

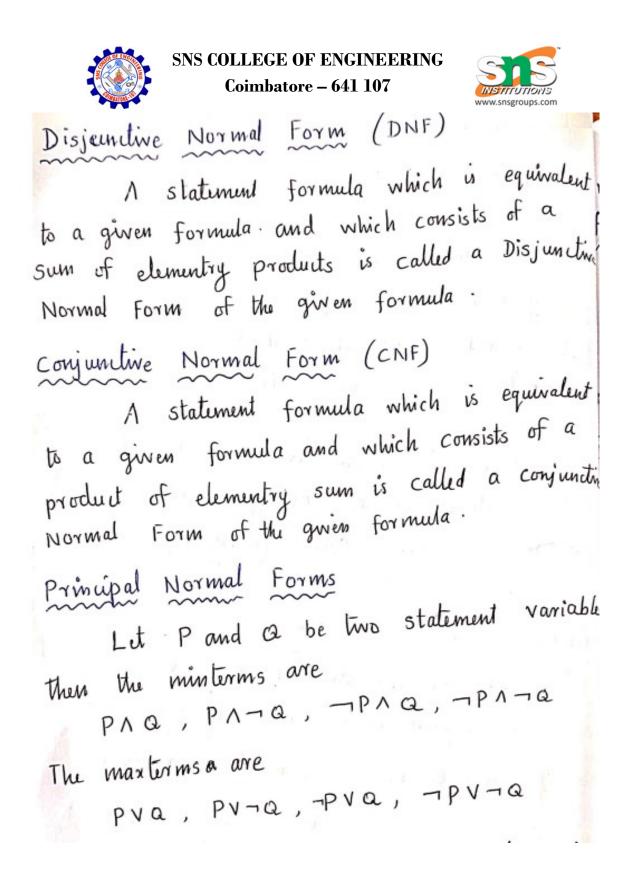
## SNS COLLEGE OF ENGINEERING Coimbatore - 641 107



## **TOPIC:3- Normal Forms**

If we write the given statement in a porticular form (interms of A, V and -), then it is called Normal form: is called Normal form: Elementry Product Elementry Product A product of the statement variables and her negations in a formula is called Elementry products: For example, let P and Q be any two atomic variables · Then possible elementry products are P, Q, -AP, -AQ, -PAQ, -QAP, PA-P, QA-Q PA-PAQ.

A sum of the two statement variables and their negation is called Elementry sum. Let P and Q be any two atomic variables. Then P, Q, PVQ, ¬PVQ, PV¬Q, PV¬PVQ We some examples of elementry sum.



**SNS COLLEGE OF ENGINEERING** Coimbatore - 641 107 Principal Normal Forms Let P and Q be two statement variable then the minterms are PAQ, PANQ, MPAQ, MPANQ The maxterms a are PVQ, PV-Q, -PVQ, -PV-Q Prinipal Disjunctive Normal Forms (PDNF) For a given statement formula, an equivalu formula consisting of disjunction of minterms is called a Prinipal Disjunctive Normal Forms Prinipal conjunctive Normal Forms (PCNF) For a given statement formula, an equivalent formula consisting of conjunction of maxterms only is known as its Principal conjuction vormal form (PCNF).

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$$(P \rightarrow R) \land (Q \leftrightarrow P)$$
  
