

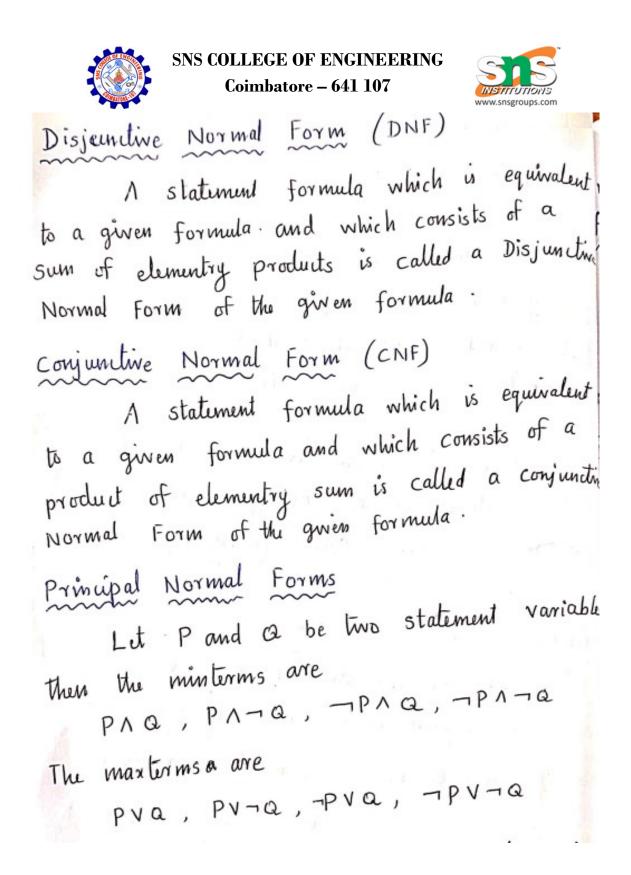
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TOPIC:3- Normal Forms

If we write the given statement in a porticular form (interms of A, V and -), then it is called Normal form: is called Normal form: Elementry Product Elementry Product A product of the statement variables and her negations in a formula is called Elementry products: For example, let P and Q be any two atomic variables · Then possible elementry products are P, Q, -AP, -AQ, -PAQ, -QAP, PA-P, QA-Q PA-PAQ.

A sum of the two statement variables and their negation is called Elementry sum. Let P and Q be any two atomic variables. Then P, Q, PVQ, ¬PVQ, PV¬Q, PV¬PVQ We some examples of elementry sum.



SNS COLLEGE OF ENGINEERING Coimbatore - 641 107 Principal Normal Forms Let P and Q be two statement variable then the minterms are PAQ, PANQ, MPAQ, MPANQ The maxterms a are PVQ, PV-Q, -PVQ, -PV-Q Prinipal Disjunctive Normal Forms (PDNF) For a given statement formula, an equivalu formula consisting of disjunction of minterms is called a Prinipal Disjunctive Normal Forms Prinipal conjunctive Normal Forms (PCNF) For a given statement formula, an equivalent formula consisting of conjunction of maxterms only is known as its Principal conjuction vormal form (PCNF).

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$$(P \rightarrow R) \land (Q \leftrightarrow P)$$

 $(P \rightarrow R) \land (Q \leftrightarrow P)$
 $(P \rightarrow R) \land (Q \leftrightarrow P) \land (P \rightarrow Q)$
 $(P \rightarrow R) \land (Q \rightarrow P) \land (P \rightarrow Q)$
 $(P \rightarrow R \lor R) \land (P (Q \land P) \land (P \rightarrow Q))$
 $(P \lor R \lor (Q \land Q)) \land (P \rightarrow Q)$
 $(P \lor R \lor (Q \land Q)) \land (P \lor Q \lor (R \land R)) \land (P \lor Q \lor (R \land R))$
 $(P \lor Q \lor (R \land Q)) \land (P \lor Q \lor (R \land R))$
 $(P \lor Q \lor (R \land Q)) \land (P \lor Q \lor (R \land R))$
 $(P \lor Q \lor (R \land Q)) \land (P \lor Q \lor (R \land R))$
 $(P \lor Q \lor (R \land Q)) \land (P \lor Q \lor R) \land (P \lor Q \lor R)$
 $\land (P \lor Q \lor R) \land (P \lor Q \lor R) \land (P \lor Q \lor R)$
 $\land (P \lor Q \lor R) \land (P \lor Q \lor R) \land (P \lor Q \lor R)$
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 $\land (P \land Q \land R) \lor (P \land Q \land R) \lor (P \land Q \land R)$



