



FUNCTIONAL DEPENDENCY

- It requires that the value for a certain set of attributes determines uniquely the value for another set of attributes.
- In a given relation R, X and Y are attributes. Attributes Y is functionally dependent on attribute X if each value of X determines exactly one value of Y, which is represented as

$$X \rightarrow Y$$

$X \rightarrow Y$ does not imply $Y \rightarrow X$

Marks \rightarrow Grade, Reg.No \rightarrow Name



Closure set of Functional Dependency

- The closure set is a set of all functional dependencies implied by a given set F .
- It is denoted by F^+ .



Closure set of Functional Dependency

➤ Armstrong's Axioms:

R. No	Name	Marks	Dept	Couse
1	A	78	CS	C1
2	B	60	EE	C1
3	A	78	CS	C2
4	B	60	EE	C3
5	C	80	IT	C2
6	D	80	EC	C4



Closure set of Functional Dependency

➤ Armstrong's Axioms:

- Reflection: if $X \twoheadrightarrow Y$, then $X \rightarrow Y$
- Augmentation: if $X \rightarrow Y$, then $XZ \rightarrow YZ$
- Transitivity: if $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$
- Decomposition: If $X \rightarrow YZ$, then $X \rightarrow Y$ and $X \rightarrow Z$
- Union: If $X \rightarrow Y$ and $X \rightarrow Z$, then $X \rightarrow YZ$
- Pseudotransitivity: If $X \rightarrow Y$ and $WY \rightarrow Z$, then $WX \rightarrow Z$



Closure set of Functional Dependency

- Compute the closure of the following set of functional dependencies for a relation schema $R(A, B, C, D, E)$, $F = \{A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A\}$ and Find the candidate key.



FUNCTIONAL DEPENDENCY

- Closure Dependencies:
 - F – Functional Dependencies
 - F^+ - Closure Functional Dependencies
 - X – Attributes of F
 - X^+ - Attributes of F^+
 - F covers G, if $G^+ \subset F^+$
 - F and G are equivalent if $F^+ = G^+$



FUNCTIONAL DEPENDENCY

- Minimal Cover – a set of F of FD is a set of G of FD such that:
 - Every dependencies in G is of the form $X \rightarrow A$, where a is a single attribute.
 - The closure F^+ is equal to the closure G^+ .



FUNCTIONAL DEPENDENCY



- Types:
 - Full functional dependency
 - Partial functional dependency
 - Transitive functional dependency



FUNCTIONAL DEPENDENCY

- Types - Full functional dependency
 - In a relation R, X and Y are attributes. X functionally determines Y. Subset of X should not functionally determine Y.
 - Marks cannot be determined either by student_no or course_no alone. It can be determined only using student_no and course_no together.
 - Marks is fully functionally dependent on {student_no, course_no}
 - RegisterNo. -> Name



FUNCTIONAL DEPENDENCY

- Types - Partial functional dependency
 - Attribute Y is partially dependent on the attribute X only if it is dependent on a subset of attribute X.
 - For example course_name, Instructor_name are partially dependent on composite attributes {student_no, course_no} because course_no alone defines course_name, Instructor_name.
 - (RegisterNo., Gender) -> Name



FUNCTIONAL DEPENDENCY

➤ Types - Transitive Dependencies functional dependency

➤ X, Y and Z are 3 attributes in the relation R.

$X \rightarrow Y, Y \rightarrow Z, X \rightarrow Z$

➤ For example, grade depends on marks and in turn mark depends on {student_no course_no}, hence Grade depends fully transitively on {student_no & course_no}.



FUNCTIONAL DEPENDENCY

➤ Types - Transitive Dependencies functional dependency

➤ X, Y and Z are 3 attributes in the relation R.

$X \rightarrow Y, \quad Y \rightarrow Z, X \rightarrow Z$

➤ RegisterNo. \rightarrow HoD,

➤ RegisterNo. \rightarrow Deptid,

➤ Deptid \rightarrow HoD



FUNCTIONAL DEPENDENCY

- Uses:
- Test relations to see if they are legal under a given set of functional dependencies.
- Specify constraints on the set of legal relations
- A specific instance of a relation schema must satisfy a functional dependency even if the functional dependency does not hold on all legal instances.



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Thank You.....