



**SNS COLLEGE OF ENGINEERING**  
**(Autonomous)**  
**DEPARTMENT OF ELECTRONICS AND COMMUNICATION ENGINEERING**



**19EC504 – TRANSMISSION LINES AND ANTENNAS**

III YEAR/ V SEMESTER

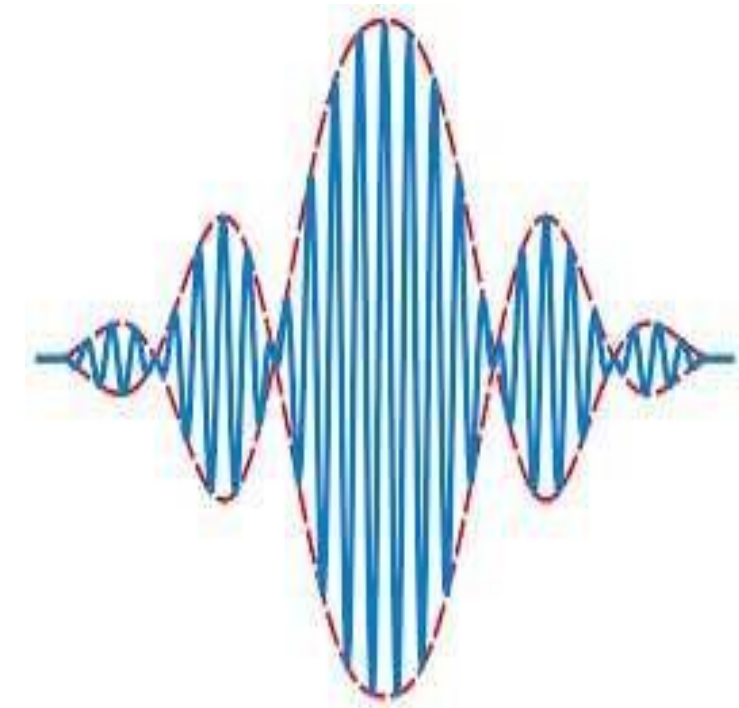
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**UNIT 2 – GUIDED WAVES**

**TOPIC 1– WAVES BETWEEN PARALLEL PLANES**



# WHAT DO YOU RELATE FROM THIS ?





# WAVES



A wave is a disturbance (change from equilibrium) of one or more fields such that the field values oscillate repeatedly about a stable equilibrium

