



**SNS COLLEGE OF ENGINEERING**  
**(Autonomous)**  
**DEPARTMENT OF CSE - IoT**



**COURSE NAME:19EC306 / DIGITAL CIRCUITS**  
**II YEAR/III SEMESTER**

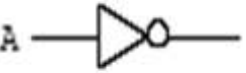
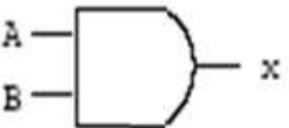
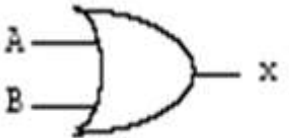
**UNIT:1- MINIMIZATION TECHNIQUES AND LOGIC GATES**

**TOPIC:LOGIC GATES**

# Boolean function and truth table



## ■ The most basic gates are

Name	Graphic symbol	Algebraic function	Truth table															
Inverter	A  x	$x = A'$	<table border="1"> <tr><td>A</td><td>x</td></tr> <tr><td>0</td><td>1</td></tr> <tr><td>1</td><td>0</td></tr> </table>	A	x	0	1	1	0									
A	x																	
0	1																	
1	0																	
AND	A  B x	$x = AB$	<table border="1"> <tr><td>A</td><td>B</td><td>x</td></tr> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>0</td></tr> <tr><td>1</td><td>0</td><td>0</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </table> <p>True if both are true.</p>	A	B	x	0	0	0	0	1	0	1	0	0	1	1	1
A	B	x																
0	0	0																
0	1	0																
1	0	0																
1	1	1																
OR	A  B x	$x = A + B$	<table border="1"> <tr><td>A</td><td>B</td><td>x</td></tr> <tr><td>0</td><td>0</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td></tr> <tr><td>1</td><td>0</td><td>1</td></tr> <tr><td>1</td><td>1</td><td>1</td></tr> </table> <p>True if either one is true.</p>	A	B	x	0	0	0	0	1	1	1	0	1	1	1	1
A	B	x																
0	0	0																
0	1	1																
1	0	1																
1	1	1																

# Boolean function and truth table



- Other common gates include:

Name	Graphic symbol	Algebraic function	Truth table															
Exclusive-OR (XOR)		$x = A \oplus B$ $= A'B + AB'$	<table border="1"> <thead> <tr> <th>A</th> <th>B</th> <th>x</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> </tr> <tr> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>0</td> </tr> </tbody> </table>	A	B	x	0	0	0	0	1	1	1	0	1	1	1	0
A	B	x																
0	0	0																
0	1	1																
1	0	1																
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NAND		$x = (AB)'$	<table border="1"> <thead> <tr> <th>A</th> <th>B</th> <th>x</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>1</td> </tr> <tr> <td>0</td> <td>1</td> <td>1</td> </tr> <tr> <td>1</td> <td>0</td> <td>1</td> </tr> <tr> <td>1</td> <td>1</td> <td>0</td> </tr> </tbody> </table>	A	B	x	0	0	1	0	1	1	1	0	1	1	1	0
A	B	x																
0	0	1																
0	1	1																
1	0	1																
1	1	0																
NOR		$x = A + B$	<table border="1"> <thead> <tr> <th>A</th> <th>B</th> <th>x</th> </tr> </thead> <tbody> <tr> <td>0</td> <td>0</td> <td>1</td> </tr> <tr> <td>0</td> <td>1</td> <td>0</td> </tr> <tr> <td>1</td> <td>0</td> <td>0</td> </tr> <tr> <td>1</td> <td>1</td> <td>0</td> </tr> </tbody> </table>	A	B	x	0	0	1	0	1	0	1	0	0	1	1	0
A	B	x																
0	0	1																
0	1	0																
1	0	0																
1	1	0																

Parity check: True if only one is true.

Inversion of AND.

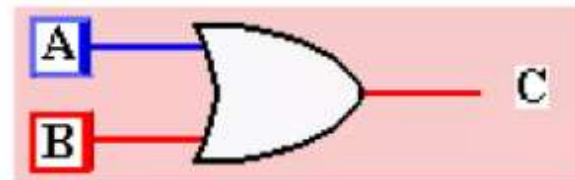
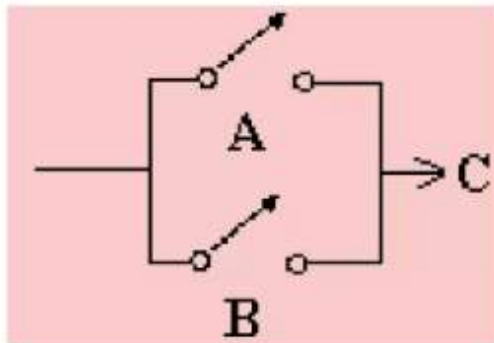
Inversion of OR.

