

① Design a simply supported at its ends & carry a live load of 25 kN/m over a span of 7 m

① Dimensions:

$$\left(\frac{l}{d} \approx 10 \text{ to } 12 \right)$$

Take $\frac{l}{d} = 12$

$$\frac{7000}{d} = 12$$

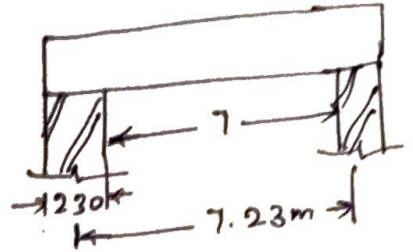
$$d = 583 \text{ say } 600 \text{ mm}$$

Take $b = 300 \text{ mm}$

Assum cover $d' = 50 \text{ mm}$

$$\therefore \text{overall depth } D = 600 + 50 = 650 \text{ mm}$$

$$d = 600 \text{ mm}, b = 300 \text{ mm}, D = 650 \text{ mm}$$



② Loads

$$D.L = 25 \times b \times D$$

$$= 25 \times 0.3 \times 0.65$$

$$= 4.875 \text{ kN/m}$$

$$L.L = 25 \text{ kN/m}$$

$$T.L = 29.875 \text{ kN/m}$$

$$\therefore \text{Factored load } W_u = 44.81 \text{ kN/m}$$

③ ultimate B.M & S.F

$$M_u = A$$

④ Eff. Span

least value of $l_{eff} = \text{clear span} + \text{eff. depth}$

i) $l_{eff} = 7000 + 600 = 7600 \text{ mm}$

ii) $l_{eff} = \text{clear span} + \text{width of support}$

$$= 7000 + 230 = 7230 \text{ mm}$$

$$\therefore l_{eff} = 7.23 \text{ m}$$

④ Ultimate moment & Shear force:

$$M_u = \frac{w_u \cdot l_{eff}^2}{8} = \frac{44.81 \times 7.23^2}{8} = 292.79 \text{ kN}\cdot\text{m}$$

$$V_u = \frac{w_u \cdot l_{eff}}{2} = \frac{44.81 \times 7.23}{2} = 161.98 \text{ kN}$$

⑤ Tension Reinforcement

$$M_{u,lim} = 0.138 f_{cu} b d^2 \\ = 0.138 \times 20 \times 230 \times 600^2 \\ = 228.53 \times 10^6 \text{ N}\cdot\text{mm} \\ = 228.53 \text{ kN}\cdot\text{m}$$

$M_u > M_{u,lim}$ — Section shall be designed as doubly reinforced section.

⑥ Check for bending

$$d = \sqrt{\frac{292.79 \times 10^6}{(0.138 \times 20 \times 300)}} \quad \text{①}$$

$$d = 594 \text{ mm}$$

$$d < d_{provided}$$

Hence safe.

Tension Reinforcement (Ref: 96)

(2)

$$i) M_u - \text{Mulin} = 292.74 - 228.53$$

$$= 64.21 \text{ KN}\cdot\text{m}$$

$$ii) f_{sc} = \frac{0.0035 (x_{u \max} - d')}{x_{u \max}} \times E_s$$

$$\frac{x_{u \max}}{d} = 0.48$$

$$x_{u \max} = 0.48 \times 600 = 288 \text{ mm}$$

$$E_s = 2 \times 10^5 \text{ N/mm}^2$$

$$= \frac{0.0035 (288 - 50)}{288} \times (2 \times 10^5)$$

$$f_{sc} = 578 \text{ N/mm}^2$$

iii) $A_{st} = A_{st1} + A_{st2}$
⑥ To calculate A_{st1} use formula G.1.1. ⑤ - P. 2096

$$\frac{x_{u \max}}{d} = \frac{0.87 f_y (A_{st1})}{0.36 f_{ck} b d}$$
$$0.48 = \frac{0.87 \times 415 \times (A_{st1})}{0.36 \times 20 \times 220 \times 600}$$

$$A_{st1} = 1321 \text{ mm}^2$$

⑦ To calculate A_{st2} use formula G.1.2.

