



# Artificial Intelligence

## Logical Agents

# Logical Agents

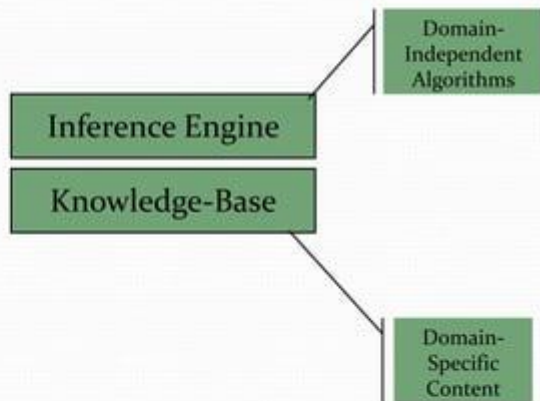
- Humans can know “things” and “reason”
  - Representation: How are the things stored?
  - Reasoning: How is the knowledge used?
    - To solve a problem...
    - To generate more knowledge...
- Knowledge and reasoning are important to artificial agents because they enable successful behaviors difficult to achieve otherwise
  - Useful in partially observable environments
- Can benefit from knowledge in very general forms, combining and recombining information

# Knowledge-Based Agents

- Central component of a Knowledge-Based Agent is a Knowledge-Base
  - A set of sentences in a formal language
    - Sentences are expressed using a knowledge representation language
- Two generic functions:
  - TELL - add new sentences (facts) to the Knowledge Base
    - “Tell it what it needs to know”
  - ASK - query what is known from the Knowledge Base
    - “Ask what to do next”

# Knowledge-Based Agents

- The agent must be able to:
  - Represent states and actions
  - Incorporate new percepts
  - Update internal representations of the world
  - Deduce hidden properties of the world
  - Deduce appropriate actions



# Knowledge-Based Agents

**function** KB-AGENT(*percept*) **returns** an *action*

**static:** *KB*, a knowledge base

*t*, a counter, initially 0, indicating time

TELL(*KB*, MAKE-PERCEPT-SENTENCE(*percept*, *t*))

*action* ← ASK(*KB*, MAKE-ACTION-QUERY(*t*))

TELL(*KB*, MAKE-ACTION-SENTENCE(*action*, *t*))

*t* ← *t* + 1

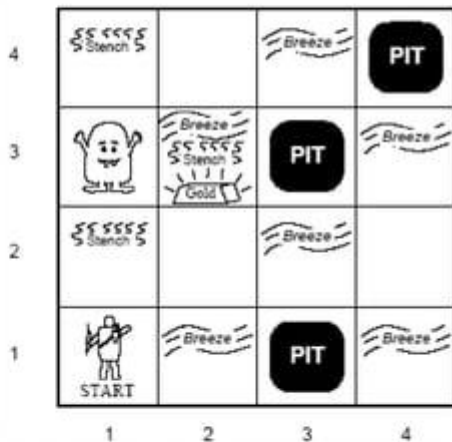
**return** *action*

# Knowledge-Based Agents

- Declarative
  - You can build a knowledge-based agent simply by “TELLing” it what it needs to know
- Procedural
  - Encode desired behaviors directly as program code
    - Minimizing the role of explicit representation and reasoning can result in a much more efficient system

# Wumpus World

- Performance Measure
  - Gold +1000, Death - 1000
  - Step -1, Use arrow -10
- Environment
  - Square adjacent to the Wumpus are smelly
  - Squares adjacent to the pit are breezy
  - Glitter iff gold is in the same square
  - Shooting kills Wumpus if you are facing it
  - Shooting uses up the only arrow
  - Grabbing picks up the gold if in the same square
  - Releasing drops the gold in the same square
- Actuators
  - Left turn, right turn, forward, grab, release, shoot
- Sensors
  - Breeze, glitter, and smell



# Wumpus World

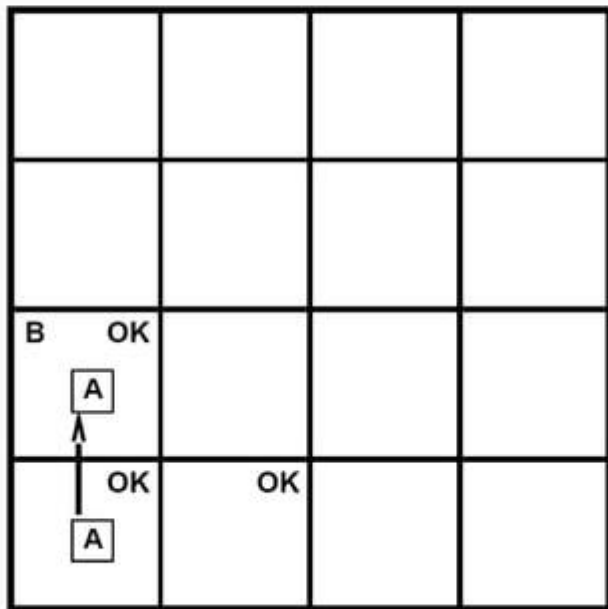
- Characterization of Wumpus World
  - Observable
    - partial, only local perception
  - Deterministic
    - Yes, outcomes are specified
  - Episodic
    - No, sequential at the level of actions
  - Static
    - Yes, Wumpus and pits do not move
  - Discrete
    - Yes
  - Single Agent
    - Yes



