

BFS:

Breadth first search:

⇒ It produces spanning tree as a final result is graph without loops.

⇒ We use Queue data structure with maximum size of total number of vertices in the graph to implement BFS of a graph:

Algorithm:

Step 1: Define a Queue of size, i.e. total number of vertices in the graph.

Step 2: Select any vertex as starting point from traversal. Visit vertex and insert it into the queue.

Step 3:

Visit all the adjacent vertices of the vertex which is at front of the queue, which is not visited and insert them into the queue.

Step 4:

When there is no new vertex to be visit from the vertex at front of the queue then delete that vertex from the Queue.

Step 5:

Repeat step 3 & 4 until queue becomes empty.

Step 6:

When Queue becomes empty then produce final spanning tree by removing unused edges from the graph.

Routines

```
void BFT (vertex u)
```

```
{
```

```
  Initialize Queue Q;
```

```
  Visited [u] = 1;
```

```
  Enqueue (u, Q);
```

```
  while (!IsEmpty(Q))
```

```
  {
```

```
    u = Dequeue (Q);
```

```
    Print u;
```

```
    for all vertices v adjacent to u
```

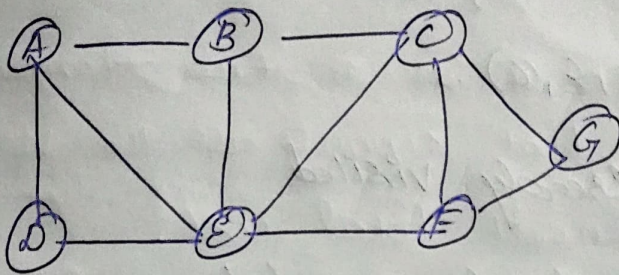
```
    if (visited [v] == 0) then
```

```
    {
```

```
      enqueue (v, Q); visited [v] = 1;
```

```
    } }
```

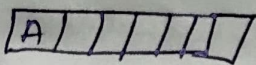

Example:



Step 1:

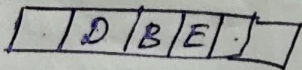
⇒ Select vertex A as starting point

⇒ Insert A into queue.



Step 2:

* Visit all $\text{adj}(A)$ which are not visited (D, B, E).

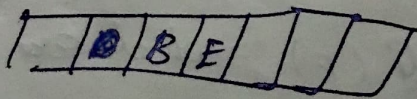


Step 3:

* Visit all $\text{adj}(D)$, which are not visited (A, E) ⇒ already visited.

* There is no vertex

* Delete D from queue.



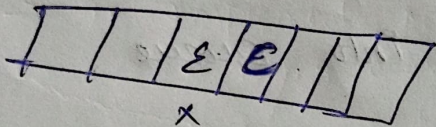
step 4:

* visit all adj (B), which are not visited (A, E, C).

* A → already visited

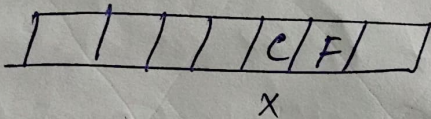
* E → already inserted

C → Inserted



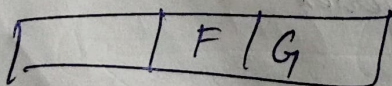
Step 5:

* visit all adj (E), which are not visited (D, B, C, F).



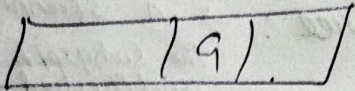
Step 6.

* visit all adj (C), which are not visited (B, E, F, G)



Step 7:

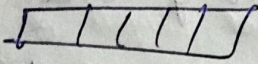
* visit all adj (F), which are not visited (E, C, G)



Step 8:

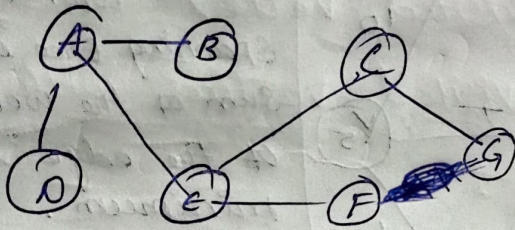
* Adj (9)

* $G = (C, E)$



* Queue is became empty, Stop BFS Process

* final spanning tree by removing unused edges.



Application of BFS:

1. unweighted Graphs
2. Peer to Peer networks.
3. Web crawlers
4. Navigation systems
5. Network Broadcasting.