# OR GATE



❖ Current flows if either switch is closed

– Logic notation  $A + B = C$



A	B	C
0	0	0
0	1	1
1	0	1
1	1	1

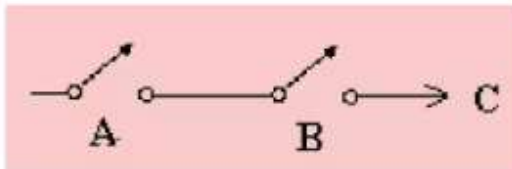
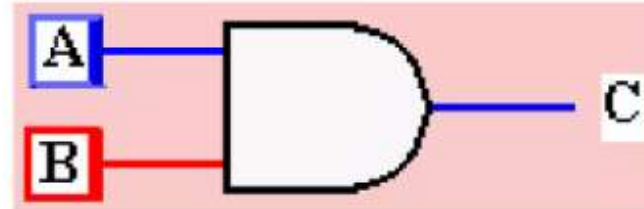


# AND GATE

## AND Gate

- ❖ In order for current to flow, both switches must be closed

– Logic notation  $A \cdot B = C$   
(Sometimes  $AB = C$ )

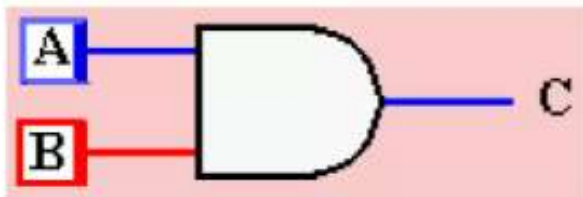


A	B	C
0	0	0
0	1	0
1	0	0
1	1	1

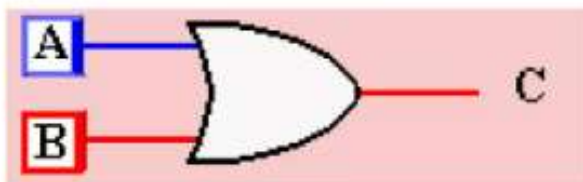
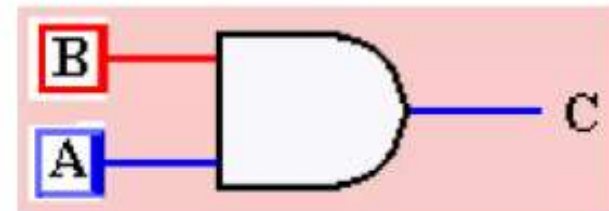
# PROPERTIES OF AND & OR



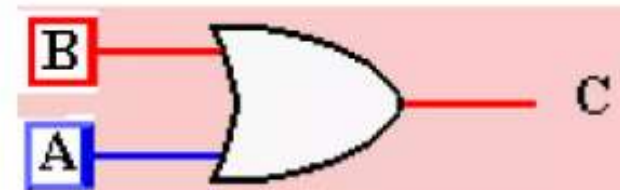
- Commutation
  - $A + B = B + A$
  - $A \cdot B = B \cdot A$