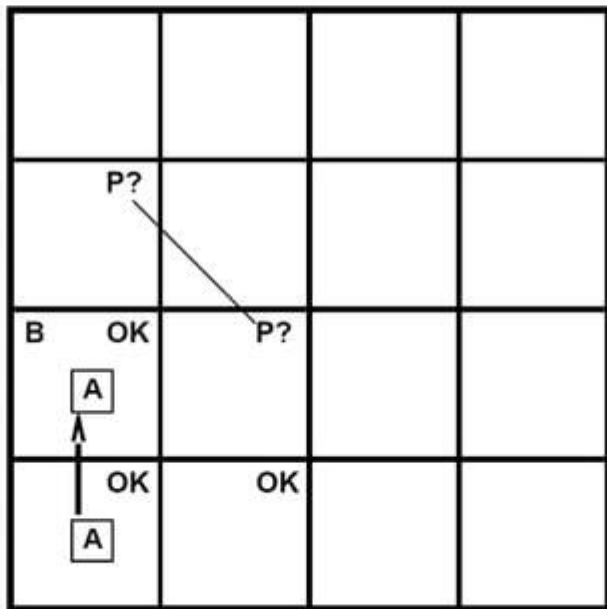
# Wumpus World

OK			
OK <input type="checkbox"/> A	OK		

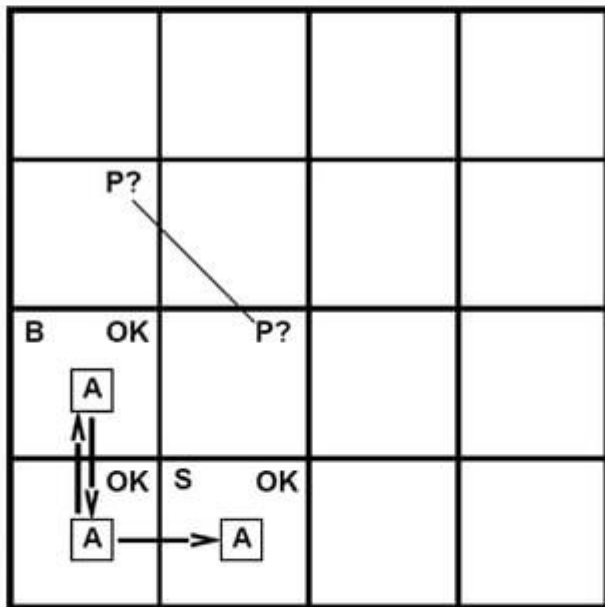
# Wumpus World



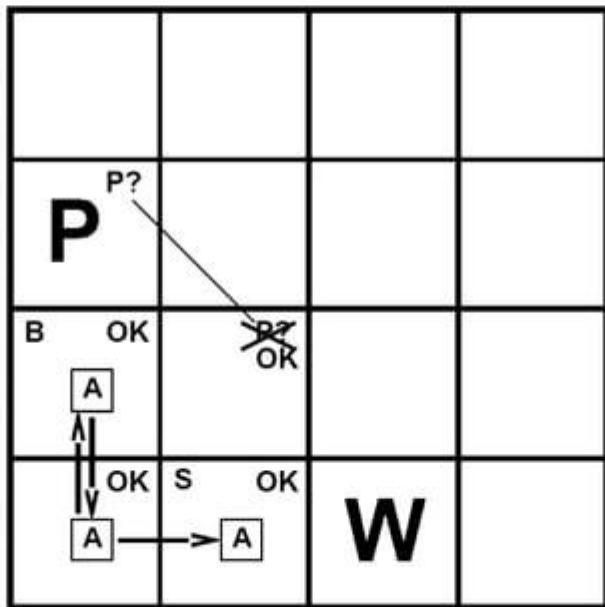
# Wumpus World



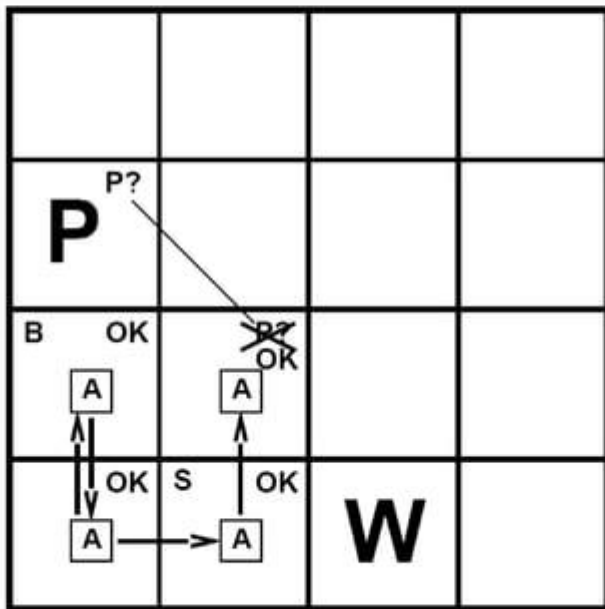
# Wumpus World



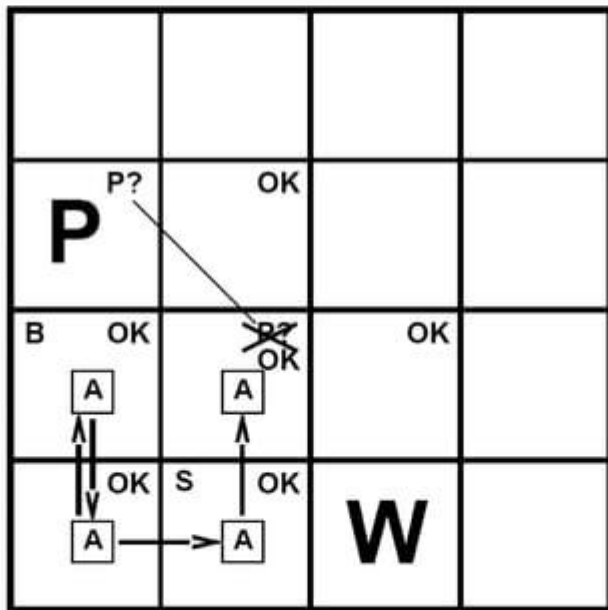
# Wumpus World



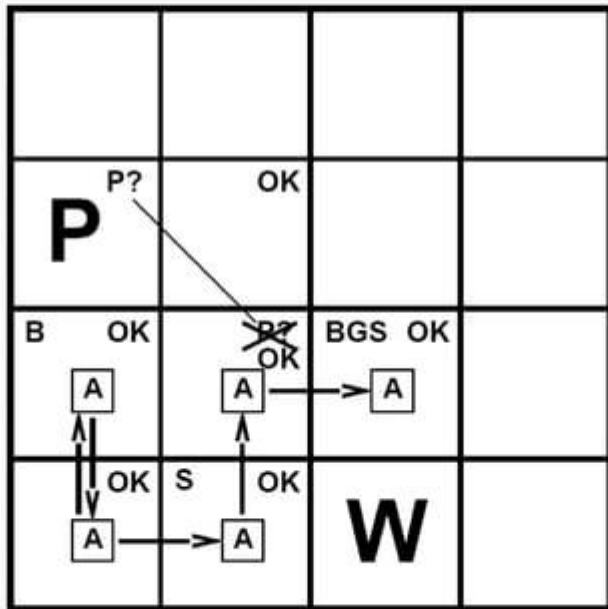
# Wumpus World



# Wumpus World

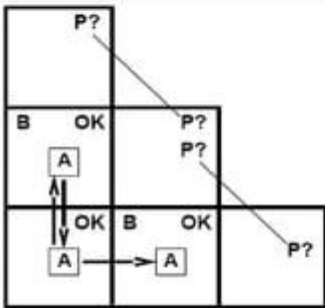


# Wumpus World

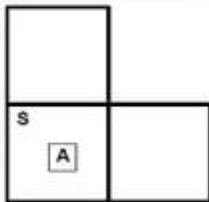




# Other Sticky Situations



- Breeze in (1,2) and (2,1)
- No safe actions



- Smell in (1,1)
- Cannot move

# Logic

- Knowledge bases consist of sentences in a formal language
  - Syntax
    - Sentences are well formed
  - Semantics
    - The “meaning” of the sentence
    - ***The truth of each sentence with respect to each possible world (model)***
- Example:
  - $x + 2 \geq y$  is a sentence
  - $x^2 + y >$  is not a sentence
  - $x + 2 \geq y$  is true iff  $x + 2$  is no less than  $y$
  - $x + 2 \geq y$  is true in a world where  $x = 7, y = 1$
  - $x + 2 \geq y$  is false in world where  $x = 0, y = 6$