 $(P \rightarrow R) \land (Q \leftrightarrow P)$   
 $(P \rightarrow R) \land (Q \leftrightarrow P) \land (P \rightarrow Q)$   
 $(P \rightarrow R) \land (Q \rightarrow P) \land (P \rightarrow Q)$   
 $(P \rightarrow R \lor R) \land (P (Q \land P) \land (P \rightarrow Q))$   
 $(P \lor R \lor (Q \land Q)) \land (P \rightarrow Q)$   
 $(P \lor R \lor (Q \land Q)) \land (P \lor Q \lor (R \land R)) \land (P \lor Q \lor (R \land R))$   
 $(P \lor Q \lor (R \land Q)) \land (P \lor Q \lor (R \land R))$   
 $(P \lor Q \lor (R \land Q)) \land (P \lor Q \lor (R \land R))$   
 $(P \lor Q \lor (R \land Q)) \land (P \lor Q \lor (R \land R))$   
 $(P \lor Q \lor (R \land Q)) \land (P \lor Q \lor R) \land (P \lor Q \lor R)$   
 $\land (P \lor Q \lor R) \land (P \lor Q \lor R) \land (P \lor Q \lor R)$   
 $\land (P \lor Q \lor R) \land (P \lor Q \lor R) \land (P \lor Q \lor R)$   
 $\land (P \lor Q \lor R) \land (P \lor Q \lor R) \land (P \lor Q \lor R)$   
 $\land (P \lor Q \lor R) \land (P \lor Q \lor R) \land (P \lor Q \lor R)$   
 $\land (P \lor Q \lor R) \land (P \lor Q \lor R) \land (P \lor Q \lor R)$   
 $\land (P \lor Q \lor R) \land (P \lor Q \lor R) \land (P \land Q \lor R)$   
 $\land (P \lor Q \lor R) \land (P \lor Q \lor R) \land (P \land Q \lor R)$   
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 $\land (P \lor Q \lor R) \land (P \land Q \lor R) \land (P \land Q \lor R)$   
 $\land (P \land Q \lor R) \land (P \land Q \lor R) \land (P \land Q \land R)$   
 $\land (P \land Q \lor R) \land (P \land Q \land R) \land (P \land Q \land R)$   
 $\land (P \land Q \lor R) \land (P \land Q \land R) \land (P \land Q \land R)$   
 $\land (P \land Q \land R) \land (P \land Q \land R) \land (P \land Q \land R)$   
 $\land (P \land Q \land R) \land (P \land Q \land R) \lor (P \land Q \land R)$   
 $\land (P \land Q \land R) \lor (P \land Q \land R) \lor (P \land Q \land R)$   
 $\land (P \land Q \land R) \lor (P \land Q \land R) \lor (P \land Q \land R)$   
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 $\land (P \land Q \land R) \lor (P \land Q \land R) \lor (P \land Q \land R)$   
 $\land (P \land Q \land R) \lor (P \land Q \land R) \lor (P \land Q \land R)$   
 $\land (P \land Q \land R) \lor (P \land Q \land R) \lor (P \land Q \land R)$   
 $\land (P \land Q \land R) \lor (P \land Q \land R) \lor (P \land Q \land R)$ 



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2. Obtain the principal disjunctive and conjunctive  
hormal forms 
$$(P \rightarrow (aAR)) \land (\neg P \rightarrow (\neg aA \neg R))$$
  
5  $\iff (P \rightarrow (aAR)) \land (\neg P \rightarrow (\neg aA \neg R))$   
( $\neg P \lor (aAR)) \land (\neg P \lor (\neg aA \neg R))$   
( $\neg P \lor a) \land (\neg P \lor R) \land (P \lor \neg a) \land (P \lor \neg R)$   
( $\neg P \lor a) \land (\neg P \lor R) \land (P \lor \neg a) \land (P \lor \neg R)$   
( $\neg P \lor a \lor (R \land \neg R)) \land (P \lor \neg a \lor F) \land (P \lor \neg R \lor F)$   
( $\neg P \lor a \lor (R \land \neg R)) \land (P \lor \neg R \lor (aA \neg a))$   
 $\land (P \lor a \lor (R \land \neg R)) \land (P \lor \neg R \lor (aA \neg a))$   
 $\land (P \lor a \lor (R \land \neg R)) \land (P \lor \neg R \lor (aA \neg a))$   
 $\land (P \lor a \lor R) \land (\neg P \lor a \lor \neg R) \land (\neg P \lor R \lor a) \land (P \lor \neg R \lor a)$   
 $\land (P \lor \neg a \lor R) \land (P \lor \neg R \lor A) \land (P \lor \neg R \lor a)$   
 $\land (P \lor \neg a \lor R) \land (P \lor \neg R \lor a) \land (P \lor \neg a \lor R)$   
 $\land (P \lor \neg a \lor R) \land (P \lor a \lor \neg R) \land (P \lor \neg a \lor R) \land (P \lor \neg a \lor R)$   
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R) \land (P \lor \neg a \lor R)$   
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R) \land (P \lor \neg a \lor R)$   
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R) \land (P \lor \neg a \lor R)$   
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R) \land (P \lor \neg a \lor R)$   
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R)$   
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 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R)$   
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R)$   
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R)$   
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R)$   
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R)$   
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R)$   
 $\land (P \land a \lor \neg R) \land (P \lor a \lor R)$   
 $\land (P \lor a \lor \neg R) \land (P \lor a \lor R)$   
 $\land (P \lor a \lor \neg R) \land (P \lor a \lor R)$   
 $\land (P \lor a \lor \neg R) \land (P \lor a \lor R)$   
 $\land (P \lor a \lor \neg R) \land (P \lor a \lor R)$ 



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Obtain 3. PDNF of (PAQ) V(-PAR) V (QAR). the

P	a	R	Рла	P	-PAF	QAR	(PAQ) V (¬PAR) V (QAR)	Min term
Т	T	Т	Т	F	F	T	Ð	PAQAR
τ	T	F	Т	F	F	F	T	PAQATR
Т	F	Т	F	F	F	F	F	
T	F	F	F	F	F ]	F	F	
F	T	Т	F	T	T	T	①	- PAQAR
F	T	F	F	г	F	F	F	
F	F	T	F	т	T	F	$\Theta$	TPATGAR
F	F	F	F	T	F	F	F	