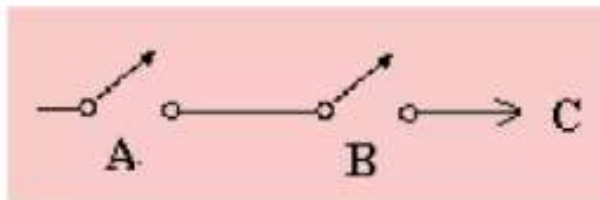
Same as



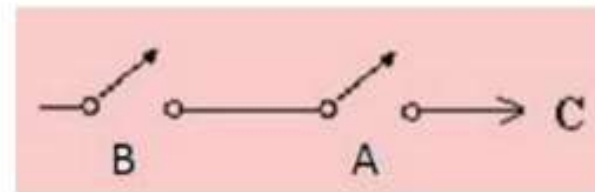
Same as



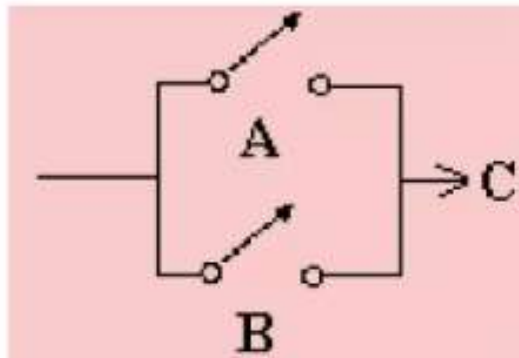
# COMMUTATION CIRCUIT



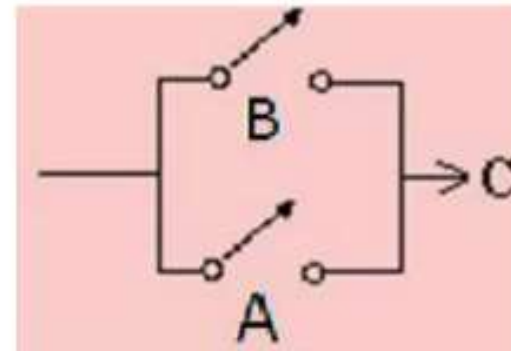
$A \cdot B$



$B \cdot A$



$A + B$

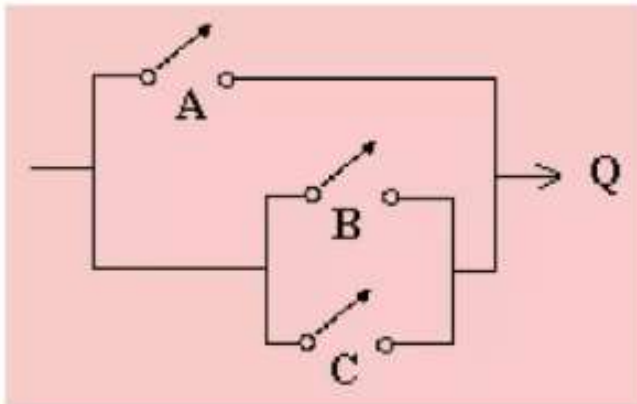


$B + A$

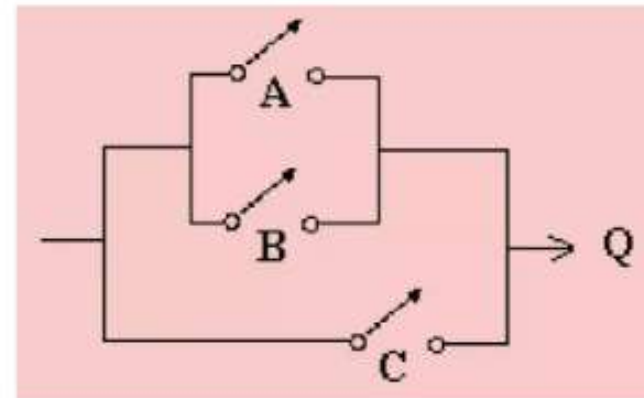
# ASSOCIATIVE CIRCUIT



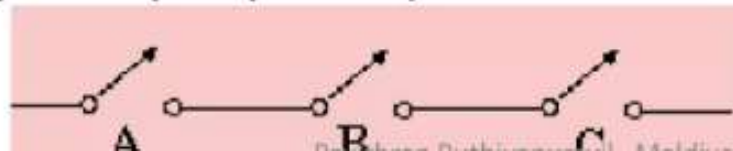
$$\blacklozenge A + (B + C) = (A + B) + C$$