# Logic

- **Entailment** means that one thing follows logically from another  
 $\alpha \models \beta$
- $\alpha \models \beta$  iff in every model in which  $\alpha$  is true,  $\beta$  is also true
- if  $\alpha$  is true, then  $\beta$  must be true
- the truth of  $\beta$  is “contained” in the truth of  $\alpha$

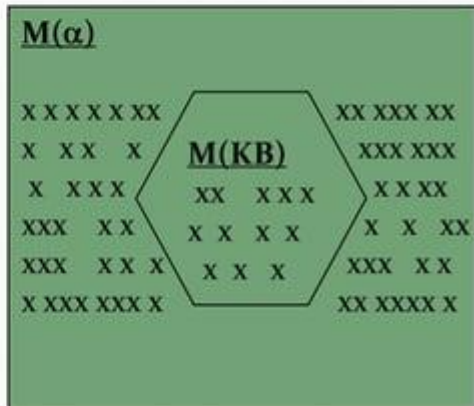
# Logic

- Example:
  - A Knowledge Base containing
    - “Cleveland won”
    - “Dallas won”
    - Entails...
      - “Either Cleveland won or Dallas won”
  
- Example:

$x + y = 4$  entails  $4 = x + y$

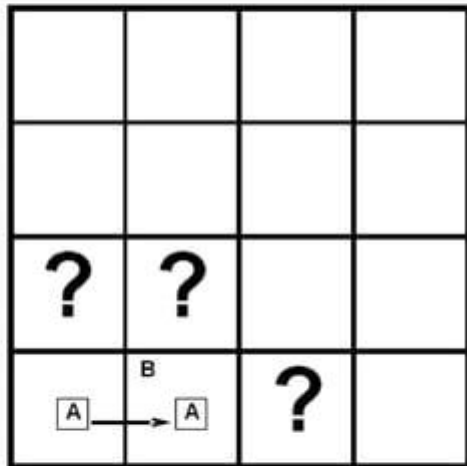
# Logic

- A model is a formally structured world with respect to which truth can be evaluated
  - M is a model of sentence  $\alpha$  if  $\alpha$  is true in m
- Then  $KB \models \alpha$  if  $M(KB) \subseteq M(\alpha)$

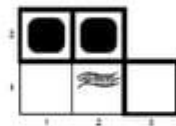
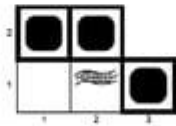
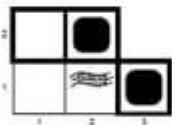
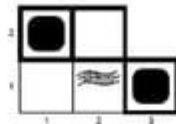
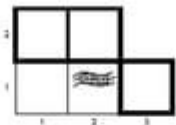
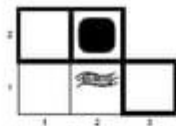
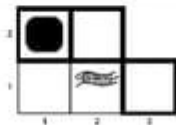
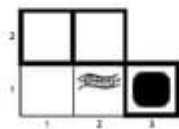


# Logic

- Entailment in Wumpus World
- Situation after detecting nothing in [1,1], moving right, breeze in [2,1]
- Consider possible models for ? assuming only pits
- 3 Boolean choices => 8 possible models



# Logic



# Logic

- ***Inference*** is the process of deriving a specific sentence from a KB (where the sentence must be entailed by the KB)
  - $KB \vdash_I \alpha$  = sentence  $\alpha$  can be derived from KB by procedure I
- “KB’s are a haystack”
  - Entailment = needle in haystack
  - Inference = finding it



# Logic

- Soundness
  - $i$  is sound if...
  - whenever  $KB \models_i \alpha$  is true,  $KB \models \alpha$  is true
- Completeness
  - $i$  is complete if
  - whenever  $KB \models \alpha$  is true,  $KB \models_i \alpha$  is true
- If  $KB$  is true in the real world, then any sentence  $\alpha$  derived from  $KB$  by a sound inference procedure is also true in the real world

# Propositional Logic

- AKA Boolean Logic
- False and True
- Proposition symbols  $P_1, P_2$ , etc are sentences
- NOT: If  $S_1$  is a sentence, then  $\neg S_1$  is a sentence (negation)
- AND: If  $S_1, S_2$  are sentences, then  $S_1 \wedge S_2$  is a sentence (conjunction)
- OR: If  $S_1, S_2$  are sentences, then  $S_1 \vee S_2$  is a sentence (disjunction)
- IMPLIES: If  $S_1, S_2$  are sentences, then  $S_1 \Rightarrow S_2$  is a sentence (implication)
- IFF: If  $S_1, S_2$  are sentences, then  $S_1 \Leftrightarrow S_2$  is a sentence (biconditional)

