



Strong Induction

In this form, we use the same basic step as before, but we use a different inductive step. We assume that $P(j)$ is true for $j=1, 2, \dots, k$ and show that $P(k+1)$ must also be true based on this assumption. This is called Strong induction (second principle of Mathematical induction).

Basic step: The proposition $P(1)$ is shown to be true.

Inductive step: It is shown that

$[P(1) \wedge P(2) \wedge \dots \wedge P(k)] \rightarrow P(k+1)$
is true for every positive integer k .



① Show that if n is an integer greater than 1, then ' n ' can be written as the product of primes.

Let $P(n)$ be the proposition that n can be written as the product of primes.

Basic step : $P(2)$ is true, since 2 can be written as the product of one prime.

Inductive step : Assume that $P(j)$ is true for all positive integer j with $j \leq k$. To complete the inductive step, it must be shown that $P(k+1)$ is true under this assumption.

There are 2 cases to consider, namely

Case : 1 If $(k+1)$ is prime, we immediately see that $P(k+1)$ is true.

Case : 2 If $(k+1)$ is composite

Then it can be written as product of two positive integer a and b with $2 \leq a < b \leq k+1$.

By the induction hypothesis, both a and b can be written as the product of primes. Thus, if $(k+1)$

is composite it can be written as the product of primes.



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