

# UNIT II

# ARITHMETIC OPERATIONS

**Addition and subtraction of signed numbers** – Design of fast adders –  
Multiplication of positive numbers - Signed operand multiplication- fast  
multiplication – Integer division – Floating point numbers and operations

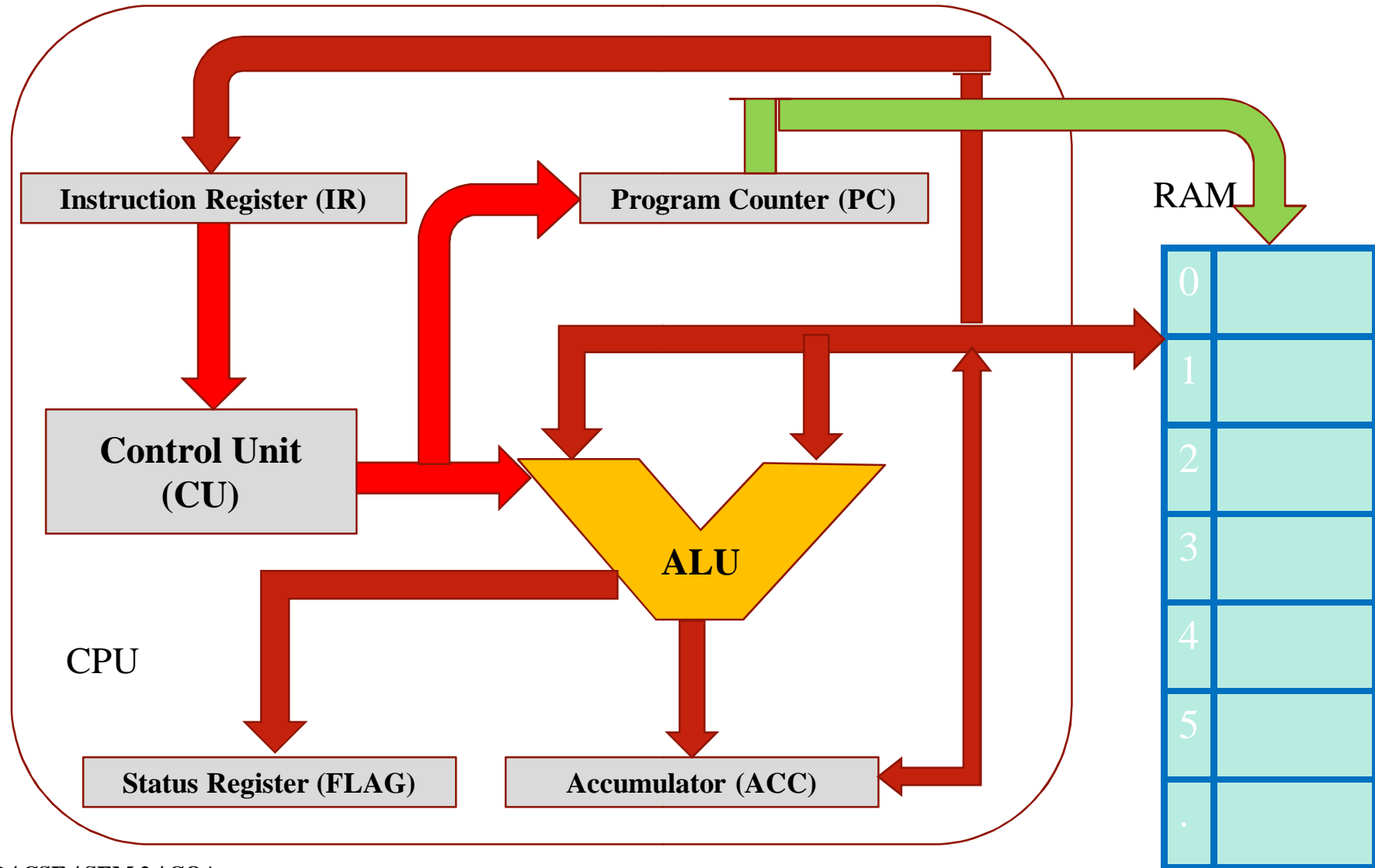


# Recall Unit I

- Functional units
- Basic operational concepts
- Bus Structures
- Performance
- Memory locations and addresses
- Memory operations
- Instruction and Instruction sequencing
- Addressing modes
- Assembly language



