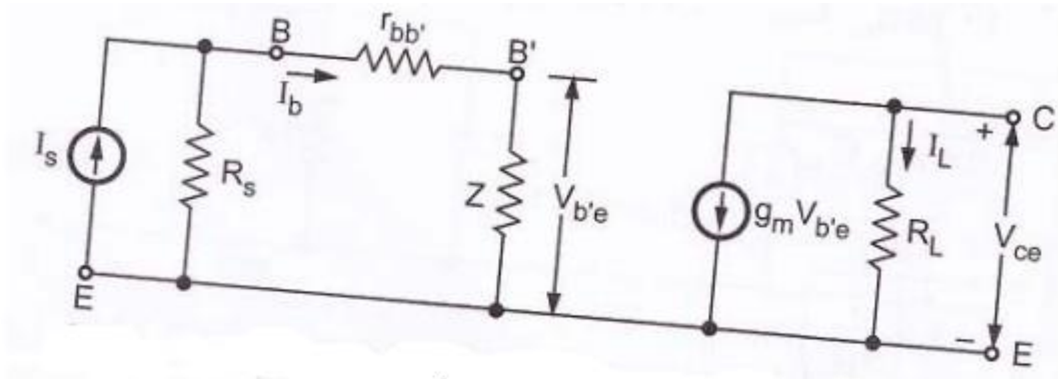

Figure 4.6.6. Equivalent circuit with current source

Diagram Source Brain Kart

$$\frac{I_L}{I_s} = \frac{-g_m \, r_{b'e} \, R_s}{R_s + r_{bb'} + r_{b'e}}$$

A_{is} at low frequency =

$$= \frac{- h_{fe} R_S}{R_s + h_{ie}}$$

Voltage gain including source resistance:

$$A_{vs} = \frac{V_o}{V_s} = \frac{I_L}{I_s}\frac{R_L}{R_s} = \frac{-g_m \, Z R_s}{R_s + r_{bb'} + Z} \times \frac{R_L}{R_s}$$

$$= \frac{-g_m \, Z R_L}{R_s + r_{bb'} + Z}$$

$$A_{vs\ low} = \frac{I_L}{I_s}\frac{R_L}{R_s} = \frac{-h_{fe} \, R_s}{R_s + h_{ie}} \times \frac{R_L}{R_s}$$

$$= \frac{-h_{fe} \, R_L}{R_s + h_{ie}}$$

Cutoff frequency including source resistance:

$$A_{is\ high} = \frac{A_{is}}{1+j\left(\frac{f}{f_H}\right)}$$

$$A_{vs\ high} = \frac{A_{vs}}{1+j\left(\frac{f}{f_H}\right)}$$

where, $$f_H = \frac{1}{2\pi R_{eq} C_{eq}}$$

where, $$R_{eq} = r_{b'e} \parallel (r_{bb'} + R_s)$$

and $$C_{eq} = C_e + C_c\,[1 + g_m R_L]$$

For $R_L = 0$,

$$f_H = \frac{1}{2\pi R(C_e + C_c)}$$

$$= \frac{f_T}{g_m R} \qquad \because\ f_T = \frac{g_m}{2\pi(C_e + C_c)}$$

$$= \frac{h_{fe}\, f_\beta}{g_m R} \qquad \because\ f_T = h_{fe}\, f_\beta$$

$$= \frac{f_\beta}{g_{b'e} R} \qquad \because\ g_{b'e} = \frac{g_m}{h_{fe}}$$

Gain Bandwidth Product:

i. Gain Bandwidth Product for Voltage:

$$|A_{vs\ low}\ f_H| = |A_{vso}\ f_H| = \frac{-h_{fe}R_L}{R_s + h_{ie}} \times \frac{1}{2\pi R_{eq} C_{eq}}$$

$$= \frac{R_L}{R_s + r_{bb'}} * \frac{f_T}{1 + 2\pi f_T C_C R_L}$$

ii. Gain Bandwidth Product for current:

$$|A_{iso} \times f_H| = \frac{g_m R_s}{2\pi C(R_s + r_{bb'})}$$

$$= \frac{f_T}{1+2\pi f_T C_c R_L} \cdot \frac{R_s}{R_s + r_{bb'}}$$