**TWO TYPES**

**Mechanical Waves**

**Electromagnetic Waves**

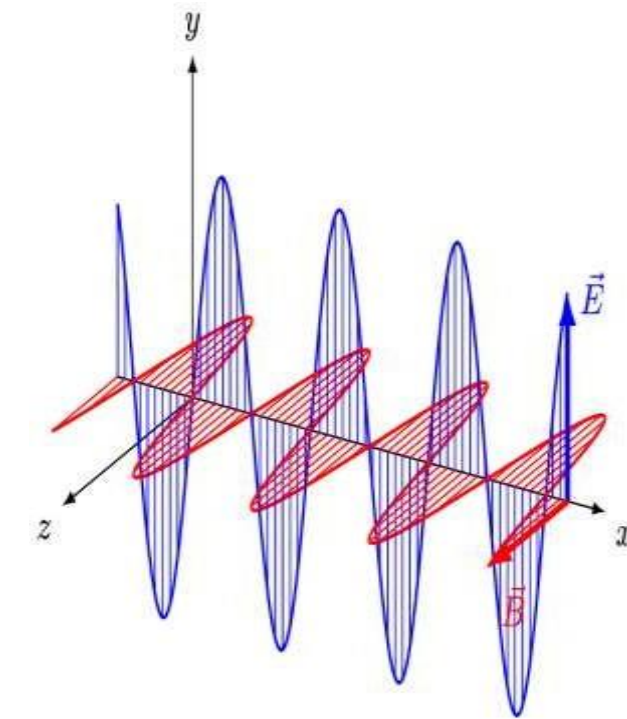




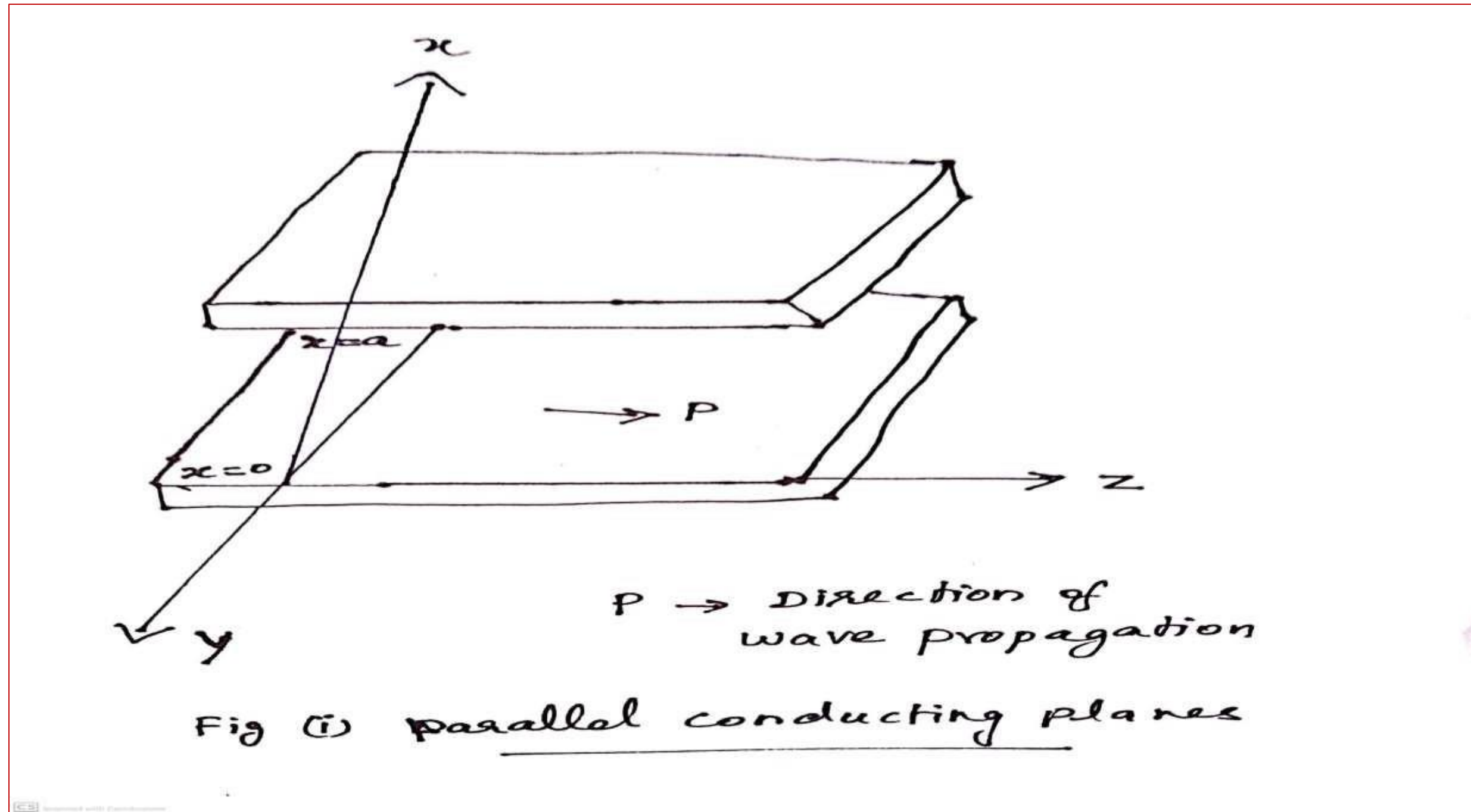
# ELECTROMAGNETIC WAVES



- Electromagnetic waves are also known as EM waves
- Produced when an electric field comes in contact with the magnetic field
- They are the composition of oscillating electric and magnetic fields
- They are solutions of Maxwell's equations which are the fundamental equations of electrodynamics



# EM WAVE PROPAGATION BETWEEN PARALLEL PLANES





# EM WAVE PROPAGATION BETWEEN PARALLEL PLANES - ANALYSIS



In order to determine the EM field configuration in the region between the planes  
→ Maxwell's equations will be solved  
→ subject to appropriate boundary conditions.

## Maxwell's Equations

$$\nabla \times H = \sigma + j\omega \epsilon E$$

( $\sigma = 0$ , since medium between the plane is air)

$$\therefore \nabla \times H = j\omega \epsilon E$$

$$\nabla \times E = -j\omega \mu H$$

## Boundary conditions for perfectly conducting planes

$$E_{\text{tan}} = 0$$

$$H_{\text{nor}} = 0$$



# EM WAVE PROPAGATION BETWEEN PARALLEL PLANES - ANALYSIS



Wave equations

$$\nabla^2 E = \gamma^2 E$$

$$\nabla^2 H = \gamma^2 H$$

$$\gamma = \sqrt{(\sigma + j\omega\epsilon)(j\omega\mu)}$$

$$\sigma = 0$$

$$\therefore \gamma = \sqrt{j\omega\epsilon \times j\omega\mu} = j\omega\sqrt{\mu\epsilon}$$

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# EM WAVE PROPAGATION BETWEEN PARALLEL PLANES - ANALYSIS



In rectangular co-ordinates & free non-conducting region

$$\boxed{\nabla \times \mathbf{H} = -j\omega \epsilon \mathbf{E}}$$
$$\begin{vmatrix} \vec{a}_x & \vec{a}_y & \vec{a}_z \\ \partial/\partial x & \partial/\partial y & \partial/\partial z \\ H_x & H_y & H_z \end{vmatrix} = -j\omega \epsilon \left[ E_x \vec{a}_x + E_y \vec{a}_y + E_z \vec{a}_z \right]$$