# Propositional Logic

<u>P</u>	<u>Q</u>	<u><math>\neg</math>P</u>	<u><math>P \wedge Q</math></u>	<u><math>P \vee Q</math></u>	<u><math>P \Rightarrow Q</math></u>	<u><math>P \Leftrightarrow Q</math></u>
<i>False</i>	<i>False</i>	<i>True</i>	<i>False</i>	<i>False</i>	<i>True</i>	<i>True</i>
<i>False</i>	<i>True</i>	<i>True</i>	<i>False</i>	<i>True</i>	<i>True</i>	<i>False</i>
<i>True</i>	<i>False</i>	<i>False</i>	<i>False</i>	<i>True</i>	<i>False</i>	<i>False</i>
<i>True</i>	<i>True</i>	<i>False</i>	<i>True</i>	<i>True</i>	<i>True</i>	<i>True</i>

# Reasoning with Horn Clauses

- Forward Chaining
  - For each new piece of data, generate all new facts, until the desired fact is generated
  - Data-directed reasoning
- Backward Chaining
  - To prove the goal, find a clause that contains the goal as its head, and prove the body recursively
  - (Backtrack when you chose the wrong clause)
  - Goal-directed reasoning

# Forward Chaining

- AND-OR Graph

- multiple links joined by an arc indicate conjunction – every link must be proved
- multiple links without an arc indicate disjunction – any link can be proved