$$A_{st2} = A_{sc} f_{sc} / 0.87 f_y$$

$$\text{but } M_u - \text{Mulin} = f_{sc} A_{sc} (d - d')$$

$$64.21 \times 10^6 = 578 \times A_{sc} (600 - 50)$$

$$A_{sc} = 201.98 \text{ mm}^2$$

Provide 2 Nos of 12mm ϕ rods $\Rightarrow 226 \text{ mm}^2$

$$A_{st2} = \frac{A_{sc} f_{sc}}{0.87 f_y} = \frac{201.98 \times 578}{0.87 \times 415}$$

$$A_{st2} = 323.35 \text{ mm}^2$$

$$A_{st} = A_{st1} + A_{st2}$$

$$= 1321 + 323$$

$$A_{st} = 1644 \text{ mm}^2$$

Adopt 4 Nos of 25mm ϕ rods } = 1963mm²
as a tension reinforcement

⑧ Step 8

Check for shear

$$\tau_v = \frac{V_u}{bd}$$

$$= \frac{161.98 \times 10^3}{300 \times 600}$$

$$= 0.89 \text{ N/mm}^2$$

$$P_E = \frac{100 A_{st}}{bd} = \frac{100 \times 1963}{300 \times 600} = 0.11$$

$$\tau_c = 0.28 \text{ N/mm}^2$$

$\tau_v > \tau_c$, Hence provide shear reinforcement.

$$V_{us} = V_u - \tau_c bd$$

$$= (161.98 \times 10^3) - (0.28 \times 300 \times 600)$$

$$= 111.58 \times 10^3 \text{ N}$$

$$V_{us} = \frac{0.87 f_y A_{sv} d}{S_v}$$

Assume 8mm 2 legged stirrups

$$A_{sv} = 2 \times \frac{\pi}{4} \times 8^2 = 100.5 \text{ mm}^2$$

$$S_v = \frac{0.87 \times 415 \times 100.5 \times 600}{111.58 \times 10^3}$$

$$= 195 \text{ mm} \approx 190 \text{ mm}$$

54
Provide
⑨ check

$$S_v \neq 0.75d = 0.75 \times 600 = 450 \text{ mm} \quad (3)$$

Provide 8mm 2 legged stirrups @ 190mm c/c.

⑨ check for deflection:

$$\left(\frac{l}{d}\right)_{\text{max}} = \left(\frac{l}{d}\right)_{\text{basic}} \times k_f \times k_c \times k_{sf}$$

$$k_f = 1.6 \quad (\text{Fig. 4 DNO 38})$$

$$k_c = \frac{100 A_{sc}}{bd} = \frac{100 \times 201}{300 \times 600} = 0.112$$

$$\therefore k_c = 1.05 \quad (\text{Fig 5 - DNO. 39})$$

$$k_f = 1$$

$$\therefore \left(\frac{l}{d}\right)_{\text{max}} = 12 \times 1.6 \times 1.05 \times 1$$

$$= 20.16$$

$$\left(\frac{l}{d}\right)_{\text{act}} = \frac{l_{\text{eff}}}{d_{\text{eff}}} = \frac{7230}{600} = 12.05$$

$$\left(\frac{l}{d}\right)_{\text{act}} < \left(\frac{l}{d}\right)_{\text{max}}$$

Hence safe.

⑩ check for torsion

$$l_d \leq \frac{M_1}{V} + L_0$$

$$l_d = \frac{0.87 f_y \phi}{A_{c,bd}}$$

$$= \frac{0.87 \times 415 \times 25}{4 \times 1.2 \times 1.6}$$

$$= 1175 \text{ mm}$$

$$M_1 = 0.87 f_y A_{st} (d - 0.42 x_{u, \text{max}})$$

$$= 0.87 \times 415 \times 1963 (600 - 0.42 \times 288)$$

$$= 339.52 \times 10^6 \text{ KN}\cdot\text{m}$$

$$l_0 \rightarrow \text{greater of } 0.6 = 12 \phi \text{ (or) } d$$

$$= 12 \times 25 \text{ (or) } 600$$

$$= 300 \text{ or } 600$$

$$\therefore l_0 = 600 \text{ mm}$$

$$\frac{M_1}{V} + l_0 = \frac{339.52 \times 10^6}{161.98 \times 10^3} + 600$$

$$= 2696 \text{ mm}$$

$$\therefore l_d < \frac{M_1}{V} + l_0$$

$$(1175) < (2696)$$