=



$$\blacklozenge A \cdot (B \cdot C) = (A \cdot B) \cdot C$$

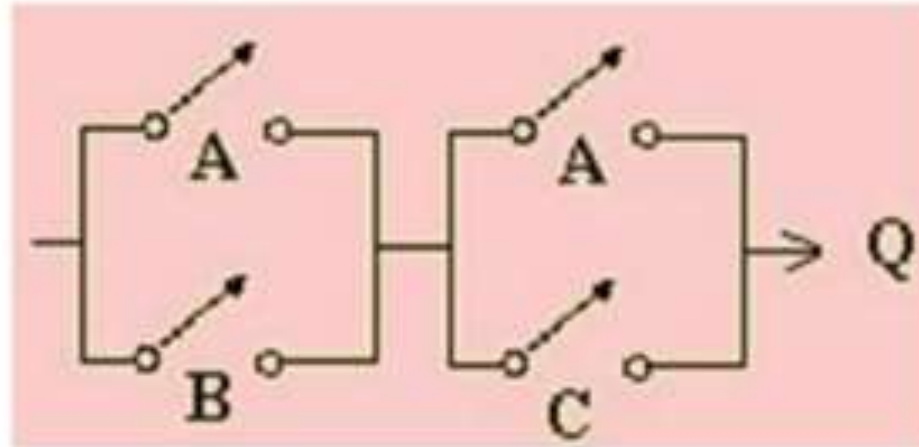




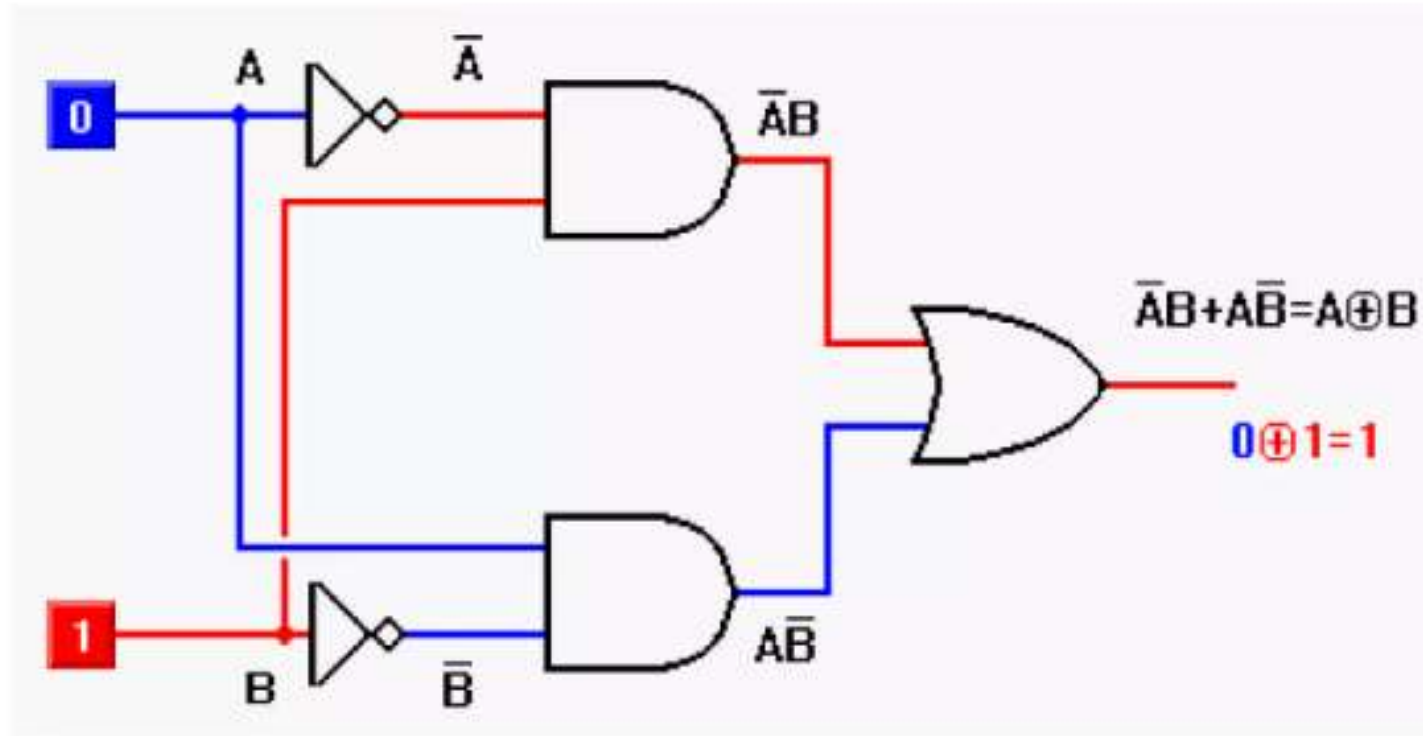
# DISTRIBUTIVE PROPERTY



$$(A + B) \cdot (A + C)$$



# CIRCUIT FOR XOR

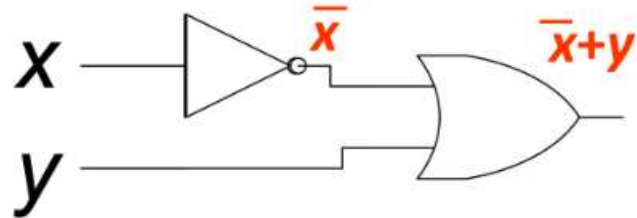


$$A \oplus B = \bar{A} \cdot B + A \cdot \bar{B}$$

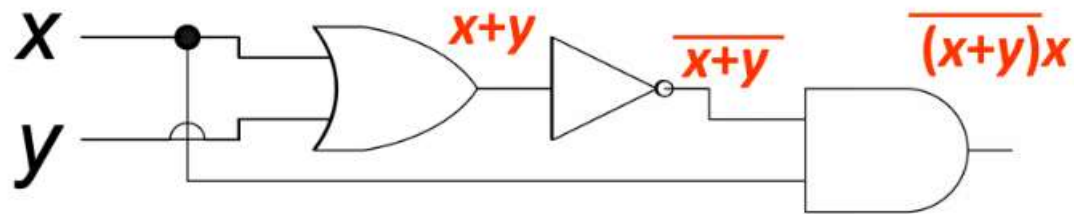
# Converting between circuits and equations



a)  $\bar{x}+y$



b)  $\overline{(x+y)}x$





*Thank  
you*