By equating, we get three equations.

$$\frac{\partial H_z}{\partial y} - \frac{\partial H_y}{\partial z} = j\omega \epsilon E_x \rightarrow \textcircled{1}$$

$$-\left[ \frac{\partial H_z}{\partial y} - \frac{\partial H_x}{\partial z} \right] = j\omega \epsilon E_y \rightarrow \textcircled{2}$$

$$\frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y} = j\omega \epsilon E_z \rightarrow \textcircled{3}$$

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# EM WAVE PROPAGATION BETWEEN PARALLEL PLANES - ANALYSIS



111deg for  $\boxed{\nabla \times \mathbf{E} = -j\omega\mu\mathbf{H}}$

$$\frac{\partial E_z}{\partial y} - \frac{\partial E_y}{\partial z} = -j\omega\mu E_x \rightarrow \textcircled{4}$$

$$- \left[ \frac{\partial E_z}{\partial x} - \frac{\partial E_x}{\partial z} \right] = -j\omega\mu E_y \rightarrow \textcircled{5}$$

$$\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} = -j\omega\mu E_z \rightarrow \textcircled{6}$$

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# EM WAVE PROPAGATION BETWEEN PARALLEL PLANES - ANALYSIS



Propagation constant

$$\bar{\gamma} = \bar{\alpha} + j\bar{\beta}$$

- \* If  $\bar{\gamma} \rightarrow$  real,  $\bar{\alpha}$  have value,  $\bar{\beta} = 0$   
 $\rightarrow$  represents there is no wave motion, but only an exponential decrease in Amplitude.
- \* If  $\bar{\gamma} \rightarrow$  imaginary,  $\bar{\alpha} = 0$ ,  $\bar{\beta}$  have value  
 $\rightarrow$  represents a wave propagation, but no attenuation.

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# EM WAVE PROPAGATION BETWEEN PARALLEL PLANES - ANALYSIS



## Important Assumptions

\* In  $y$ -direction  $\rightarrow$  the field is uniform and constant.

$$\therefore \frac{\partial}{\partial y} = 0$$

\* In  $x$ -direction  $\rightarrow$  certain boundary must met.

$$\text{so } \frac{\partial}{\partial x} \rightarrow \text{no change}$$

\* In  $z$ -direction  $\rightarrow$  the wave is assumed to propagate

$$\therefore \frac{\partial}{\partial z} = -\gamma$$
$$\frac{\partial^2}{\partial z^2} = \gamma^2$$

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# EM WAVE PROPAGATION BETWEEN PARALLEL PLANES - ANALYSIS



After substituting assumptions → eqns ① to ⑥ becomes,

$$\nabla H_y = j\omega \epsilon E_x \rightarrow \textcircled{7}$$

$$-\nabla H_x - \frac{\partial H_z}{\partial x} = j\omega \epsilon E_y \rightarrow \textcircled{8}$$

$$\frac{\partial H_y}{\partial x} = j\omega \epsilon E_z \rightarrow \textcircled{9}$$

$$\nabla E_y = -j\omega \mu H_x \rightarrow \textcircled{10}$$

$$-\nabla E_x - \frac{\partial E_z}{\partial x} = -j\omega \mu H_y \rightarrow \textcircled{11}$$

$$\frac{\partial E_y}{\partial x} = -j\omega \mu H_x \rightarrow \textcircled{12}$$



# EM WAVE PROPAGATION BETWEEN PARALLEL PLANES - ANALYSIS



Solving Eqns. (7), (8), (10) & (11) simultaneously, we get

$$E_x = \frac{\gamma}{h^2} \frac{\partial E_z}{\partial x} \rightarrow (12)$$
$$H_y = \frac{-j\omega\epsilon}{h^2} \frac{\partial E_z}{\partial x} \rightarrow (13)$$
$$E_y = \frac{j\omega\mu}{h^2} \frac{\partial H_z}{\partial x} \rightarrow (14)$$
$$H_x = -\frac{\gamma}{h^2} \frac{\partial H_z}{\partial x} \rightarrow (15)$$

where  $h^2 = \gamma^2 + \omega^2\mu\epsilon$

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## CONCLUSION



- In equations 12 & 13 there is a component of electric field in the direction of propagation ( $E_z$ ), but no component of magnetic field ( $H_z$ )
- These waves are known as E waves or Transverse Magnetic (TM) waves
- In equations 14 & 15 there is a component of magnetic field in the direction of propagation ( $H_z$ ), but no component of electric field ( $E_z$ )
- These waves are known as H waves or Transverse Electric (TE) waves