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2. Obtain the principal disjunctive and conjunctive
hormal forms
$$(P \rightarrow (aAR)) \land (\neg P \rightarrow (\neg aA \neg R))$$

5 $\iff (P \rightarrow (aAR)) \land (\neg P \rightarrow (\neg aA \neg R))$
($\neg P \lor (aAR)) \land (\neg P \lor (\neg aA \neg R))$
($\neg P \lor a) \land (\neg P \lor R) \land (P \lor \neg a) \land (P \lor \neg R)$
($\neg P \lor a) \land (\neg P \lor R) \land (P \lor \neg a) \land (P \lor \neg R)$
($\neg P \lor a \lor (R \land \neg R)) \land (P \lor \neg a \lor F) \land (P \lor \neg R \lor F)$
($\neg P \lor a \lor (R \land \neg R)) \land (P \lor \neg R \lor (aA \neg a))$
 $\land (P \lor a \lor (R \land \neg R)) \land (P \lor \neg R \lor (aA \neg a))$
 $\land (P \lor a \lor (R \land \neg R)) \land (P \lor \neg R \lor (aA \neg a))$
 $\land (P \lor a \lor R) \land (\neg P \lor a \lor \neg R) \land (\neg P \lor R \lor a) \land (P \lor \neg R \lor a)$
 $\land (P \lor \neg a \lor R) \land (P \lor \neg R \lor A) \land (P \lor \neg R \lor a)$
 $\land (P \lor \neg a \lor R) \land (P \lor \neg R \lor a) \land (P \lor \neg a \lor R)$
 $\land (P \lor \neg a \lor R) \land (P \lor a \lor \neg R) \land (P \lor \neg a \lor R) \land (P \lor \neg a \lor R)$
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R) \land (P \lor \neg a \lor R)$
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R) \land (P \lor \neg a \lor R)$
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R) \land (P \lor \neg a \lor R)$
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R) \land (P \lor \neg a \lor R)$
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 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R)$
 $\land (P \lor \neg a \lor \neg R) \land (P \lor a \lor R)$
 $\land (P \land a \lor \neg R) \land (P \lor a \lor R)$
 $\land (P \lor a \lor \neg R) \land (P \lor a \lor R)$
 $\land (P \lor a \lor \neg R) \land (P \lor a \lor R)$
 $\land (P \lor a \lor \neg R) \land (P \lor a \lor R)$
 $\land (P \lor a \lor \neg R) \land (P \lor a \lor R)$



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Obtain 3. PDNF of (PAQ) V(-PAR) V (QAR). the

| P | a | R | Рла | P | -PAF | QAR | (PAQ) V (¬PAR) V (QAR) | Min term |
|---|---|---|-----|---|------|-----|------------------------------|----------|
| Т | T | Т | Т | F | F | T | Ð | PAQAR |
| τ | T | F | Т | F | F | F | T | PAQATR |
| Т | F | Т | F | F | F | F | F | |
| T | F | F | F | F | F] | F | F | |
| F | T | Т | F | T | T | T | ① | - PAQAR |
| F | T | F | F | г | F | F | F | |
| F | F | T | F | т | T | F | Θ | TPATGAR |
| F | F | F | F | T | F | F | F | |