



Unit-4

DYNAMICS OF PARTICLES



Particle Kinematics



Dynamics = Kinematics + Kinetics

Kinematics: The *description* of motion (**position, velocity, acceleration, time**) without regard to forces.

Kinetics: Determining the *forces* (**based on $F=ma$**) associated with motion.

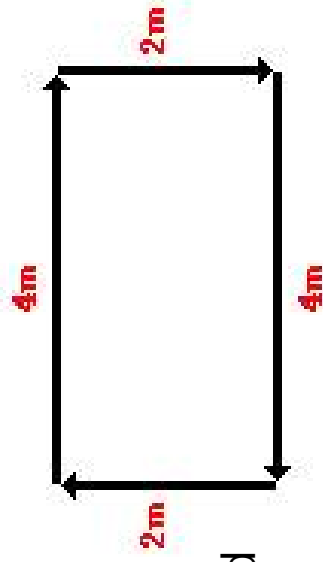


Distance and Displacement

Distance is a scalar quantity that refers to "how much ground an object has covered" during its motion.

Displacement is a vector quantity that refers to "how far out of place an object is"; it is the object's overall change in position.

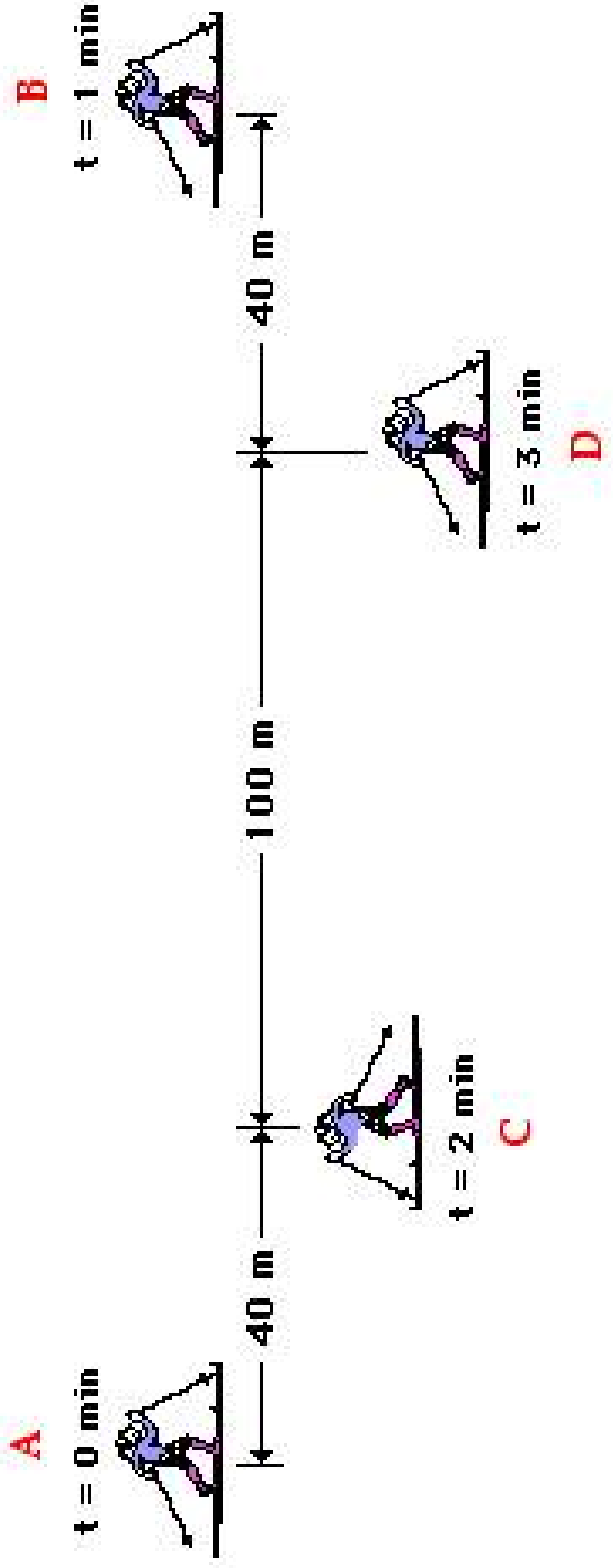
To test your understanding of this distinction, consider the motion depicted in the diagram below. A person walks 4 meters East, 2 meters South, 4 meters West, and finally 2 meters North.