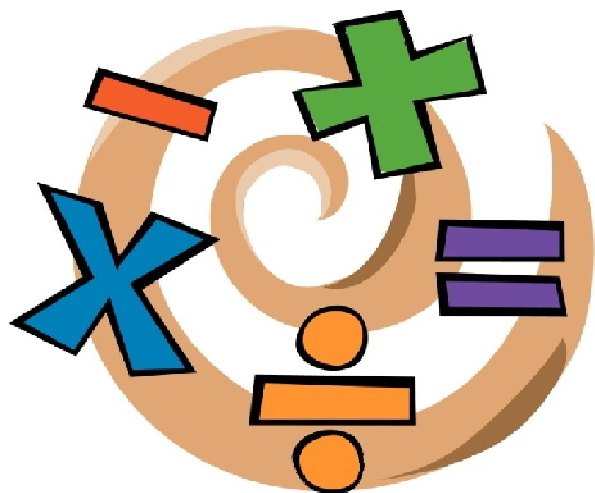
# Recall Unit I





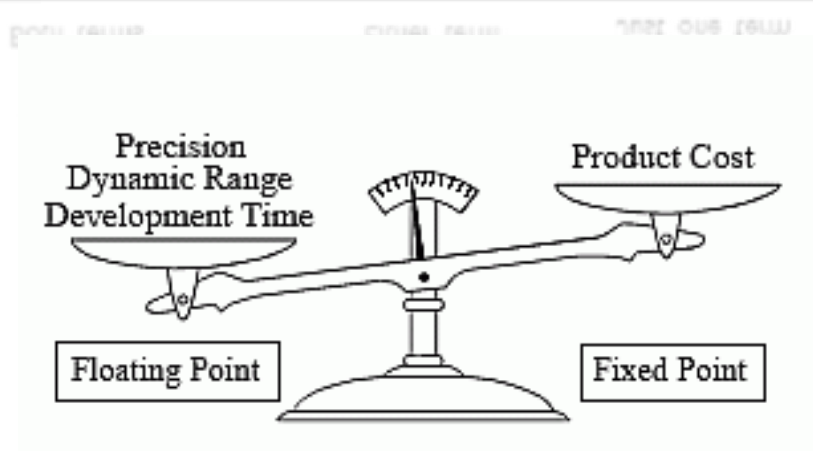
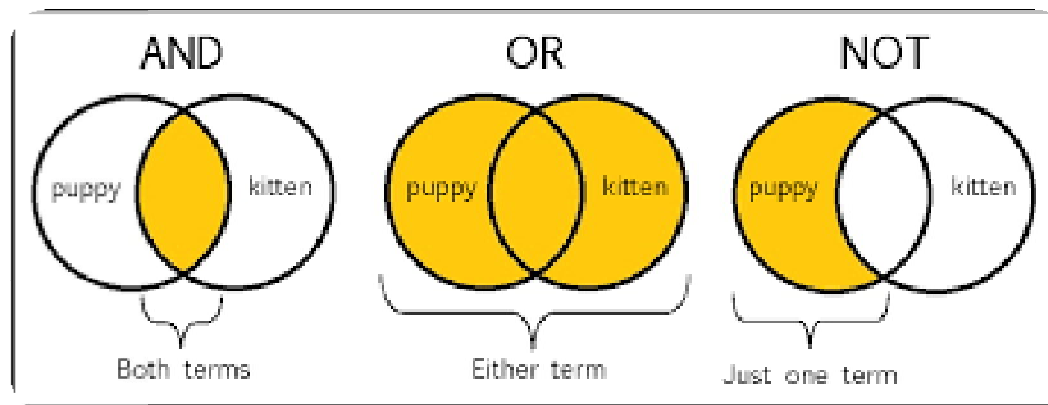
# Introduction

## Basic Arithmetic Operation

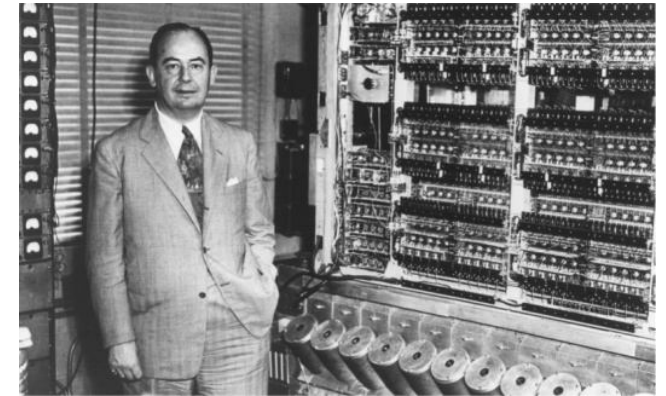


## Representation

## Logical Operation



# What's ALU?



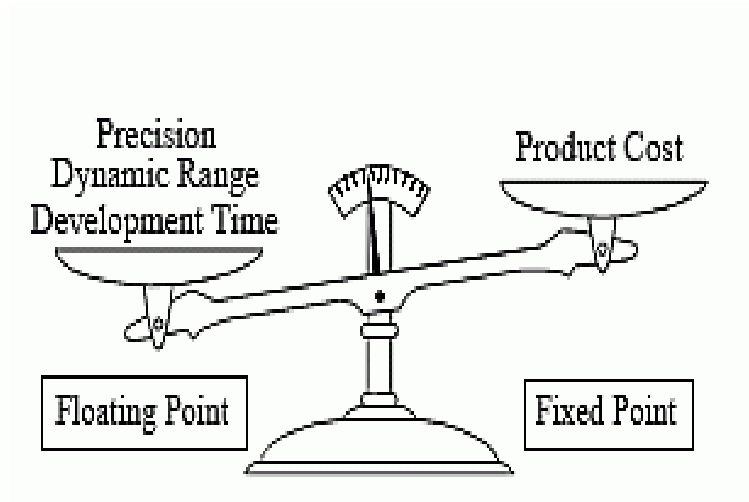
- Stands for **A**rithmetic and **L**ogic **U**nit
- Performs Arithmetic (Add, Sub, . . .) and Logical (AND, OR, NOT) operations.
- John Von Neumann proposed the ALU in 1945 when he was working on EDVAC (**E**lectronic **D**iscrete **V**ariable **A**utomatic Computer)



