## TUTORIAL 3

1. Prove that $(\forall \mathbf{x})(\mathbf{P}(\mathbf{x}) \rightarrow \mathbf{Q}(\mathbf{x})),(\forall \mathbf{x})(\mathbf{R}(\mathbf{x}) \rightarrow\rceil \mathbf{Q}(\mathbf{x})) \Rightarrow(\forall \mathbf{x})(\mathbf{R}(\mathbf{x}) \rightarrow\rceil \mathbf{P}(\mathbf{x}))$.
2. Show that the conclusion $(\forall \mathbf{x})(F(x) \rightarrow 7 S(x))$ follows from the premises $(\exists x)(F(x) \wedge S(x)) \rightarrow(y)$ $(M(y) \rightarrow W(y))$ and $(\exists y)(M(y) \wedge\rceil W(y))$.
3. Show that $(\forall \mathbf{x})(\mathbf{P}(\mathbf{x}) \vee \mathbf{Q}(x)) \Rightarrow(\forall \mathbf{x})(\mathbf{P}(\mathbf{x}) \vee(\exists \mathbf{x}) \mathbf{Q}(\mathbf{x}))$ by indirect method of proof.
4. Show that $(\mathbf{x})(\mathbf{P}(\mathbf{x}) \rightarrow \mathbf{Q}(\mathbf{x}) \wedge(\mathbf{x})(\mathbf{Q}(\mathbf{x}) \rightarrow \mathbf{R}(\mathbf{x})) \Rightarrow(\mathbf{x})(\mathbf{P}(\mathbf{x}) \rightarrow \mathbf{R}(\mathbf{x})$