He covered 12 meters of ground
(distance = 12 m)

There is no displacement for
his motion
(displacement = 0 m)

Use the diagram to determine the resulting displacement and the distance traveled by the skier during these three minutes.



The skier covers a distance of

$$(180 \text{ m} + 140 \text{ m} + 100 \text{ m}) = 420 \text{ m}$$

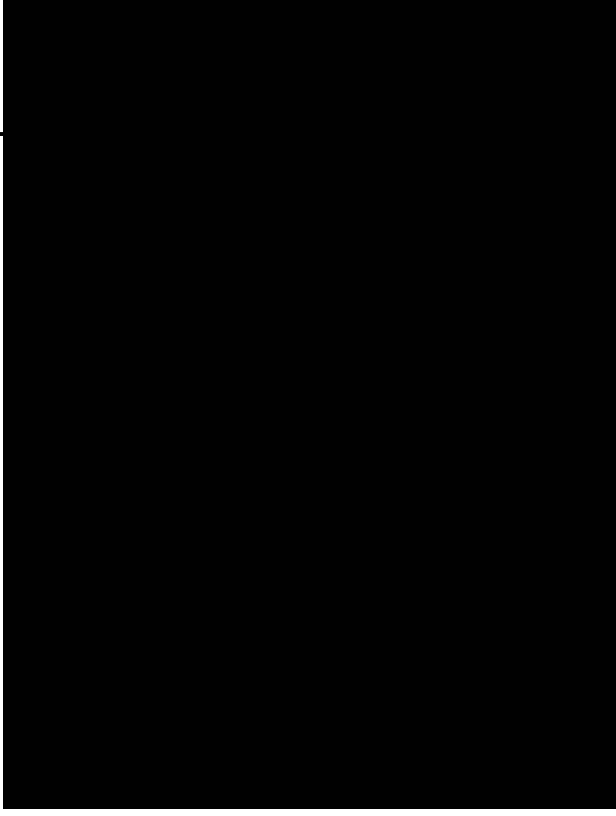
has a displacement of **140 m, rightward**.



Speed and Velocity



- **Speed** is a scalar quantity that refers to "how fast an object is moving."
- Speed can be thought of as the rate at which an object covers distance.
- A fast-moving object has a high speed and covers a relatively large distance in a short amount of time.
- Contrast this to a slow-moving object that has a low speed; it covers a relatively small amount of distance in the same amount of time.
- An object with no movement at all has a zero speed.

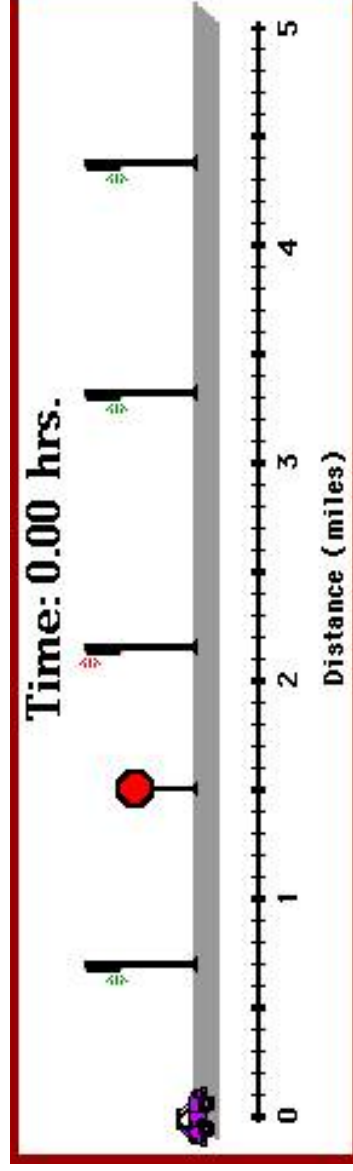




- **Velocity** is a [vector quantity](#) that refers to "the rate at which an object changes its position."



- Imagine a person moving rapidly - one step forward and one step back - always returning to the original starting position.
- While this might result in a frenzy of activity, it would result in a zero velocity.
- Because the person always returns to the original position, the motion would never result in a change in position.
- Since velocity is defined as the rate at which the position changes, this motion results in zero velocity.