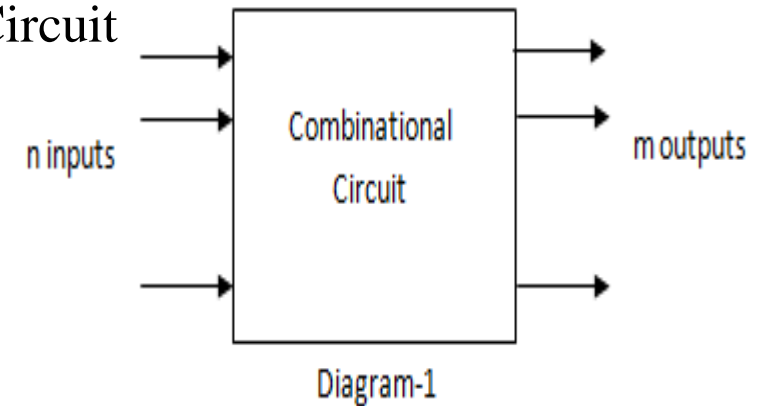
# Arithmetic and Logical Unit

## Circuit Design

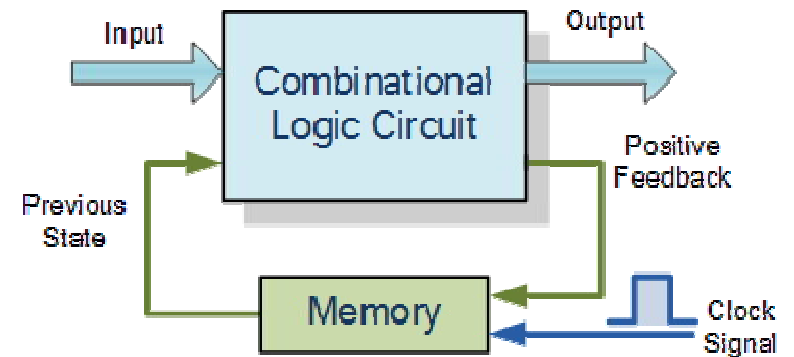
### Operations



### Combinational Logic Circuit



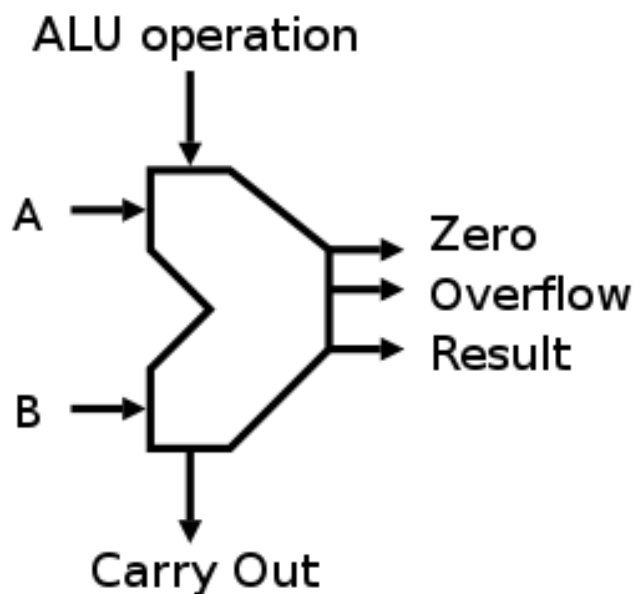
### Sequential Logic Circuit



# Typical Schematic Symbol of an ALU

Basic Hardware Components

AND Gates , OR Gates, Inverters & Multiplexers



ALU control lines	Function
0000	AND
0001	OR
0010	add
0110	subtract
0111	set on less than
1100	NOR



# 1 Bit ALU

## Logic Gates

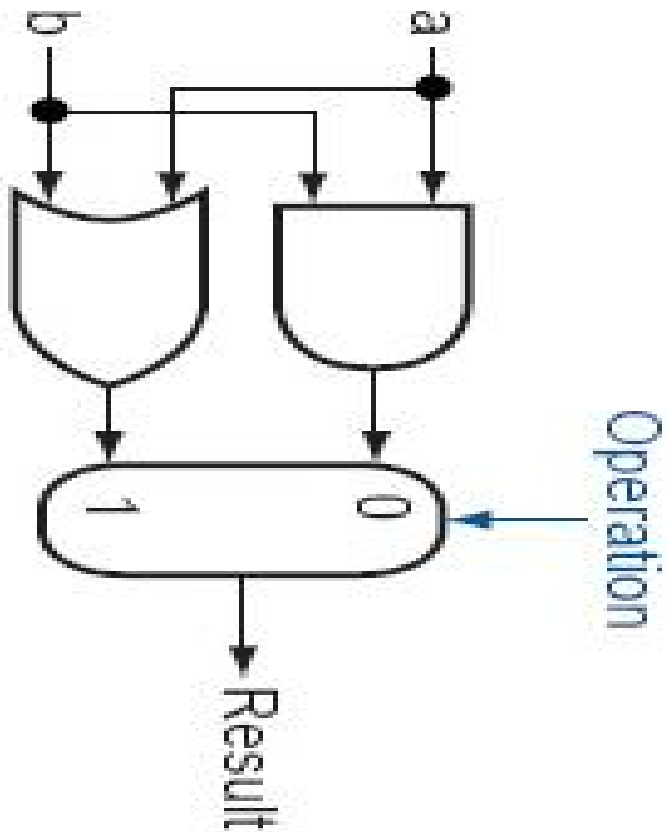
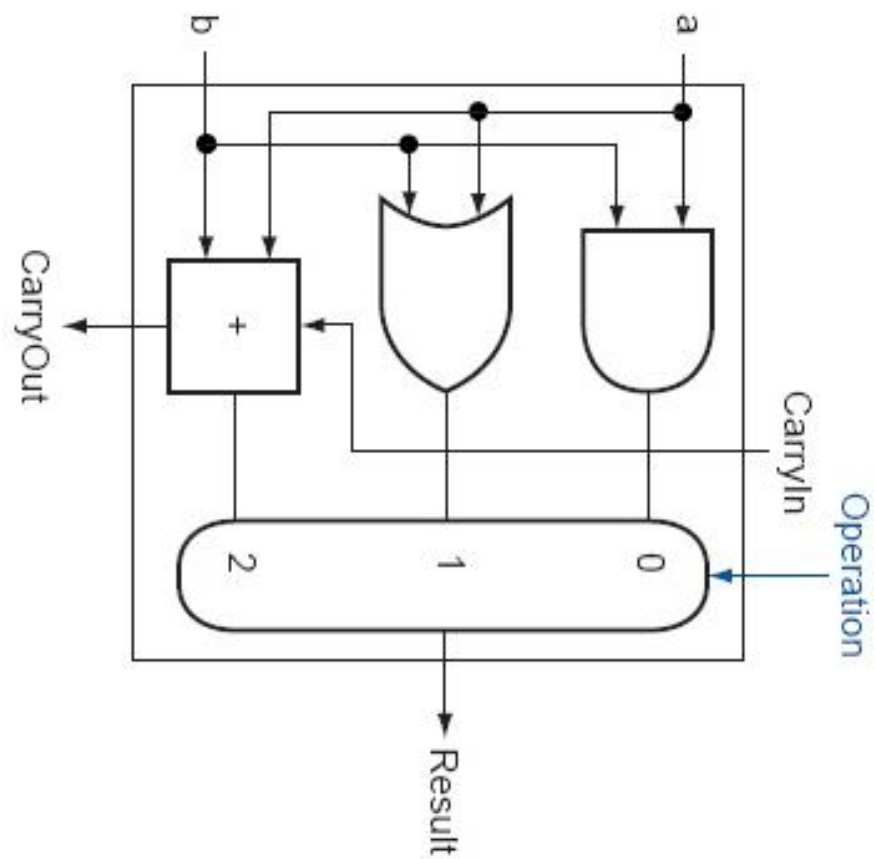
Name	NOT	AND	NAND	OR	NOR	XOR	XNOR																																																																																																
Alg. Expr.	$\bar{A}$	$AB$	$\overline{AB}$	$A+B$	$\overline{A+B}$	$A \oplus B$	$\overline{A \oplus B}$																																																																																																
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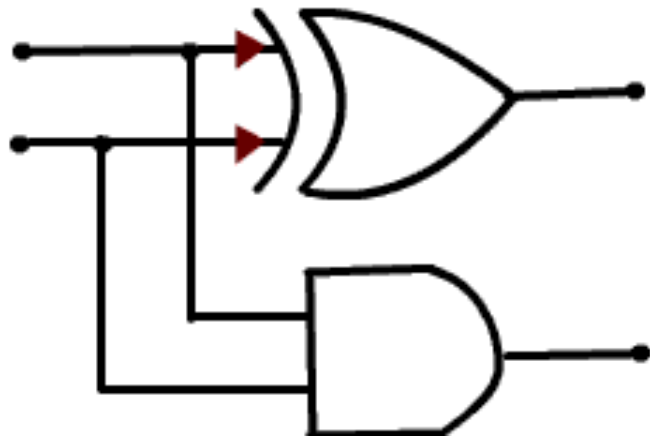
# 1 Bit ALU