$$P \Rightarrow Q$$

$$L \wedge M \Rightarrow P$$

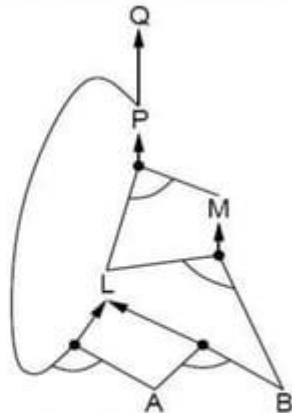
$$B \wedge L \Rightarrow M$$

$$A \wedge P \Rightarrow L$$

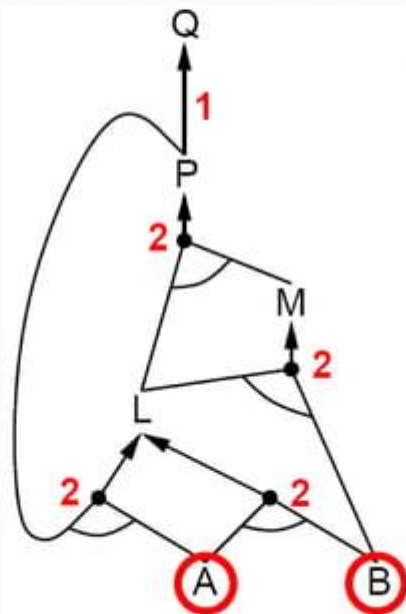
$$A \wedge B \Rightarrow L$$

$A$

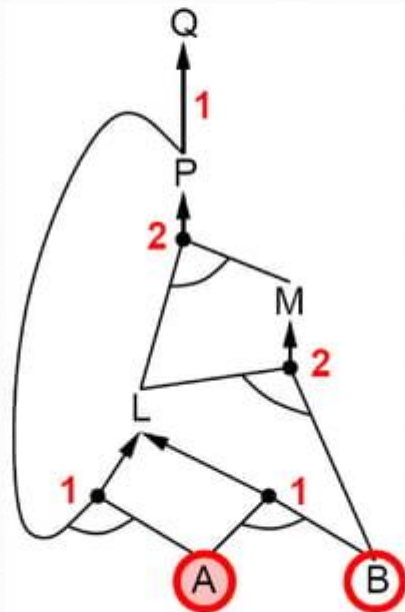
$B$



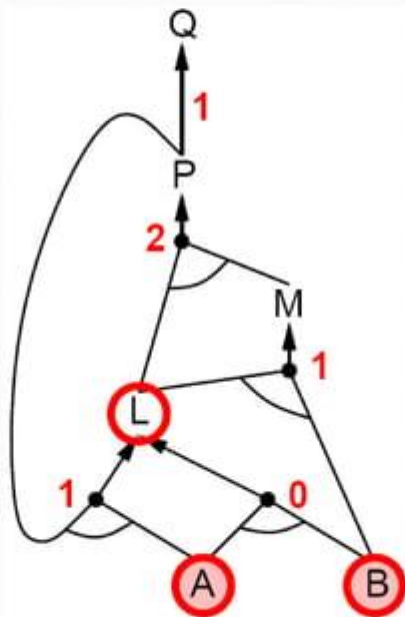
# Forward Chaining



# Forward Chaining

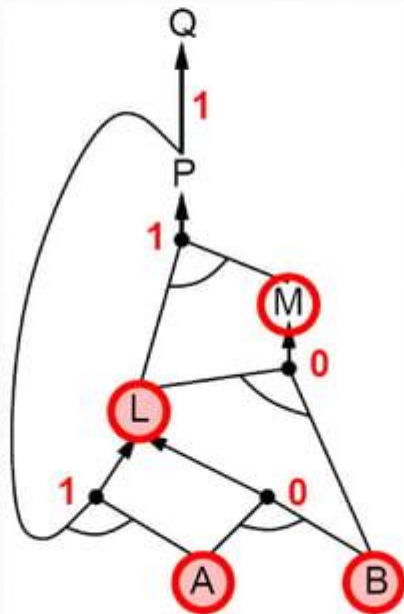


# Forward Chaining

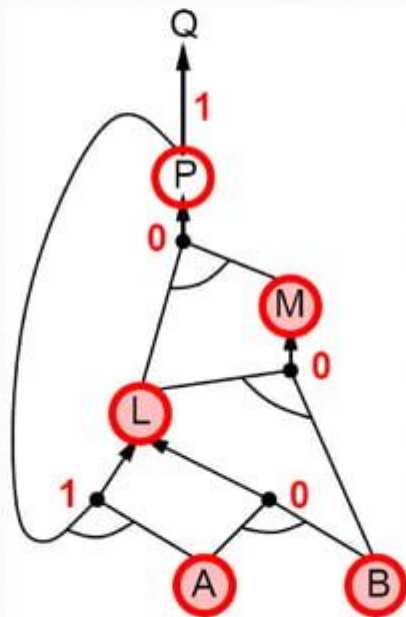




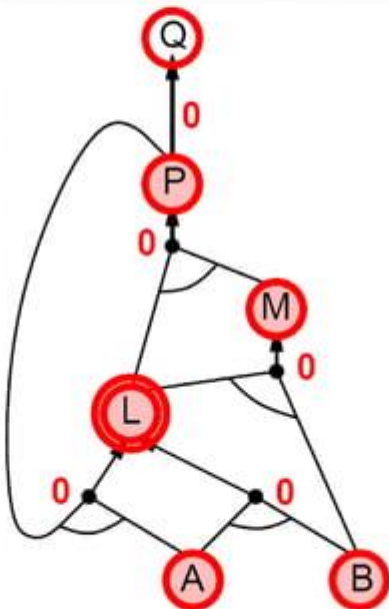
# Forward Chaining



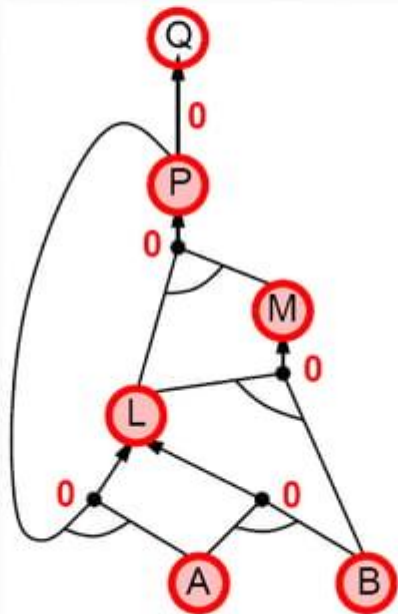
