



# **SNS COLLEGE OF ENGINEERING**

Kurumbapalayam (Po), Coimbatore – 641 107

**An Autonomous Institution**

Accredited by NBA – AICTE and Accredited by NAAC – UGC with ‘A’ Grade  
Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

**DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING(IoT and  
Cybersecurity Including BCT)**

COURSE NAME : Fundamentals Of Cryptography

II YEAR / III SEMESTER

Unit I

Topic :Modular Arithmetic



# Modular Arithmetic



## Congruence

In cryptography congruence ( $\cong$ ) instead of equality (=)



### Examples:

$$15 \cong 3(\text{mod } 12)$$

$$23 \cong 11(\text{mod } 12)$$

$$33 \cong 3(\text{mod } 10)$$

$$10 \cong -2(\text{mod } 12)$$

So ,  $a \cong b(\text{mod } m)$

i.e  $a = km + b$



## VALID OR INVALID

$$38 \cong 2 \pmod{12}$$

$$38 \cong 14 \pmod{12}$$

$$5 \cong 0 \pmod{5}$$

$$10 \cong 2 \pmod{6}$$

$$13 \cong 3 \pmod{13}$$

$$2 \cong -3 \pmod{5}$$



## One more Analogy

NO of wraps (Quotient)	Remaining Thread (Remainder)	Congruence
1	25	$35 \cong 25 \pmod{1}$
2	15	$35 \cong 15 \pmod{2}$
3	5	$35 \cong 5 \pmod{3}$



# Properties Of Modular Arithmetic

1.  $[(a \bmod n) + (b \bmod n)] \bmod n = (a + b) \bmod n$
2.  $[(a \bmod n) - (b \bmod n)] \bmod n = (a - b) \bmod n$
3.  $[(a \bmod n) * (b \bmod n)] \bmod n = (a * b) \bmod n$