Data line and control Line



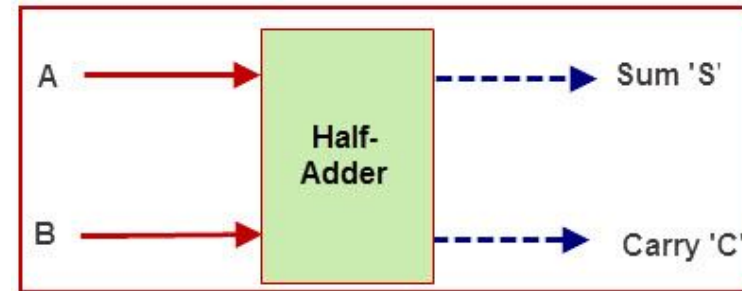


# Logic specification for a stage of Binary Addition <sup>10/18</sup>



$$S = A \oplus B$$

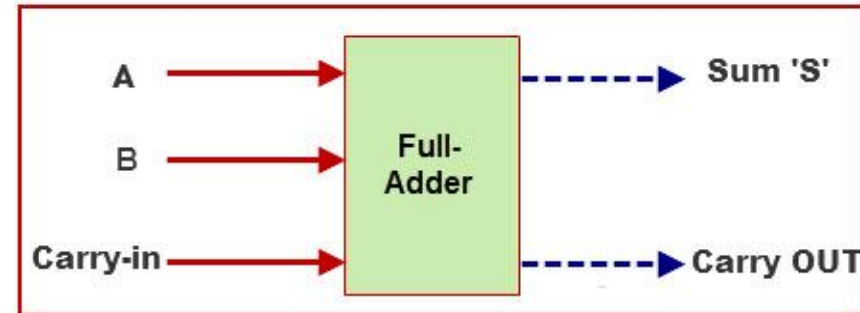
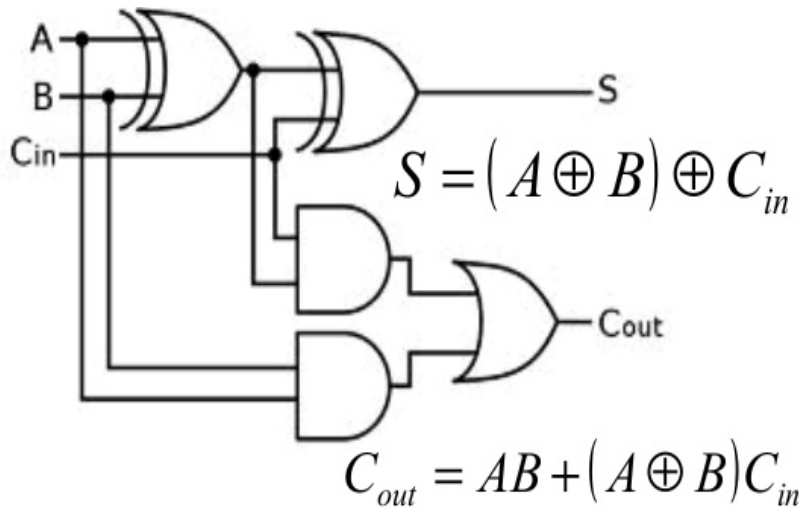
$$C = A \cdot B$$