# Forward Chaining



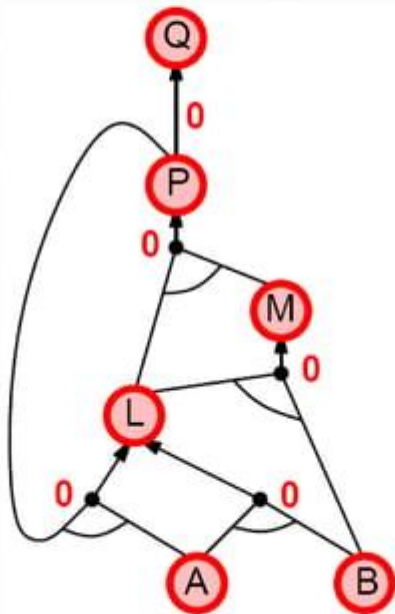
# Forward Chaining



# Forward Chaining



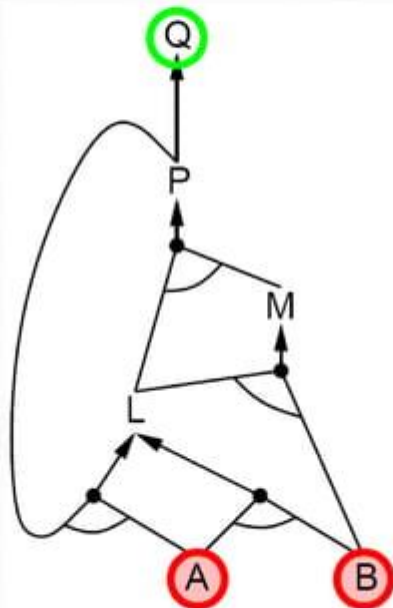
# Forward Chaining



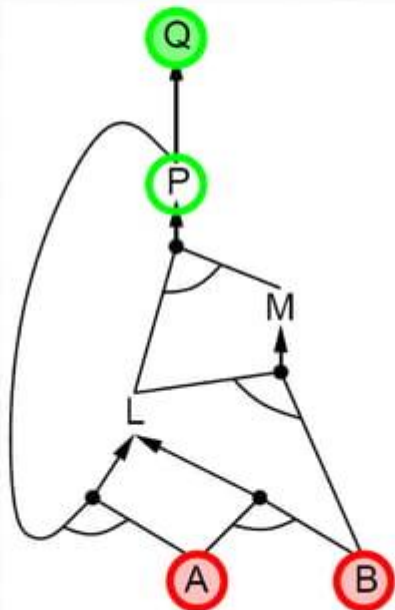
# Backward Chaining

- Idea: work backwards from the query  $q$ :
  - To prove  $q$  by BC,
    - Check if  $q$  is known already, or
    - Prove by BC all premises of some rule concluding  $q$
- Avoid loops
  - Check if new subgoal is already on the goal stack
- Avoid repeated work: check if new subgoal
  - Has already been proved true, or
  - Has already failed