The average speed during the course of a motion is often computed using the following formula:

$$\text{Average Speed} = \frac{\text{Distance Traveled}}{\text{Time of Travel}}$$

In contrast, the average velocity is often computed using this formula

$$\text{Average Velocity} = \frac{\Delta \text{ position}}{\text{time}} = \frac{\text{displacement}}{\text{time}}$$

An object moving with a constant speed of 6 m/s

Time (s)	Position (m)
0	0
1	6
2	12
3	18
4	24

An object moving with a changing speed

Time (s)	Position (m)
0	0
1	1
2	4
3	9
4	16

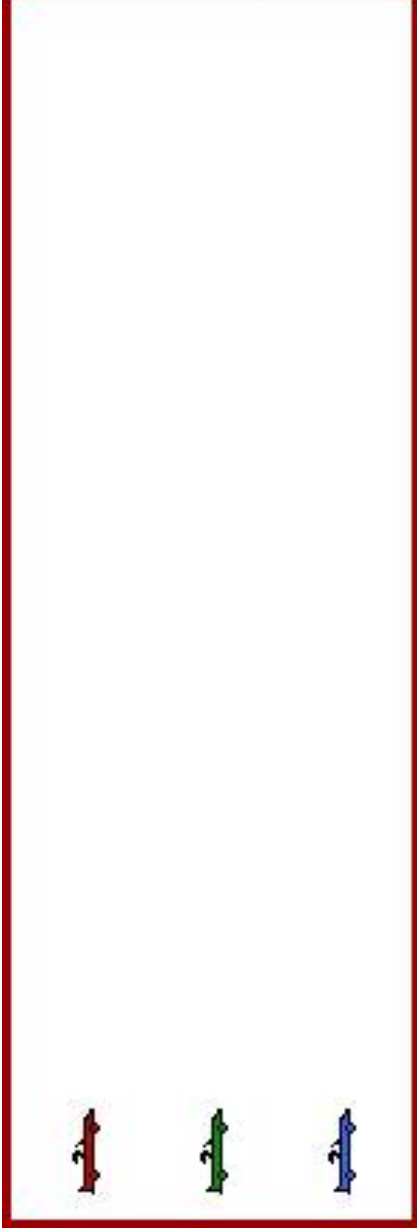
$$v = ds/dt$$



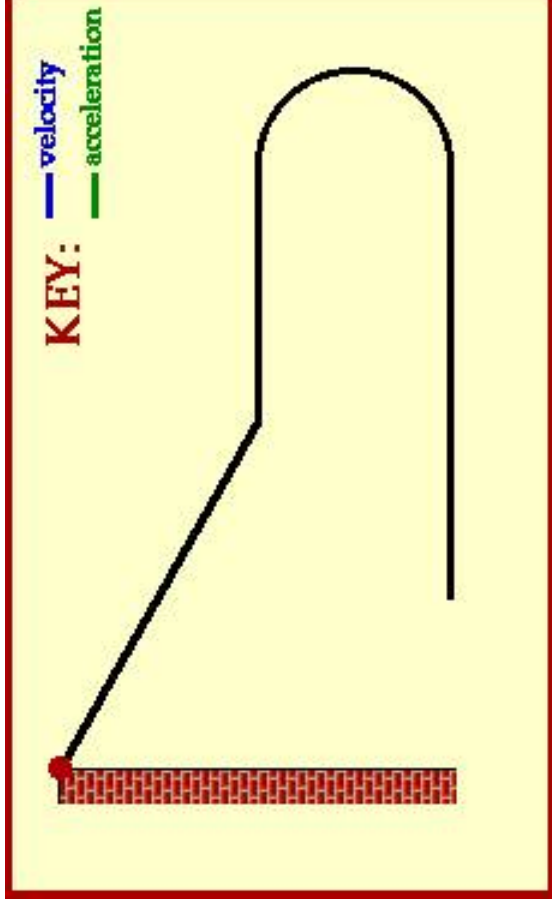
Acceleration



Acceleration is a vector quantity that is defined as the rate at which an object changes its velocity. An object is accelerating if it is changing its velocity. $\mathbf{a} = \mathbf{dv}/\mathbf{dt}$



1. Which car or cars (red, green, and/or blue) are undergoing an acceleration?
2. Which car (red, green, or blue) experiences the greatest acceleration?



An object moving with a constant speed of 6 m/s

Time (s)	Position (m)
0	0
1	6
2	12
3	18
4	24

An object moving with a changing speed

Time (s)	Position (m)
0	0
1	1
2	4
3	9
4	16



Kinematic Variables



Particle kinematics involves describing a particle's **position, velocity and acceleration versus time.**

Kinematic Variables		
Description	Vector	Scalar
Position	\vec{r}	s
Velocity	\vec{v}	v
Acceleration	\vec{a}	a
Time	t	t