INPUTS		OUTPUTS	
A	B	SUM	CARRY
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1



# Logic specification for a stage of Binary Addition <sup>11/18</sup>



INPUTS			OUTPUT	
A	B	C-IN	C-OUT	S
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1



# EXECUTION & OPERATION INSIDE PROCESSOR

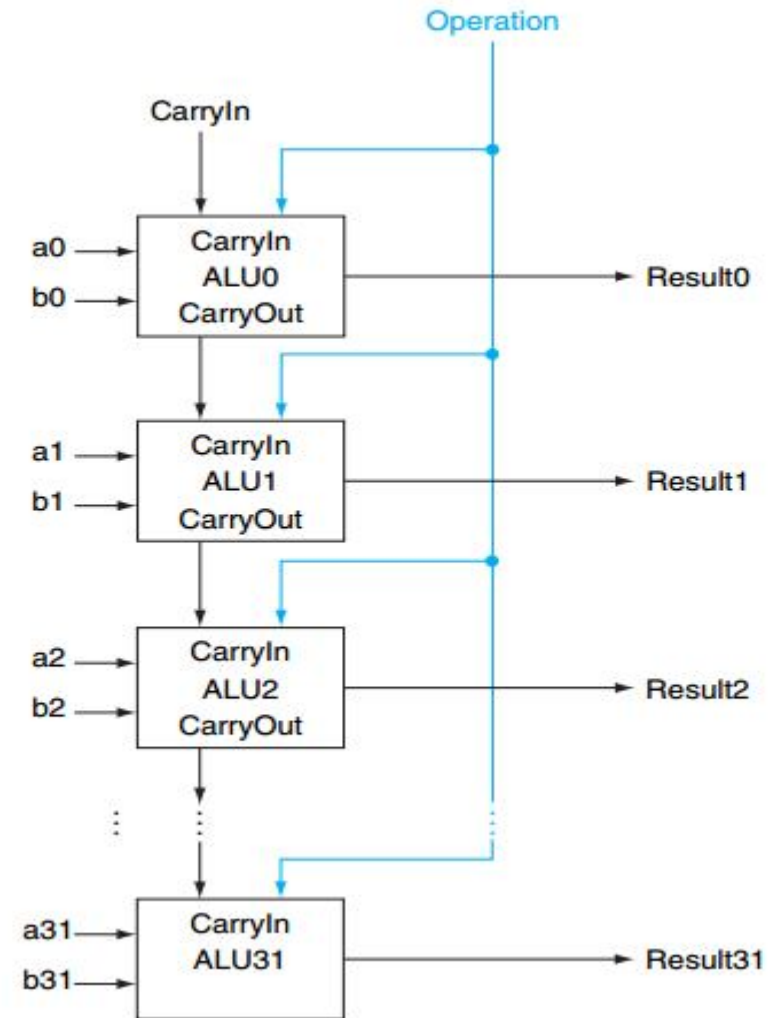
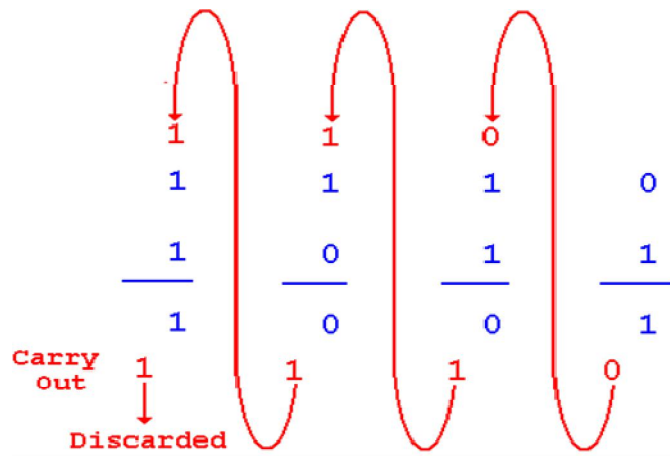
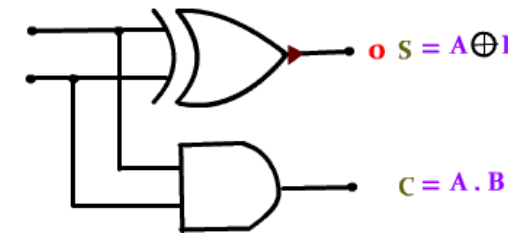
## 32 BIT ALU

Half-Adder

A	B	S	C
0	0	0	

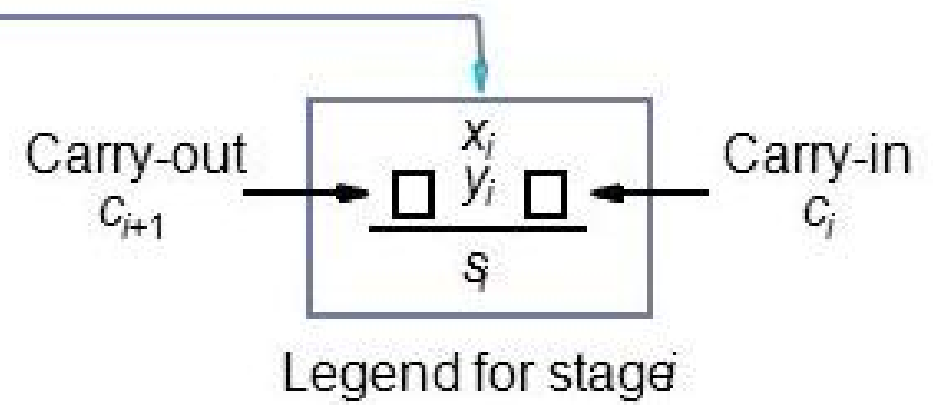
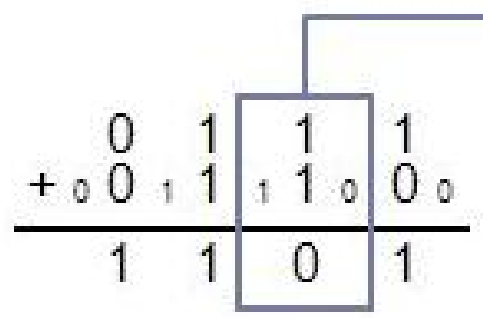
INPUT