# Backward Chaining

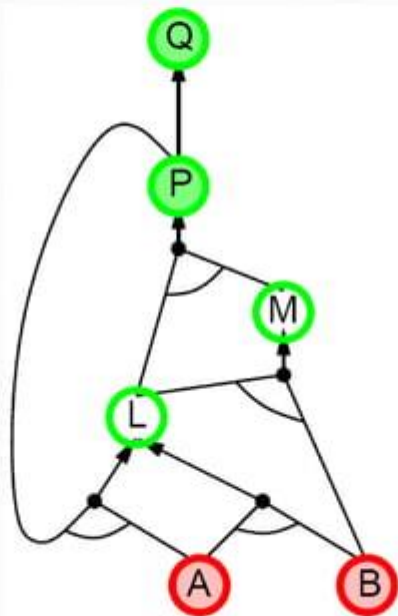


# Backward Chaining

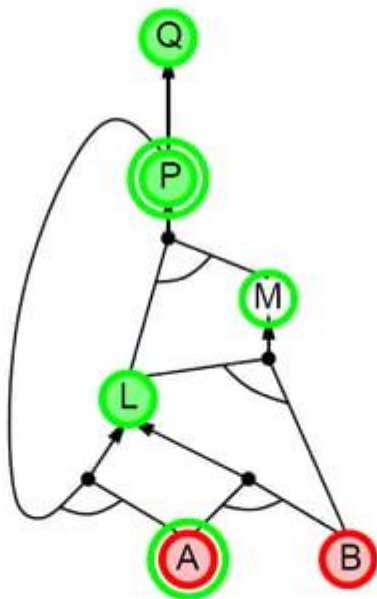




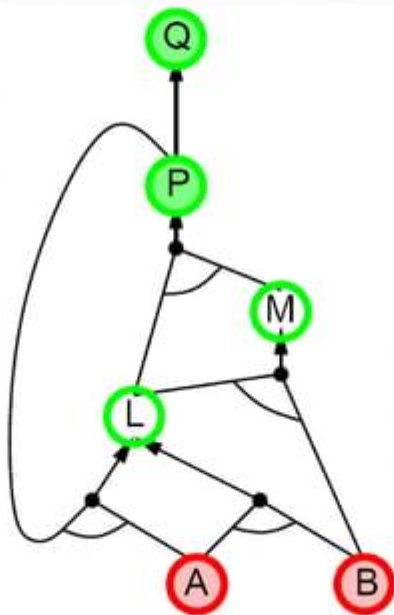
# Backward Chaining



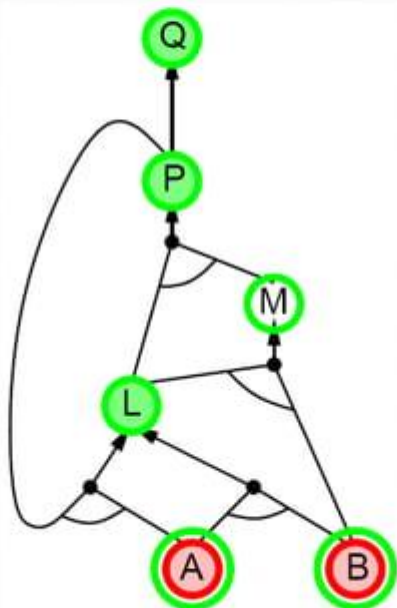
# Backward Chaining



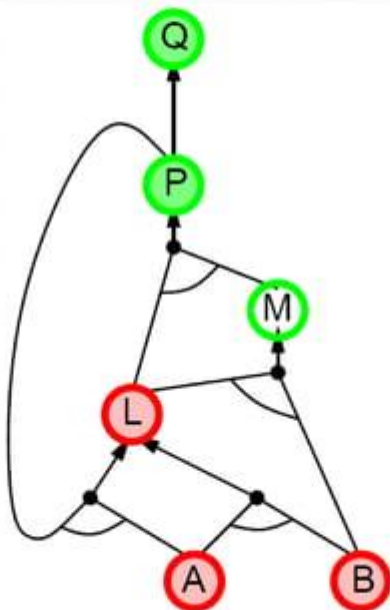
# Backward Chaining



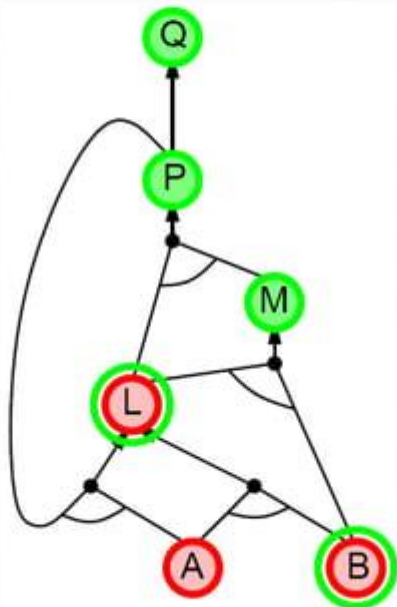
# Backward Chaining



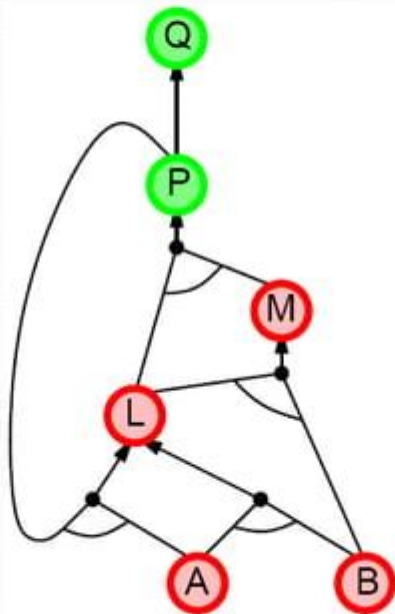
# Backward Chaining



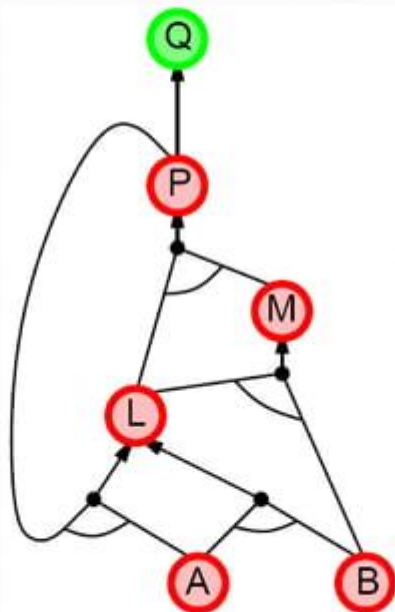
# Backward Chaining



# Backward Chaining

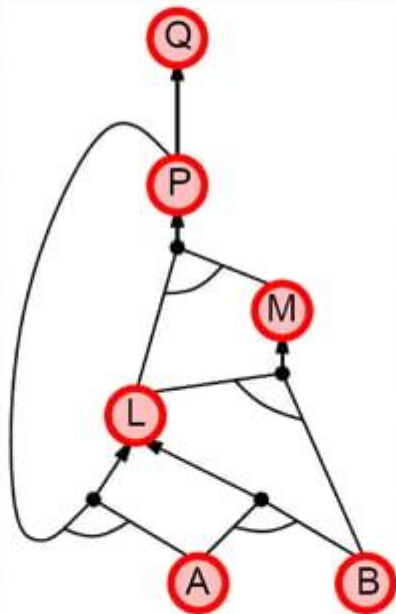


# Backward Chaining





# Backward Chaining



# Forward Chaining vs. Backward Chaining

- Forward Chaining is data driven
  - Automatic, unconscious processing
  - E.g. object recognition, routine decisions
  - May do lots of work that is irrelevant to the goal
- Backward Chaining is goal driven
  - Appropriate for problem solving
  - E.g. “Where are my keys?”, “How do I start the car?”
- The complexity of BC can be much less than linear in size of the KB



Thanks...