A 0  
B 0



# Example for Binary Addition

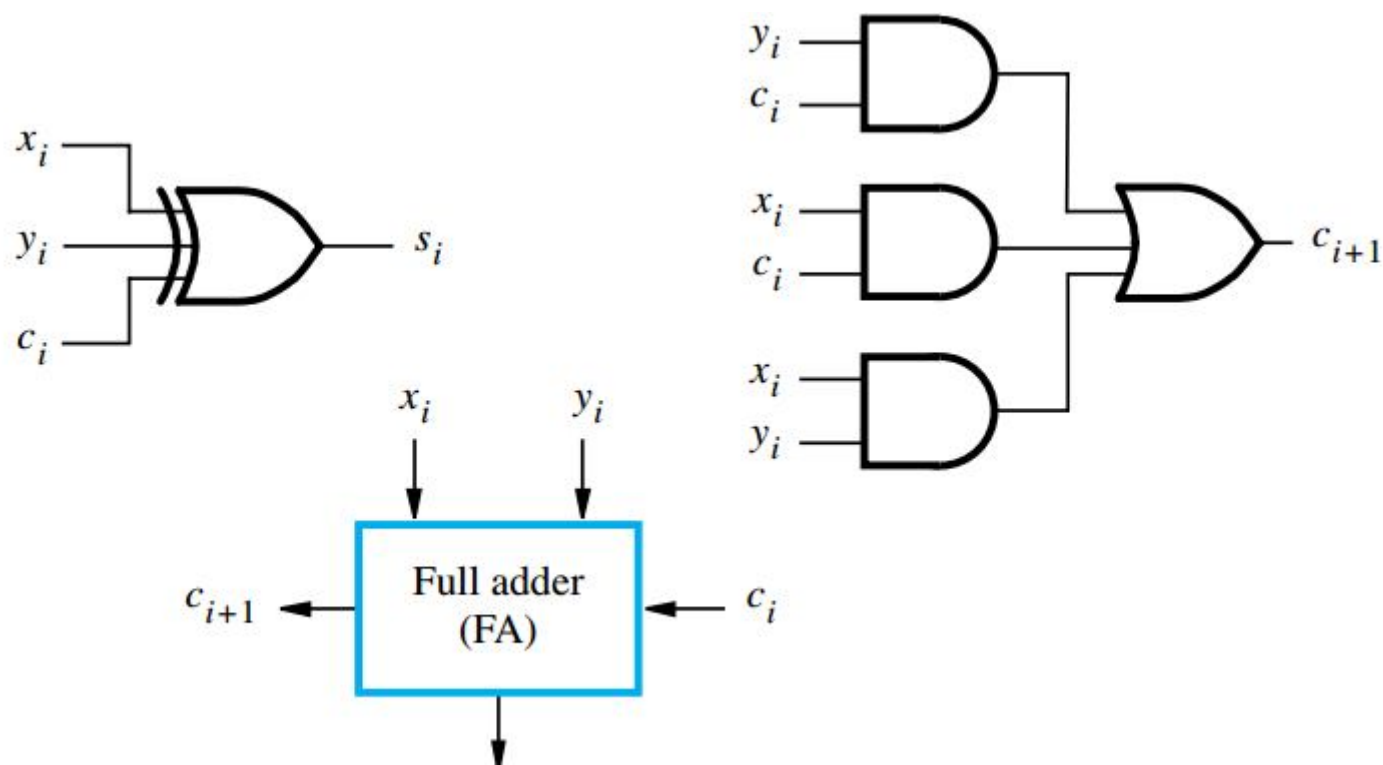
$$\begin{array}{r} X \\ + Y \\ \hline Z \end{array} = \begin{array}{r} 7 \\ + 6 \\ \hline 13 \end{array}$$



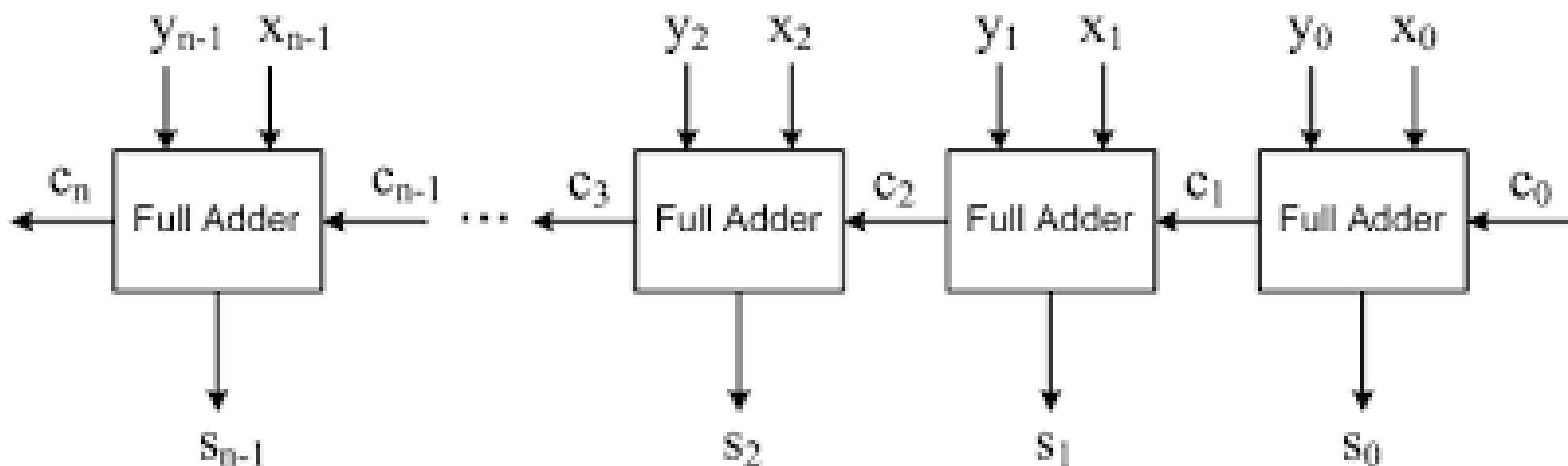


# Addition and Subtraction Logic Unit

Logic for Single Stage

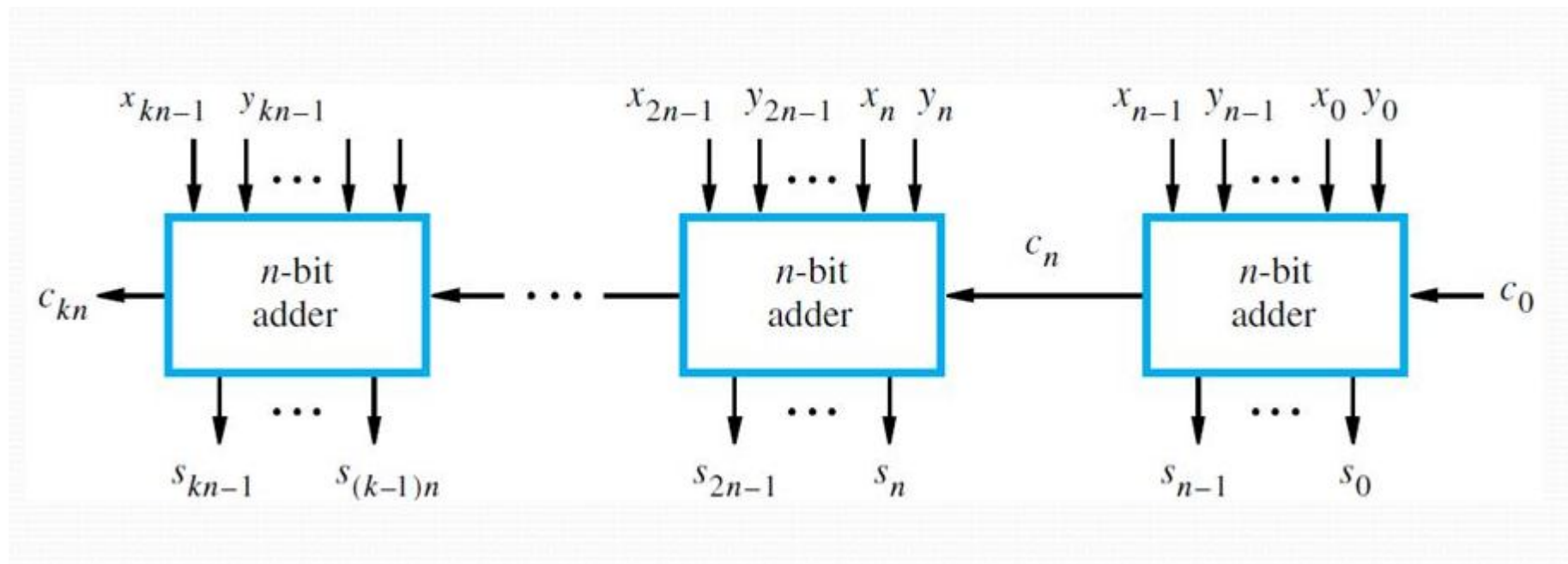


# n bit ripple carry adder



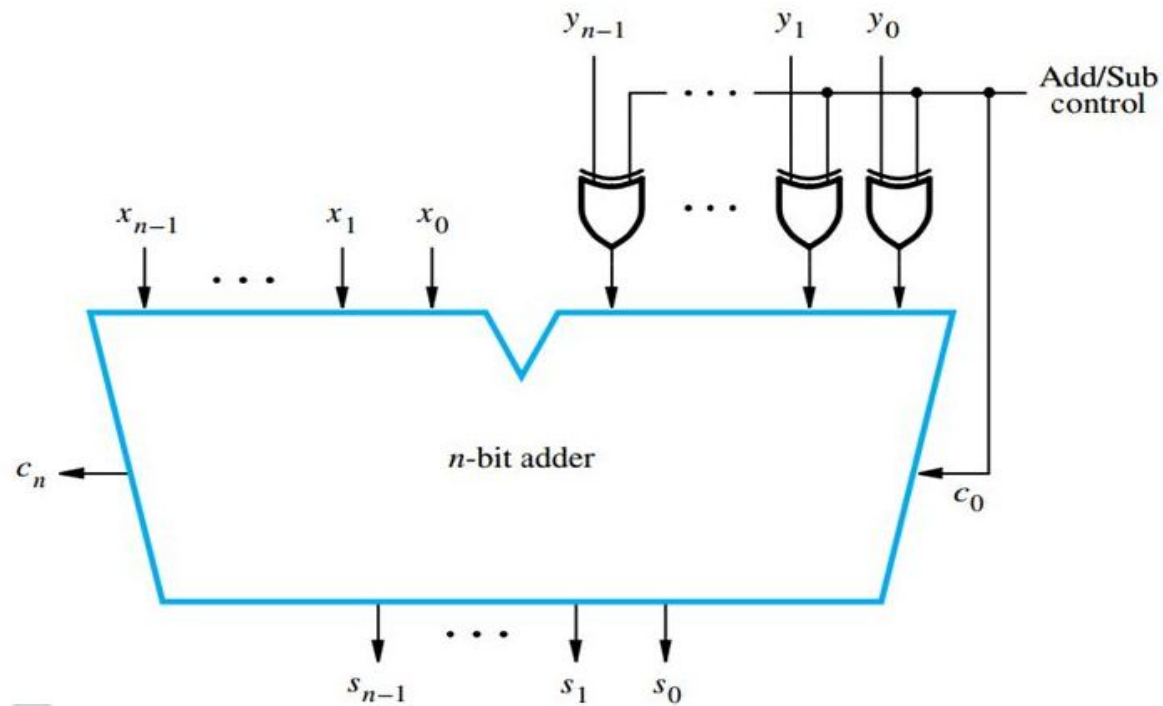


# cascaded k n bit adders





# Binary addition and subtraction <sup>17/18</sup> logic network



- Addition  $\rightarrow$  Add/sub control = 0.
- Subtraction  $\rightarrow$  Add/sub control = 1



# Assessment



A	B	Output
0	0	0
0	1	1
1	0	1
1	1	1



A	B	Output
0	0	0
0	1	0
1	0	0
1	1	1



A	B	Output
0	0	1
0	1	0
1	0	0
1	1	0



A	B	Output
0	0	1
0	1	0
1	0	0
1	1	0



A	B	Output
0	0	1
0	1	1
1	0	1
1	1	0



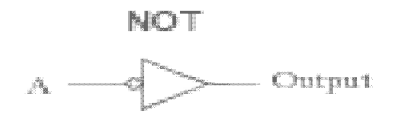
A	B	Output
0	0	1
0	1	1
1	0	1
1	1	0



A	B	Output
0	0	0
0	1	1
1	0	1
1	1	0

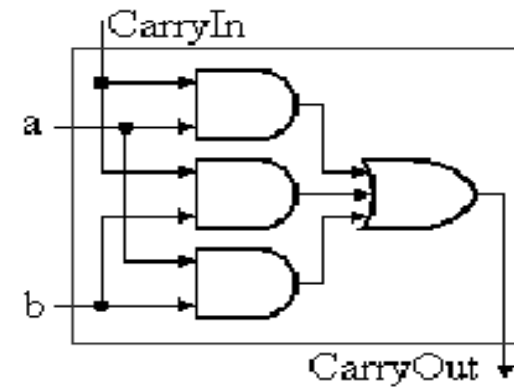
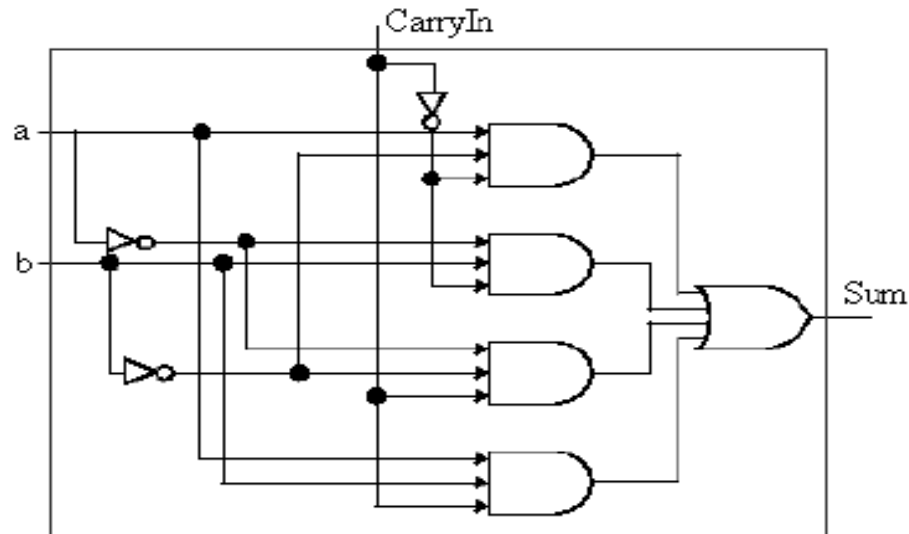


A	B	Output
0	0	1
0	1	0
1	0	0
1	1	1



A	Output
0	1
1	0





$$\text{Carryout} = (b \cdot \text{CarryIn}) + (a \cdot \text{CarryIn}) + (a \cdot b)$$

$$\text{Sum} = (a \cdot b' \cdot \text{CarryIn}') + (a' \cdot b \cdot \text{CarryIn}') + (a' \cdot b' \cdot \text{CarryIn}) + (a \cdot b \cdot \text{CarryIn})$$

## TEXT BOOK

Carl Hamacher, Zvonko Vranesic and Safwat Zaky, "Computer Organization", McGraw-Hill, 6th Edition 2012.

## REFERENCES

1. David A. Patterson and John L. Hennessey, "Computer organization and design", MorganKauffman ,Elsevier, 5th edition, 2014.
2. William Stallings, "Computer Organization and Architecture designing for Performance", Pearson Education 8th Edition, 2010
3. John P.Hayes, "Computer Architecture and Organization", McGraw Hill, 3rd Edition, 2002
4. M. Morris R. Mano "Computer System Architecture" 3rd Edition 2007
5. David A. Patterson "Computer Architecture: A Quantitative Approach", Morgan Kaufmann; 5th edition 2011

# THANK YOU